



Runtime Enforcement of Timed Properties

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INRIA Rennes, Team: Sumo, Project: ANR Vacsim

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Jury

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Traditional design and verification

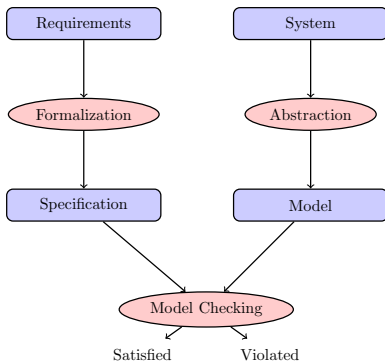
- Cannot guarantee absence of errors.
- Late detection of errors (some times after deployment).
- Inadequate for safety-critical systems.

Some software bugs



- Ariane 5, Therac-25, Toyota's ETCS.

Formal verification techniques



- *Spec*: Set of requirements/properties (LTL, CTL, ...).
- Abstraction of system/program (automata, ...).
- Static: Model checking, static analysis.
- Dynamic: Testing, **runtime verification/enforcement**.

Runtime verification and enforcement (monitors)

Runtime verification and enforcement:

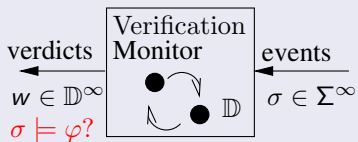
- Monitor execution of a system (e.g., trace, log, messages).
- No system model.
- A formal requirement: Property φ .

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Runtime verification



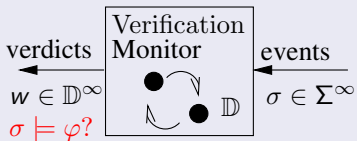
- Input: stream of events.
- Output: stream of **verdicts**.
- Does the run satisfy the property?

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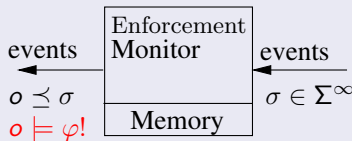
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Runtime verification



- Input: stream of events.
- Output: stream of **verdicts**.
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Runtime enforcement



- Input: stream of events.
- Output: stream of **events** (**should** satisfy the property).
- Allowed to block/modify input.

Motivations for *timed* enforcement

Specifying the timing behavior

Allowing to specify desired behaviors of a system with constraints on both the **order of events** and **timing**.

- After action “a”, action “b” should occur

Motivations for *timed* enforcement

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- After action “a”, action “b” should occur **with a delay of at least 5 time units between them**.
- The system should allow consecutive requests **with a delay of at least 10 time units between any two requests**.

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Application domains

- Real-time embedded systems, monitoring hardware failures, communication protocols, web services, etc.
- Examples of monitor usage:
 - firewall to prevent DOS attacks ensuring minimal delay between input events;
 - checking pre-conditions of a service in web applications.

Related work on monitoring

Runtime enforcement of **untimed** properties

- Enforceable security policies – **F. B. Schneider et al-2000**.
- Runtime enforcement of non-safety policies – **J. Ligatti et al-2009**.
- Enforcement Monitoring wrt. the Safety-Progress Classification of Properties – **Y. Falcone et al-2010**.

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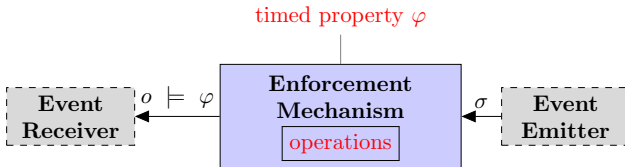
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Runtime **verification** of timed properties

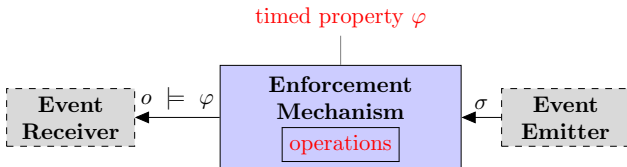
Efforts mainly to *verify* timed properties at runtime:

- Runtime verification of TLTL – [A. Bauer et al-2011](#).
- Algorithms for monitoring real-time properties – [D. Basin et al-2011](#).
- The Analog Monitoring Tool.(monitoring specifications over continuous signals) – [D. Nickovic et al-2010](#).
- Safe runtime verification of real-time properties – [C. Colombo et al](#).

Context and objectives



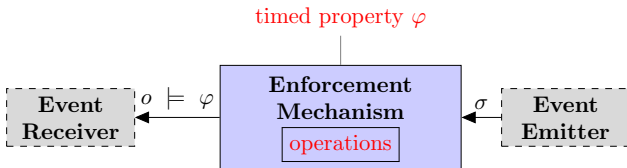
Context and objectives



Objective

- Given a timed property, synthesize **enforcement mechanism** operating at **runtime**.
- Enforcer between event emitter and event receiver.
- Reliable channels, safe communication.
- Mechanism to transform input σ in to output o such that $o \models \varphi$.

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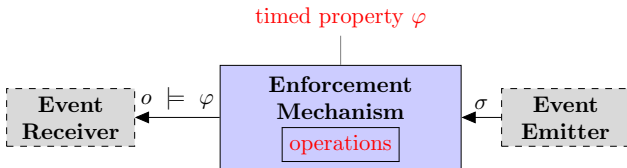
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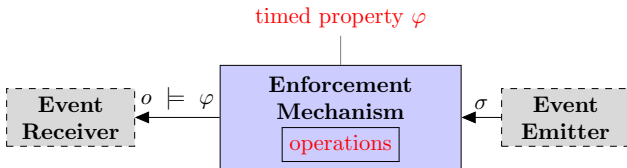
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- Power of the enforcement mechanism.

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- Expressiveness of the supported specification formalism.
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- Implementability.

Contributions

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A formal framework for runtime enforcement of timed properties

- General definitions for all regular timed properties.
- Work as **delayers**: either **increase input dates** or **suppress events** in order to satisfy the property.
- Enforcement mechanisms defined at **several abstraction levels** to ease their design and implementation.

Outline

- 1 Specifying Timed Properties
- 2 RE of Regular Timed Properties
 - Requirements on an Enforcement Mechanism
 - Functional Definition of an Enforcement Mechanism
 - Operational Description of an Enforcement Mechanism
- 3 Implementation
- 4 RE of Parametric Timed Properties
 - PTAVs
 - Runtime Enforcement of PTAVs
 - Application Domains
- 5 Conclusions and Future Work

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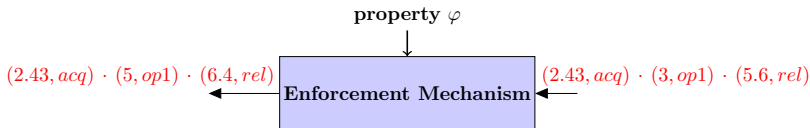
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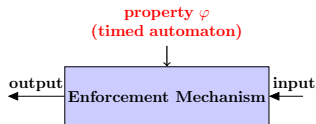
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Input/output stream of events



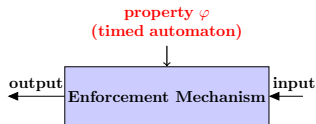
- Input/output streams of **timed events** are modelled as **timed words**.
- Given an alphabet of actions Σ ,
 - Timed word: $\sigma = (t_1, a_1) \cdot (t_2, a_2) \cdots (t_n, a_n)$ **dates** are increasing.
 - $\text{tw}(\Sigma)$: set of timed words over Σ .

Specifying timed properties



- Enforced timed property: any **regular timed language** $\varphi \subseteq \text{tw}(\Sigma)$, accepted by a **timed automaton** \mathcal{A}_φ .

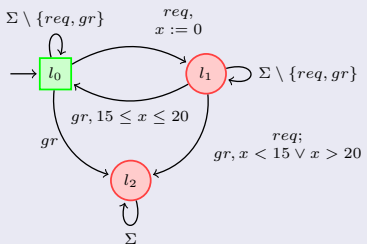
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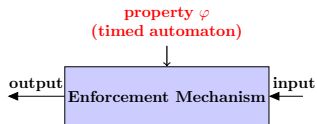
Examples: Properties specified by TAs

Regular: any property.



“Requests and grants should alternate in this order with a delay between 15 and 20 t.u between request and grant.”

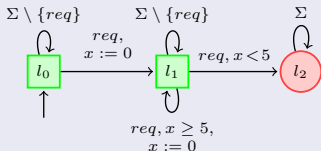
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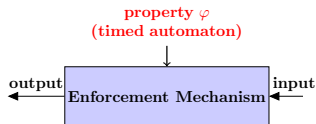
Examples: Properties specified by TAs

Safety: nothing bad should ever happen (prefix closed).



“A delay of 5 t.u. between any two requests.”

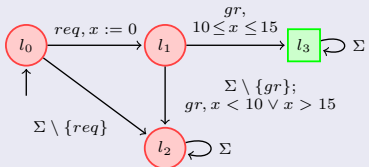
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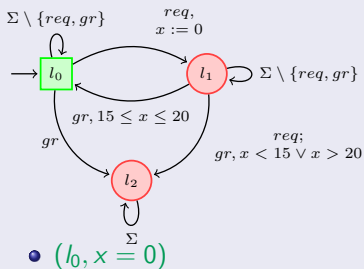
Co-safety: something good will eventually happen within a finite amount of time (extension closed).



“A request, and then a grant should arrive between 10 and 15 t.u.”

Timed automata semantics

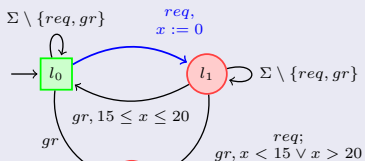
Semantics of a timed automaton



- Timed transition system.
- States of the form $q = (l, \nu)$ (location, valuation of clocks).

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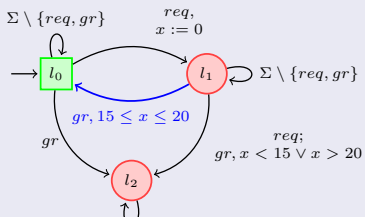


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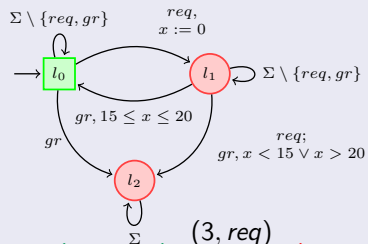


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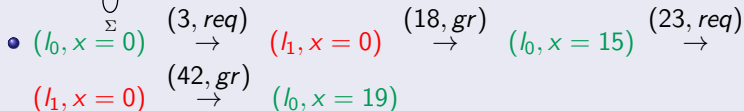
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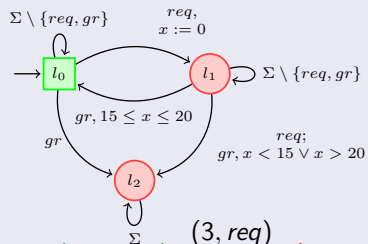


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- $(l_0, x = 0) \xrightarrow{(3, req)} (l_1, x = 0) \xrightarrow{(18, gr)} (l_0, x = 15) \xrightarrow{(23, req)}$
- $(l_1, x = 0) \xrightarrow{(42, gr)} (l_0, x = 19)$
- $(3, req) \cdot (18, gr) \cdot (23, req) \cdot (42, gr)$

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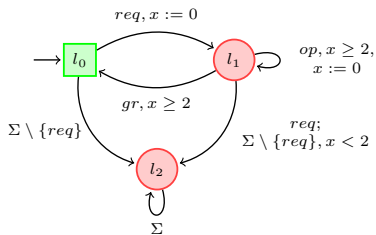
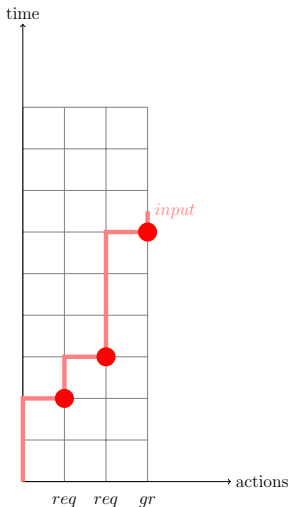
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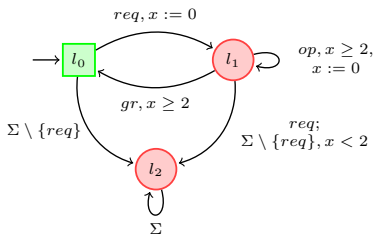
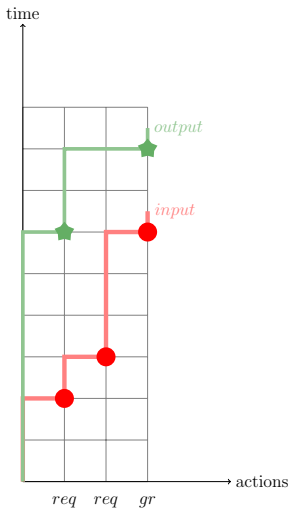
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Enforcement mechanism behavior: example



- input: $(2, req) \cdot (3, req) \cdot (6, gr)$

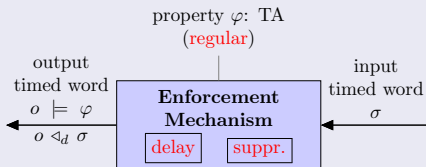
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- output: $(6, req) \cdot (8, gr)$

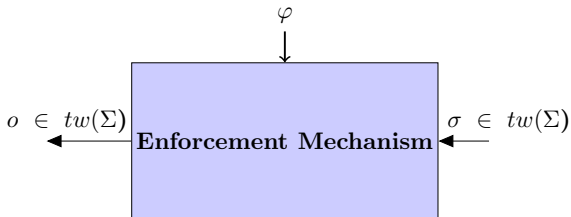
Enforcement mechanism behavior

What can an enforcement mechanism do?

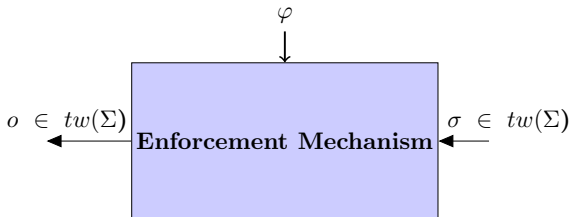


- CAN increase the dates of events to satisfy φ .
- CAN suppress events if no future can satisfy φ .

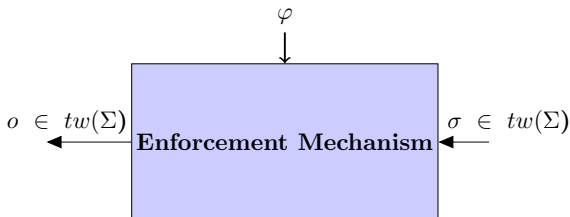
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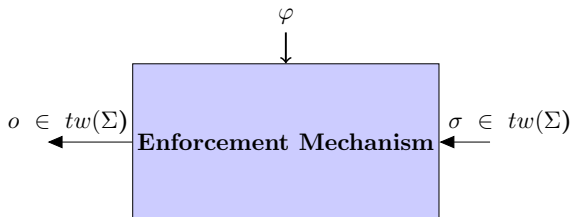


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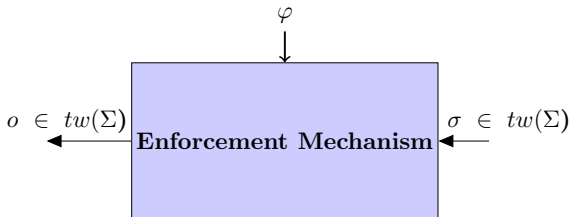
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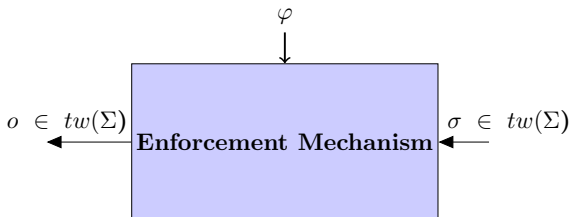
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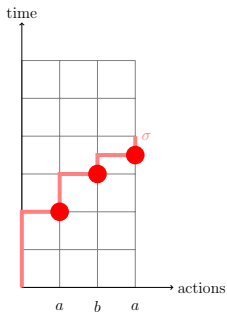
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 - runtime (online) behavior of the enforcement mechanism;
- **Implementation:** translation of the EM semantic rules into algorithms.

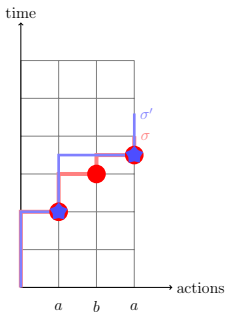
Preliminaries



Subsequence: $\sigma' \triangleleft \sigma$ if σ' obtained from σ by suppressions.

$$(2, a) \cdot (3.5, a) \triangleleft (2, a) \cdot (3, b) \cdot (3.5, a)$$

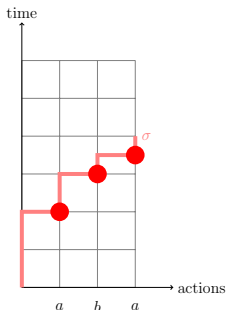
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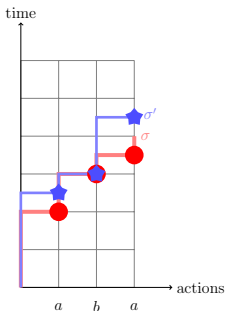
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Delaying order \succsim_d : $\sigma' \succsim_d \sigma$ if they have same untimed projections but dates in σ' exceed corresponding dates in σ .

$$(2.5, a) \cdot (3, b) \cdot (4.5, c) \succsim_d (2, a) \cdot (3, b) \cdot (3.5, a).$$

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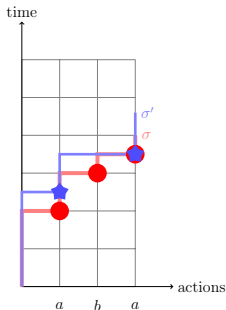
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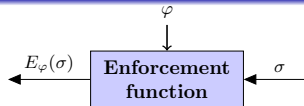
Delaying subsequence order \triangleleft_d :

$$\sigma' \triangleleft_d \sigma \stackrel{\text{def}}{=} \exists \sigma'' \in \text{tw}(\Sigma) : \sigma'' \triangleleft \sigma \wedge \sigma' \succcurlyeq_d \sigma''$$

$$(2.5, a) \cdot (3.5, a) \triangleleft_d (2, a) \cdot (3, b) \cdot (3.5, a)$$

i.e., σ' obtained from σ by first suppressing some actions, and then increasing the dates of the actions to be kept.

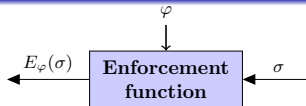
Requirements on an enforcement mechanism



$$E_\varphi : \text{tw}(\Sigma) \rightarrow \text{tw}(\Sigma)$$

Physical constraint: $\forall \sigma, \sigma' \in \text{tw}(\Sigma) : \sigma \preceq \sigma' \implies E_\varphi(\sigma) \preceq E_\varphi(\sigma')$.
 (where \preceq is the prefix ordering)
 i.e., **the output cannot be undone.**

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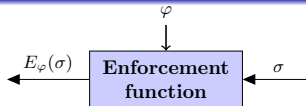
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Soundness: $\forall \sigma \in \text{tw}(\Sigma) : E_\varphi(\sigma) \models \varphi \vee E_\varphi(\sigma) = \epsilon$.

i.e., **the output either satisfies property φ , or is empty.**

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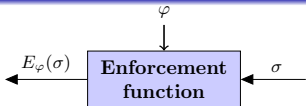
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Transparency: $\forall \sigma \in \text{tw}(\Sigma) : E_\varphi(\sigma) \triangleleft_d \sigma$.

i.e., **the output is a delaying subsequence of the input.**

Requirements on an enforcement mechanism



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 i.e., **the output cannot be undone.**

Soundness: $\forall \sigma \in \text{tw}(\Sigma) : E_\varphi(\sigma) \models \varphi \vee E_\varphi(\sigma) = \epsilon$.
 i.e., **the output either satisfies property φ , or is empty.**

Transparency: $\forall \sigma \in \text{tw}(\Sigma) : E_\varphi(\sigma) \triangleleft_d \sigma$.
 i.e., **the output is a delaying subsequence of the input.**

Additional requirements

Streaming behavior, deciding to output as soon as possible.

Optimal dates.

Optimal suppression.

Functional definition: principle

$$E_\varphi : \text{tw}(\Sigma) \rightarrow \text{tw}(\Sigma)$$

$$E_\varphi(\sigma) = \Pi_1(\text{store}_\varphi(\sigma))$$

$$\text{store}_\varphi : \text{tw}(\Sigma) \rightarrow \text{tw}(\Sigma) \times \text{tw}(\Sigma)$$

- $\text{store}_\varphi(\sigma) = (\sigma_s, \sigma_c)$ describes how the input stream is transformed:
 - σ_s : computed output (to be released);
 - σ_c : a sub-seq. of the suffix of σ for which output dates cannot be computed (e.g., co-safety, response).

Functional definition: principle

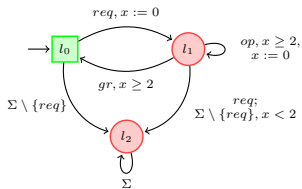
$$E_\varphi : \text{tw}(\Sigma) \rightarrow \text{tw}(\Sigma)$$

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- $\text{store}_\varphi(\sigma) = (\sigma_s, \sigma_c)$ describes how the input stream is transformed:
 - σ_s : computed output (to be released);
 - σ_c : a sub-seq. of the suffix of σ for which output dates cannot be computed (e.g., co-safety, response).
- $\text{store}_\varphi(\sigma)$ is inductively defined, has 3 cases upon reading a new event (t, a) .
 - $\sigma_c \cdot (t, a)$ can be corrected.
 - $\sigma_c \cdot (t, a)$ can never be corrected.
 - $\sigma_c \cdot (t, a)$ can be corrected in future.

Functional definition: example

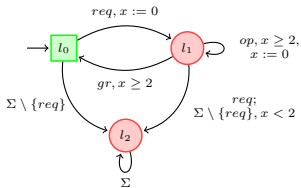

 σ

$$\sigma = \epsilon$$

$$\text{store}_\varphi(\sigma) = (\sigma_s, \sigma_c) = (\epsilon, \epsilon)$$

$$E_\varphi(\sigma) = \Pi_1(\text{store}_\varphi(\sigma)) = \sigma_s$$

Functional definition: example


 σ

$$\sigma = \epsilon$$

$$\text{store}_\varphi(\sigma) = (\sigma_s, \sigma_c) = (\epsilon, \epsilon)$$

$$E_\varphi(\sigma) = \Pi_1(\text{store}_\varphi(\sigma)) = \sigma_s$$

 $(2, req)$

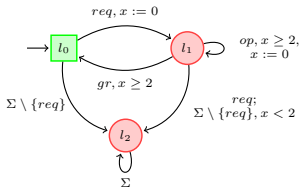
$$\sigma = (2, req)$$

$$\sigma'_c = \epsilon \cdot (2, req)$$

$$\text{store}_\varphi(\sigma) = (\sigma_s, \sigma_c) = (\epsilon, (2, req))$$

Do not output, but store!!

Functional definition: example

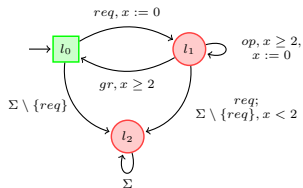

 σ
 $\sigma = \epsilon$
 $\text{store}_\varphi(\sigma) = (\sigma_s, \sigma_c) = (\epsilon, \epsilon)$
 $E_\varphi(\sigma) = \Pi_1(\text{store}_\varphi(\sigma)) = \sigma_s$
 $(2, req)$
 $\sigma = (2, req)$
 $\sigma'_c = \epsilon \cdot (2, req)$
 $\text{store}_\varphi(\sigma) = (\sigma_s, \sigma_c) = (\epsilon, (2, req))$

Do not output, but store!!

 $(3, req)$
 $\sigma = (2, req) \cdot (3, req)$
 $\sigma'_c = (2, req) \cdot (3, req)$
 $\text{store}_\varphi(\sigma) = (\sigma_s, \sigma_c) = (\epsilon, (2, req))$

Suppress!!

Functional definition: example


 σ

$$\sigma = \epsilon$$

$$\text{store}_\varphi(\sigma) = (\sigma_s, \sigma_c) = (\epsilon, \epsilon)$$

$$E_\varphi(\sigma) = \Pi_1(\text{store}_\varphi(\sigma)) = \sigma_s$$

 $(2, req)$

$$\sigma = (2, req)$$

$$\sigma'_c = \epsilon \cdot (2, req)$$

$$\text{store}_\varphi(\sigma) = (\sigma_s, \sigma_c) = (\epsilon, (2, req))$$

Do not output, but store!!

 $(3, req)$

$$\sigma = (2, req) \cdot (3, req)$$

$$\sigma'_c = (2, req) \cdot (3, req)$$

$$\text{store}_\varphi(\sigma) = (\sigma_s, \sigma_c) = (\epsilon, (2, req))$$

Suppress!!

 $(6, gr)$

$$\sigma = (2, req) \cdot (3, req) \cdot (6, gr)$$

$$\sigma'_c = (2, req) \cdot (6, gr)$$

$$\text{store}_\varphi(\sigma) = (\sigma_s, \sigma_c) = (\epsilon \cdot (6, req) \cdot (8, gr), \epsilon)$$

Delay, add to output!!

Functional definition: formal definition

$$E_\varphi : \text{tw}(\Sigma) \rightarrow \text{tw}(\Sigma)$$

$$E_\varphi(\sigma) = \Pi_1(\text{store}_\varphi(\sigma))$$

$$\text{store}_\varphi : \text{tw}(\Sigma) \rightarrow \text{tw}(\Sigma) \times \text{tw}(\Sigma)$$

$\text{store}_\varphi(\epsilon) = (\epsilon, \epsilon)$ and

$$\text{store}_\varphi(\sigma \cdot (t, a)) = \begin{cases} (\sigma_s \cdot \min \kappa_\varphi(\sigma_s, \sigma'_c), \epsilon) & \text{if } \kappa_\varphi(\sigma_s, \sigma'_c) \neq \emptyset, \\ (\sigma_s, \sigma_c) & \text{if } \kappa_{\text{pref}(\varphi)}(\sigma_s, \sigma'_c) = \emptyset, \\ (\sigma_s, \sigma'_c) & \text{otherwise,} \end{cases}$$

$\sigma'_c = \sigma_c \cdot (t, a)$

$$\kappa_\varphi(\sigma_s, \sigma'_c) = \text{CanD}(\sigma'_c) \cap \sigma_s^{-1} \cdot \varphi, \quad \kappa_{\text{pref}(\varphi)}(\sigma_s, \sigma'_c) = \text{CanD}(\sigma'_c) \cap \sigma_s^{-1} \cdot \text{pref}(\varphi)$$

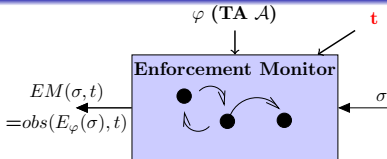
- $\text{CanD}(\sigma'_c) = \{w \in \text{tw}(\Sigma) \mid w \succ_d \sigma'_c \wedge \text{start}(w) \geq \text{end}(\sigma'_c)\}$
i.e., sequences delaying σ'_c and starting after t .
- $\sigma_s^{-1} \cdot \varphi = \{w \in \text{tw}(\Sigma) \mid \sigma_s \cdot w \models \varphi\}$.
- $\sigma_s^{-1} \cdot \text{pref}(\varphi) = \{w \in \text{tw}(\Sigma) \mid \exists w' \in \text{tw}(\Sigma) : \sigma_s \cdot w \cdot w' \models \varphi\}$.

The enforcement function satisfies the requirements

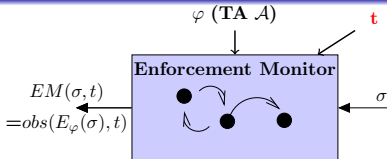
Proposition: Enforcement function vs requirements

The proposed definition of enforcement function satisfies the **physical**, **soundness**, **transparency** constraints.

Enforcement monitor



Enforcement monitor

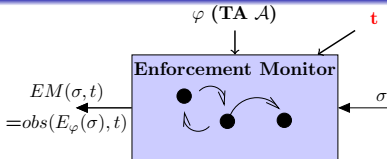


A rule-based transition system:

EM configuration: $(\sigma_{ms}, \sigma_{mc}, t, q)$

- σ_{ms} : corrected sequence (yet to be released),
- σ_{mc} : input sequence read by the EM (yet to be corrected),
- t : clock indicating the current time instant,
- q : current state of $\llbracket \mathcal{A} \rrbracket$.

Enforcement monitor



A rule-based transition system:

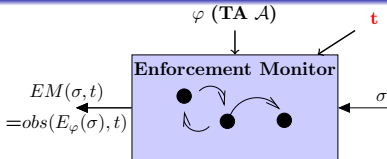
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Correspondence with E_φ

- $\text{obs}(\sigma, t)$: Maximal prefix of σ observed at t ,
- $E_\varphi(\text{obs}(\sigma, t)) = \text{obs}(E_\varphi(\text{obs}(\sigma, t)), t) \cdot \sigma_{ms}$,
- $\sigma_c = \sigma_{mc}$,
- q state reached in $\llbracket \mathcal{A} \rrbracket$ upon $E_\varphi(\text{obs}(\sigma, t))$ (corresponds to σ_s).

Enforcement monitor



A rule-based transition system:

EM configuration: $(\sigma_{ms}, \sigma_{mc}, t, q)$

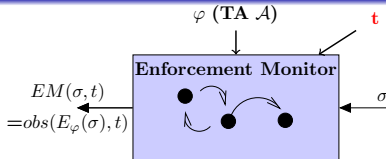
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- enforcement operations (cf. next slide)

Enforcement monitor



A rule-based transition system:

EM configuration: $(\sigma_{ms}, \sigma_{mc}, t, q)$

- σ_{ms} : corrected sequence (yet to be released),
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- $\sigma_c = \sigma_{mc}$,
- q state reached in $\llbracket \mathcal{A} \rrbracket$ upon $E_\varphi(\text{obs}(\sigma, t))$ (corresponds to σ_s).

- enforcement operations (cf. next slide)
- update function: $\text{update}(q, \sigma_{mc}, (t, a))$ (similar to store_φ , computing online using $\llbracket \mathcal{A} \rrbracket$)

Enforcement monitor: Operations

1. $store-\varphi$

when update returns **ok**, $(\sigma_{ms}, \sigma_{mc}, t, q) \xrightarrow{\mathcal{E}}^{(t,a)/store-\varphi(t,a)/\epsilon} (\sigma_{ms} \cdot w, \epsilon, t, q')$

2. $store-sup-\bar{\varphi}$

when update returns **bad**, $(\sigma_{ms}, \sigma_{mc}, t, q) \xrightarrow{\mathcal{E}}^{(t,a)/store_{sup}-\bar{\varphi}(t,a)/\epsilon} (\sigma_{ms}, \sigma_{mc}, t, q)$

3. $store-\bar{\varphi}$

when update returns **c-bad**, $(\sigma_{ms}, \sigma_{mc}, t, q) \xrightarrow{\mathcal{E}}^{(t,a)/store-\bar{\varphi}(t,a)/\epsilon} (\sigma_{ms}, \sigma_{mc} \cdot (t, a), t, q)$

Enforcement monitor: Operations

1. *store-φ*

when update returns **ok**, $(\sigma_{\text{ms}}, \sigma_{\text{mc}}, t, q) \xrightarrow{\mathcal{E}}^{(t,a)/\text{store-}\varphi(t,a)/\epsilon} (\sigma_{\text{ms}} \cdot w, \epsilon, t, q')$

2. *store-sup-φ̄*

when update returns **bad**, $(\sigma_{\text{ms}}, \sigma_{\text{mc}}, t, q) \xrightarrow{\mathcal{E}}^{(t,a)/\text{store}_{\text{sup}}-\bar{\varphi}(t,a)/\epsilon} (\sigma_{\text{ms}}, \sigma_{\text{mc}}, t, q)$

3. *store-φ̄*

when update returns **c-bad**, $(\sigma_{\text{ms}}, \sigma_{\text{mc}}, t, q) \xrightarrow{\mathcal{E}}^{(t,a)/\text{store-}\bar{\varphi}(t,a)/\epsilon} (\sigma_{\text{ms}}, \sigma_{\text{mc}} \cdot (t, a), t, q)$

4. *dump*

at t , $((t, a) \cdot \sigma'_{\text{ms}}, \sigma_{\text{mc}}, t, q) \xrightarrow{\mathcal{E}}^{\epsilon/\text{dump}(t,a)/(t,a)} (\sigma'_{\text{ms}}, \sigma_{\text{mc}}, t, q)$

Enforcement monitor: Operations

1. *store-φ*

when update returns **ok**, $(\sigma_{\text{ms}}, \sigma_{\text{mc}}, t, q) \xrightarrow{\mathcal{E}}^{(t,a)/\text{store-}\varphi(t,a)/\epsilon} (\sigma_{\text{ms}} \cdot w, \epsilon, t, q')$

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when update returns **bad**, $(\sigma_{\text{ms}}, \sigma_{\text{mc}}, t, q) \xrightarrow{\mathcal{E}}^{(t,a)/\text{store}_{\text{sup}}-\bar{\varphi}(t,a)/\epsilon} (\sigma_{\text{ms}}, \sigma_{\text{mc}}, t, q)$

3. *store-φ̄*

when update returns **c-bad**, $(\sigma_{\text{ms}}, \sigma_{\text{mc}}, t, q) \xrightarrow{\mathcal{E}}^{(t,a)/\text{store-}\bar{\varphi}(t,a)/\epsilon} (\sigma_{\text{ms}}, \sigma_{\text{mc}} \cdot (t, a), t, q)$

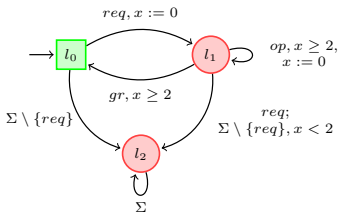
4. *dump*

at t , $((t, a) \cdot \sigma'_{\text{ms}}, \sigma_{\text{mc}}, t, q) \xrightarrow{\mathcal{E}}^{\epsilon/\text{dump}(t,a)/(t,a)} (\sigma'_{\text{ms}}, \sigma_{\text{mc}}, t, q)$

5. *idle*

when no other rule applies, $(\sigma_{\text{ms}}, \sigma_{\text{mc}}, t, q) \xrightarrow{\mathcal{E}}^{\epsilon/\text{idle}(\delta)/\epsilon} (\sigma_{\text{ms}}, \sigma_{\text{mc}}, t + \delta, q)$

Enforcement monitor: example



Operation: none

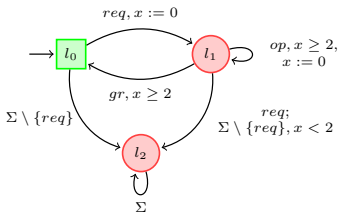
ϵ

←

t	q	σ_{ms}	σ_{mc}
0	$(l_0, 0)$	ϵ	ϵ

← $(2, req) \cdot (3, req) \cdot (6, gr)$

Enforcement monitor: example



Operation: **idle(2)**

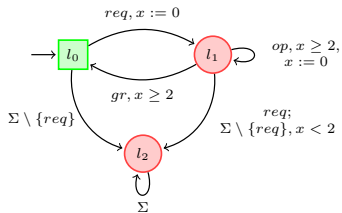
ϵ

\leftarrow

t	q	σ_{ms}	σ_{mc}
2	$(l_0, 0)$	ϵ	ϵ

$\leftarrow (2, req) \cdot (3, req) \cdot (6, gr)$

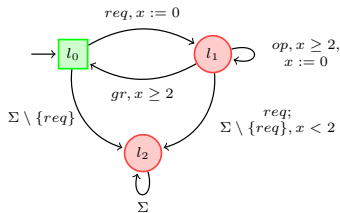
Enforcement monitor: example



Operation: $store-\bar{\varphi}$

$$\epsilon \quad \leftarrow \quad \begin{array}{c|c|c|c} t & q & \sigma_{ms} & \sigma_{mc} \\ \hline 2 & (l_0, 0) & \epsilon & (2, req) \end{array} \quad \leftarrow \quad (3, req) \cdot (6, gr)$$

Enforcement monitor: example



Operation: **idle(1)**

ϵ

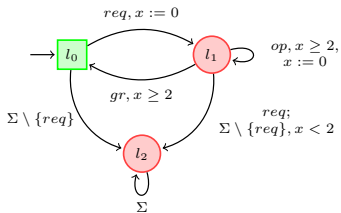
←

t	q	σ_{ms}	σ_{mc}
3	$(l_0, 0)$	ϵ	$(2, req)$

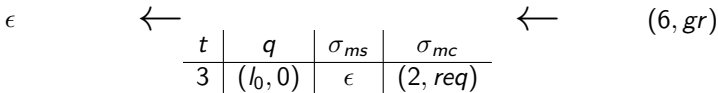
←

$(3, req) \cdot (6, gr)$

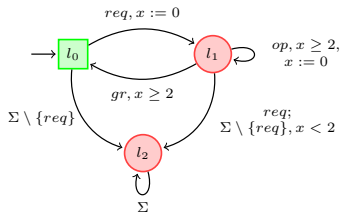
Enforcement monitor: example



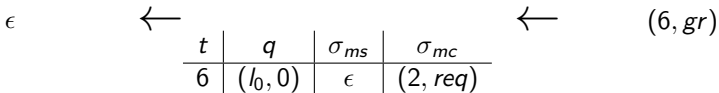
Operation: $store-sup-\bar{\varphi}$



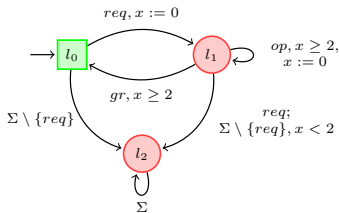
Enforcement monitor: example



Operation: **idle(3)**



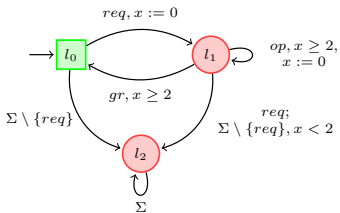
Enforcement monitor: example



Operation: *store- φ*

\leftarrow	\leftarrow	\leftarrow	\leftarrow	\leftarrow
ϵ				ϵ
t	q	σ_{ms}	σ_{mc}	
6	$(l_0, 2)$	$(6, req) \cdot (8, gr)$	ϵ	

Enforcement monitor: example



Operation: *dump*

(6, req)

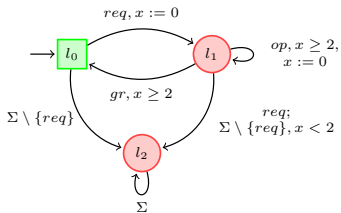
←

t	q	σ_{ms}	σ_{mc}
6	$(l_0, 2)$	$(8, gr)$	ϵ

←

ϵ

Enforcement monitor: example



Operation:

idle(2)

(6, req)

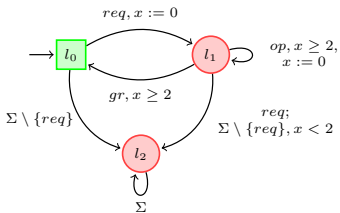
←

t	q	σ_{ms}	σ_{mc}
8	$(l_0, 2)$	$(8, gr)$	ϵ

←

ϵ

Enforcement monitor: example



Operation:

dump

$(6, req) \cdot (8, gr)$

←

t	q	σ_{ms}	σ_{mc}
8	$(l_0, 2)$	ϵ	ϵ

←

ϵ

Enforcement monitor: correctness

Implementation relation between Enforcement Monitor and Enforcement Function

Given some property φ , at any time t , the input/output behavior of the synthesized enforcement monitor is the same as the one of the corresponding enforcement function at time t , i.e., $\text{obs}(E_\varphi(\sigma), t)$.

Corollary

Enforcement Monitors respect physical, soundness, and transparency constraints.

1 Specifying Timed Properties

2 RE of Regular Timed Properties

- Requirements on an Enforcement Mechanism
- Functional Definition of an Enforcement Mechanism
- Operational Description of an Enforcement Mechanism

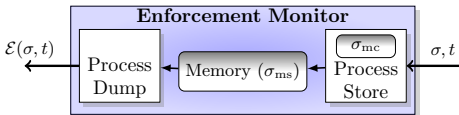
3 Implementation

4 RE of Parametric Timed Properties

- PTAVs
- Runtime Enforcement of PTAVs
- Application Domains

5 Conclusions and Future Work

Enforcement algorithms



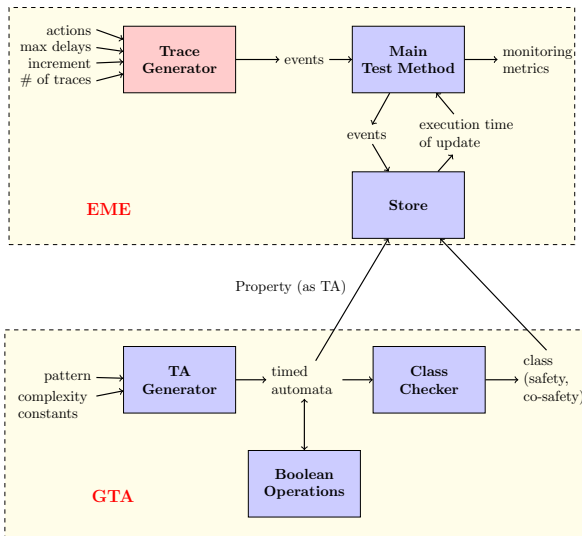
Algorithm: StoreProcess

 $(t, q) \leftarrow (0, q_0)$
 $(\sigma_{ms}, \sigma_{mc}) \leftarrow (\epsilon, \epsilon)$
while tt **do**
 $(t, a) \leftarrow \text{await}(\text{event})$
 $(q', \sigma'_{mc}, \text{isPath}) \leftarrow \text{update}(q, \sigma_{mc}, (t, a))$
if $\text{isPath} = \text{ok}$ **then**
 $\sigma_{ms} \leftarrow \sigma_{ms} \cdot \sigma'_{mc}$
 $\sigma_{mc} \leftarrow \epsilon$
 $q \leftarrow q'$
else
 $\sigma_{mc} \leftarrow \sigma'_{mc}$
end if
end while

Algorithm: DumpProcess

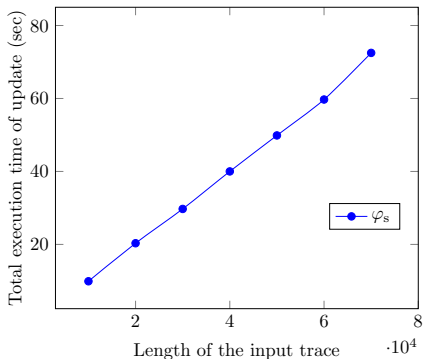
 $d \leftarrow 0$
while tt **do**
 $\text{await}(\sigma_{ms} \neq \epsilon)$
 $(t, a) \leftarrow \text{dequeue}(\sigma_{ms})$
 $\text{wait}(t - d)$
 $\text{dump}(a)$
end while

TIPEX tool



Evaluation

“There should be a delay of at least 5 time units between any two request actions”.



φ_s	
$ tr $	t_update
10,000	9.895
20,000	20.323
30,000	29.722
40,000	40.007
50,000	49.869
60,000	59.713
70,000	72.494

1 Specifying Timed Properties

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5 Conclusions and Future Work

Motivations for enforcement with *time* and data

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Specifying constraints over time and data

Support richer requirements in our enforcement framework (time constraints between events, and allowing events to carry data).

Motivations for enforcement with *time* and data

Specifying constraints over time and data

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- *After a request, there should be a response **after a delay of 5 t.u.***

Motivations for enforcement with *time* and *data*

Specifying constraints over time and data

Support richer requirements in our enforcement framework (time constraints between events, and allowing events to carry data).

- *After a request, there should be a response after a delay of 5 t.u. if there are more than 10 request messages.*

Motivations for enforcement with *time* and *data*

Specifying constraints over time and data

Support richer requirements in our enforcement framework (time constraints between events, and allowing events to carry data).

- *After a request, there should be a response **after a delay of 5 t.u.** if there are more than 10 request messages.*
- *For each client, after a request, there should be a response after a delay of 5 t.u. if the number of request messages is more than 10.*

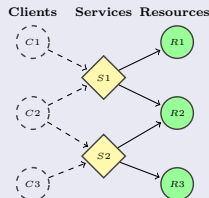
Motivations for enforcement with *time* and *data*

Specifying constraints over time and data

Support richer requirements in our enforcement framework (time constraints between events, and allowing events to carry data).

- After a request, there should be a response *after a delay of 5 t.u. if there are more than 10 request messages*.
- *For each client*, after a request, there should be a response after a delay of 5 t.u. if the number of request messages is more than 10.

Resource allocation in a client-server model



Parameterized Timed Automata with Variables (PTAV)

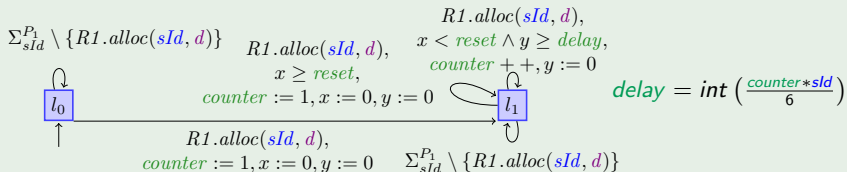
Syntax of PTAV

$A(p) = (p, V, C, \Theta, L, l_0, F, X, \Sigma_p, \Delta)$.

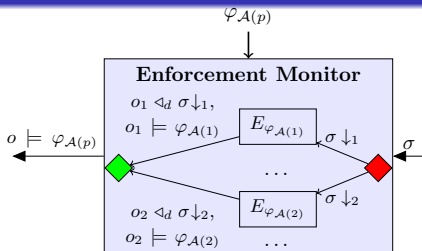
- p - A parameter (for example to handle multiple clients/instances).
- C - External variables (to model transfer of data from the monitored system along with events).
- V - Internal variables (used for internal computation).

A PTAV is denoted as $A(p)$, and an instance of a PTAV for a value π of p is denoted as $A(\pi)$.

PTAV Example: in the context of resource allocation

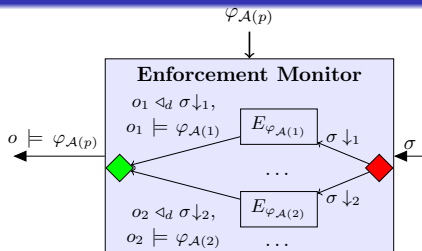


Enforcement of parametric timed properties



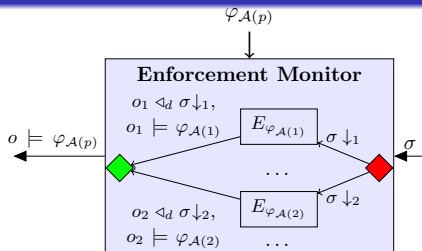
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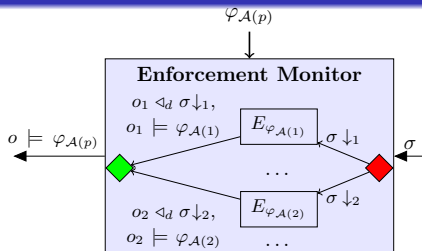
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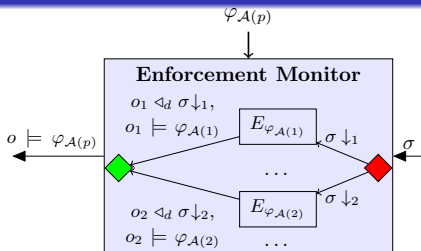
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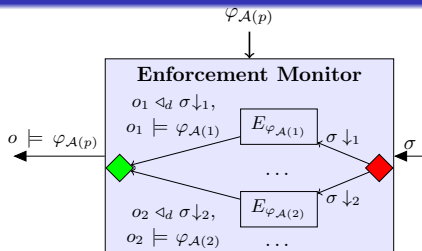
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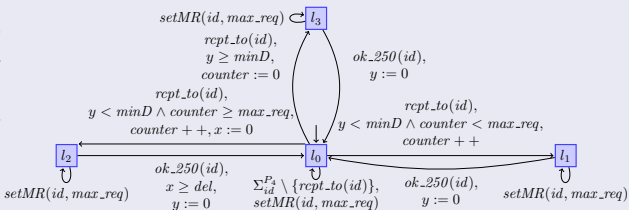


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- **Update** function is computable (straightforward adaptation).
- Output of each EM instance satisfies constraints.

Other application domains

Protecting mail servers

If the number of RCPT_TO messages from a client is greater than maxreq, then there should be a delay of at least del t.u. before responding an OK_250.¹



1 Specifying Timed Properties

2 RE of Regular Timed Properties

- Requirements on an Enforcement Mechanism
- Functional Definition of an Enforcement Mechanism
- Operational Description of an Enforcement Mechanism

3 Implementation

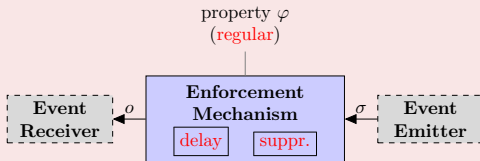
4 RE of Parametric Timed Properties

- PTAVs
- Runtime Enforcement of PTAVs
- Application Domains

5 Conclusions and Future Work

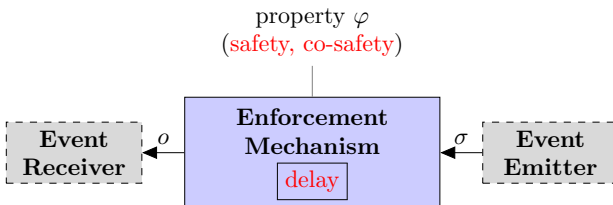
Conclusions

Enforcement monitoring for systems with timing requirements.



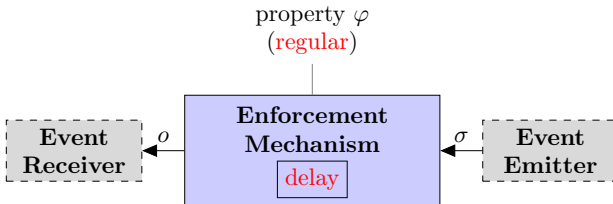
- Formally based runtime enforcement mechanisms for requirements with real-time constraints.
- For all regular timed properties modeled as a timed automaton.
- Enforcer can **delay** and **suppress** events.
- Enforcement mechanisms described at several levels of abstraction (enforcement function, enforcement monitor and algorithms).
- Prototype tool implementation (TIPEX).
- Requirements with constraints both on time and data (PTAV).

Summary: Evolution of results



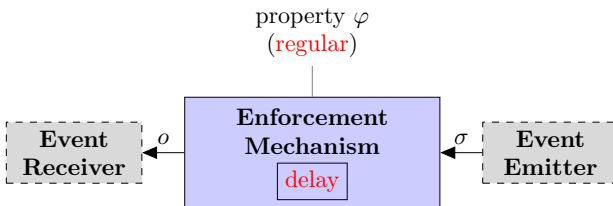
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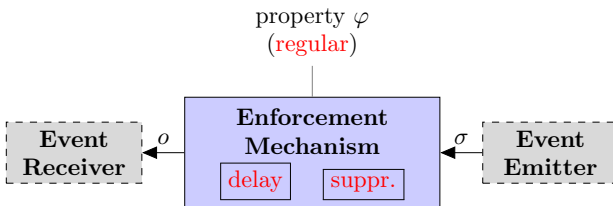
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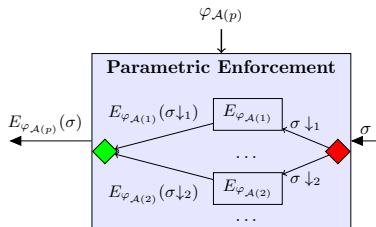
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Perspectives

Theoretical extensions

- Predictive enforcement.
 - $E_{\varphi/\psi} : \psi \subseteq \text{tw}(\Sigma) \rightarrow \{\epsilon\} \cup \varphi \subseteq \text{tw}(\Sigma)$.
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Applications

- Implementing efficient enforcement monitors (in application scenarios).
- Enforcement monitoring techniques to guarantee behavior of off-the-shelf components.
- Enforcement monitor synthesis mechanism to realize some requirements automatically.