

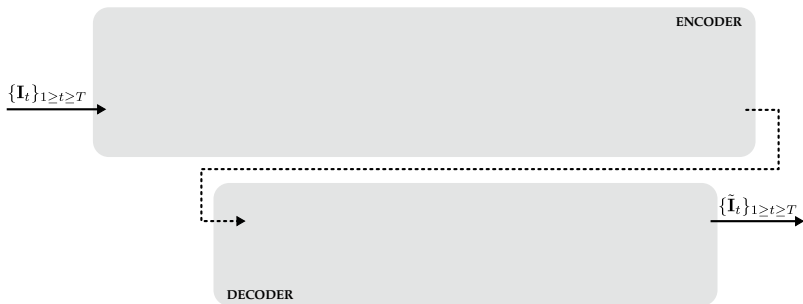
Visual data compression: beyond conventional approaches

Thomas Maugey
thomas.maugey@inria.fr

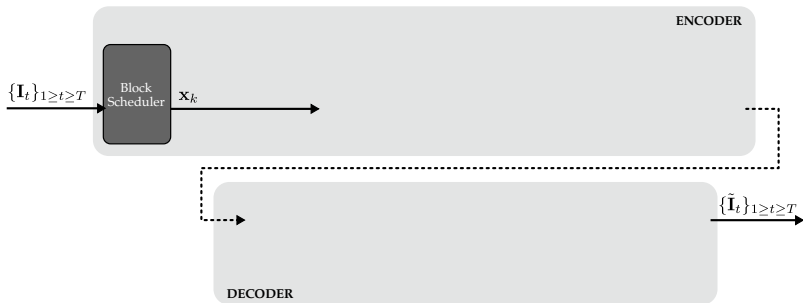


HDR defense, Rennes
June, 27th 2022

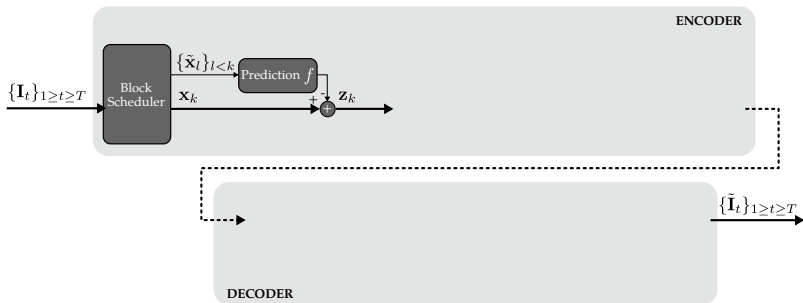
Conventional compression pipeline



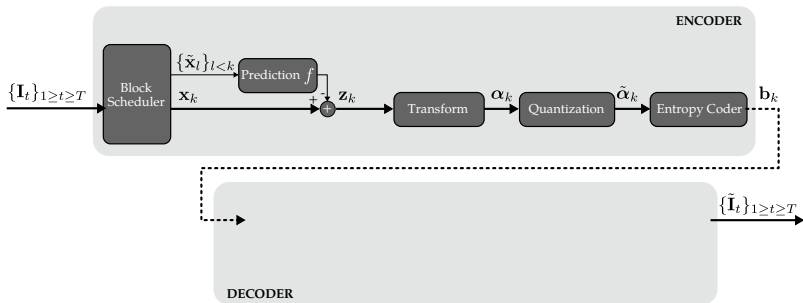
Conventional compression pipeline



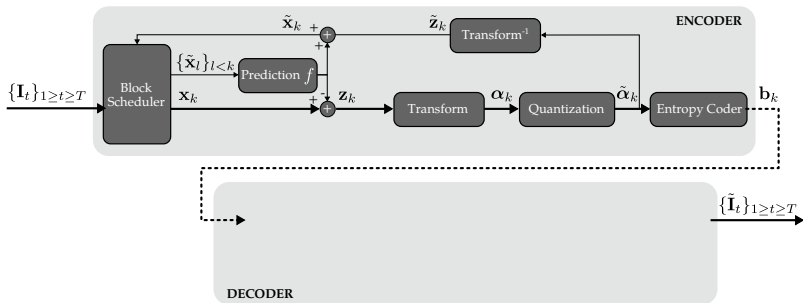
Conventional compression pipeline



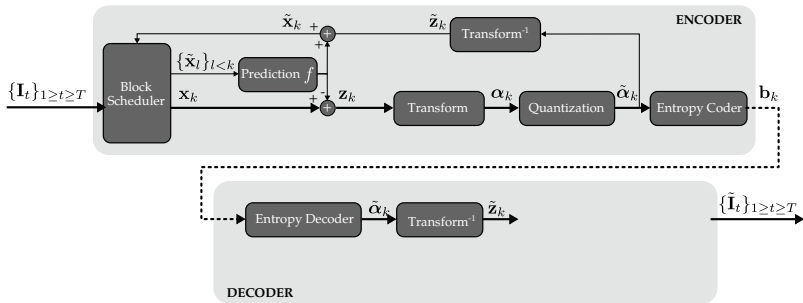
Conventional compression pipeline



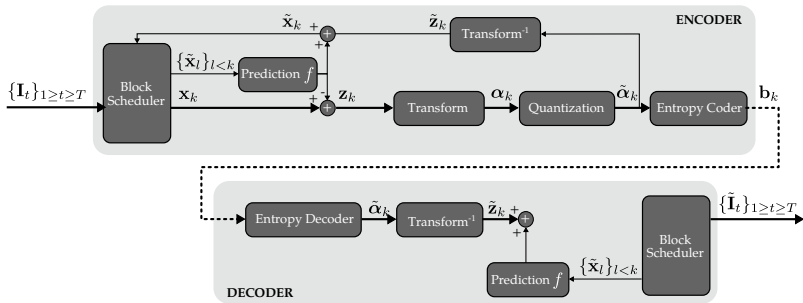
Conventional compression pipeline



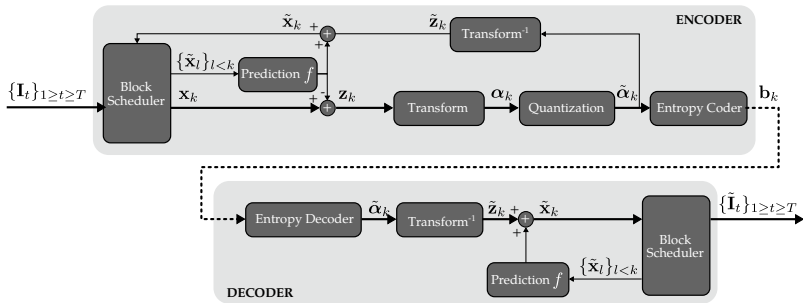
Conventional compression pipeline



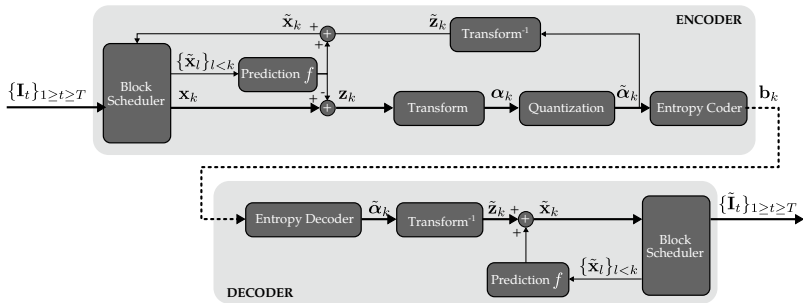
Conventional compression pipeline



Conventional compression pipeline



Conventional compression pipeline



To simplify, the conventional compression pipeline is:

block subdivision \rightarrow prediction \rightarrow transform \rightarrow quantization \rightarrow entropy coding

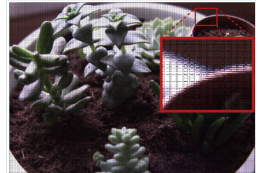
and targets $\min R + \lambda D$ where $R = |\mathbf{b}_k|$ and $D = \|\mathbf{x}_k - \tilde{\mathbf{x}}_k\|_2^2$

Raising of new 3D image modalities

Omnidirectional images/videos



Light Field images/videos

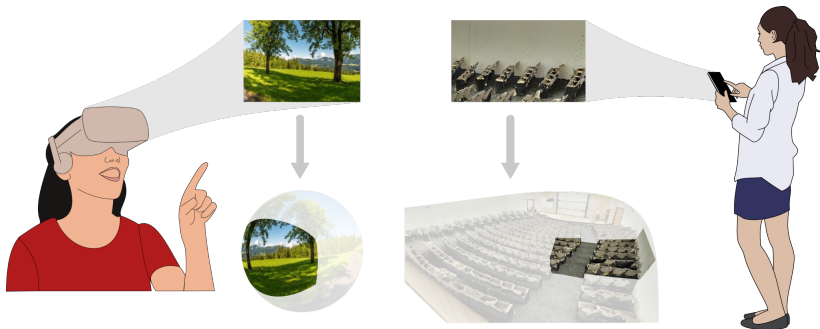


Point Cloud / 3D Mesh



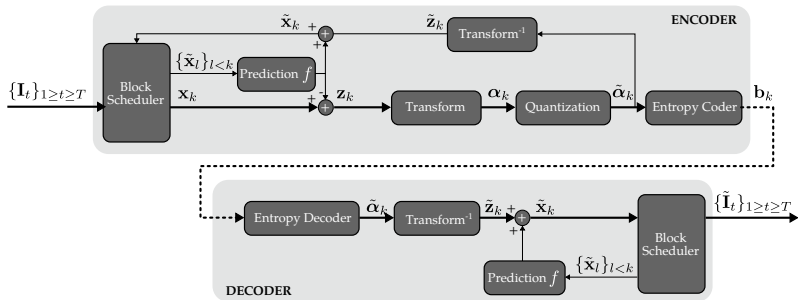
Two peculiarities of 3D data (among others)

- ★ Only a **subset** of the visual data can be watched at a given time

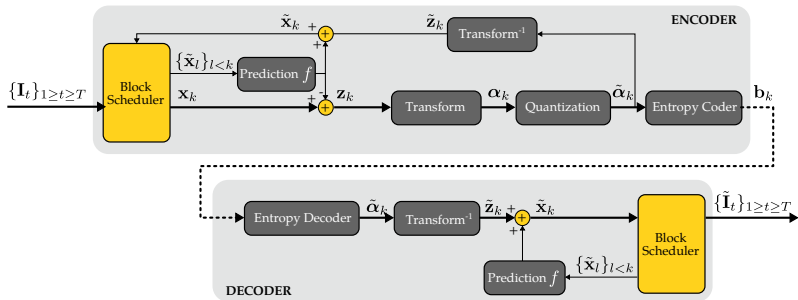


- ★ The pixels lie on **non-euclidean domain**

Incompatibilities of conventional approaches

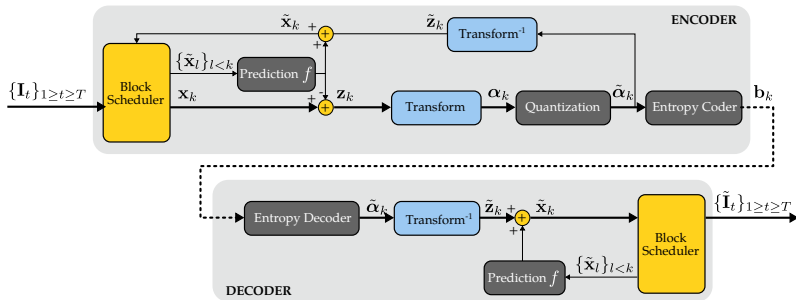


Incompatibilities of conventional approaches



Coding steps incompatible with Random Access

Incompatibilities of conventional approaches



- Coding steps incompatible with Random Access
- Coding steps incompatible with Irregular Topologies

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① Compression with random access

② Compression with Graph-based Transforms

③ Perspectives

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① Compression with random access

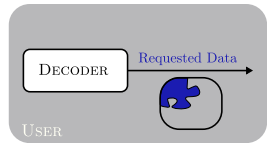
② Compression with Graph-based Transforms

③ Perspectives

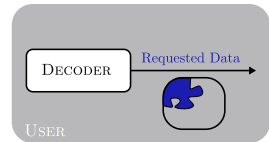
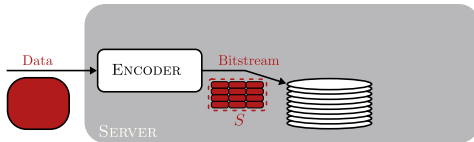
Definition



Definition



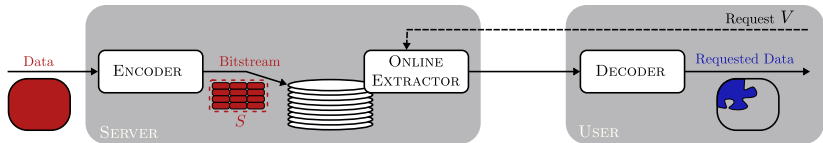
Definition



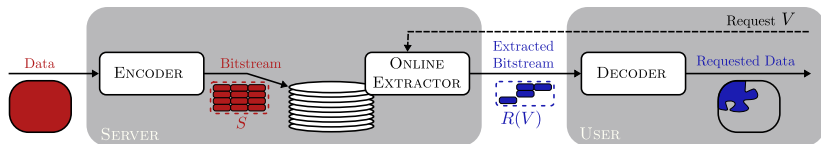
Definition



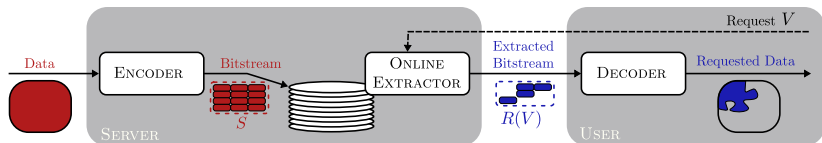
Definition



Definition



Definition



The rate is split into two quantities:

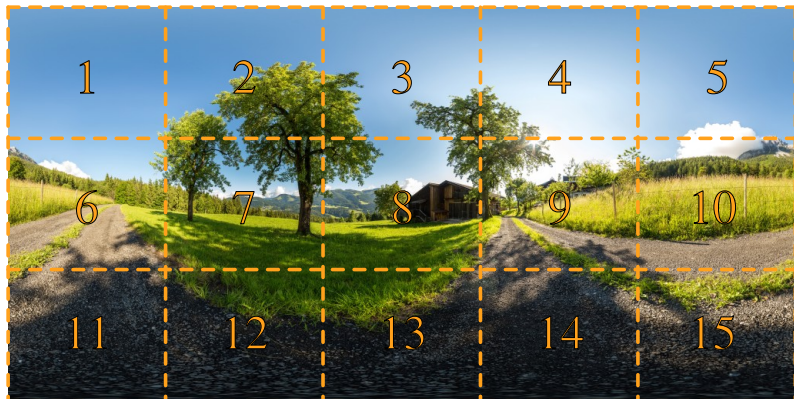
- the **storage** rate S
- the **transmission** rate R :

$$R = \mathbb{E}_{V \sim p_V} [R(V)]$$

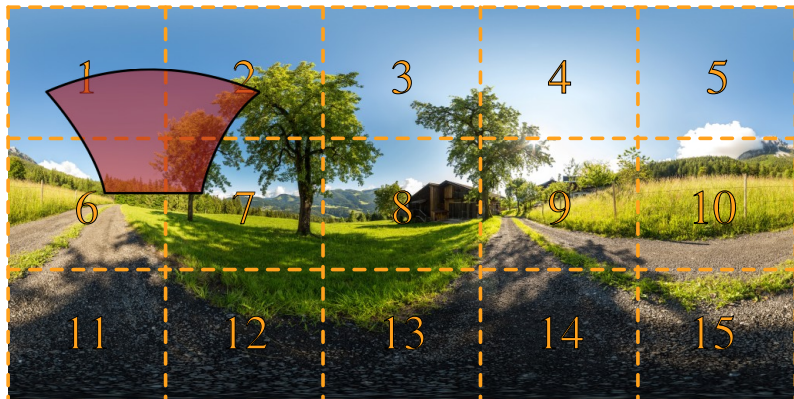
Common solution: data segmentation / tiling



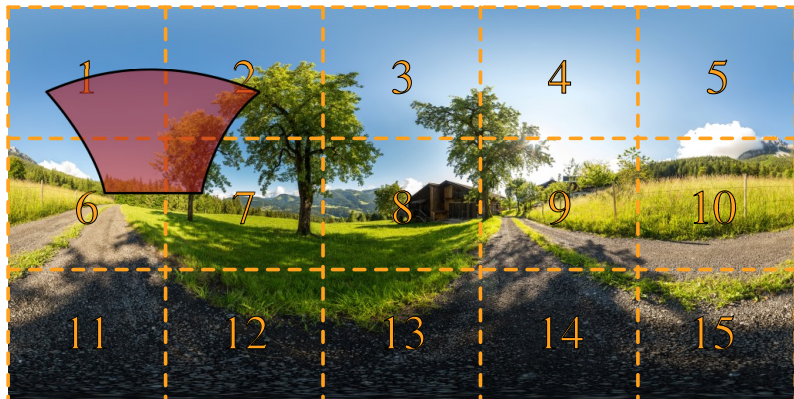
Common solution: data segmentation / tiling



Common solution: data segmentation / tiling

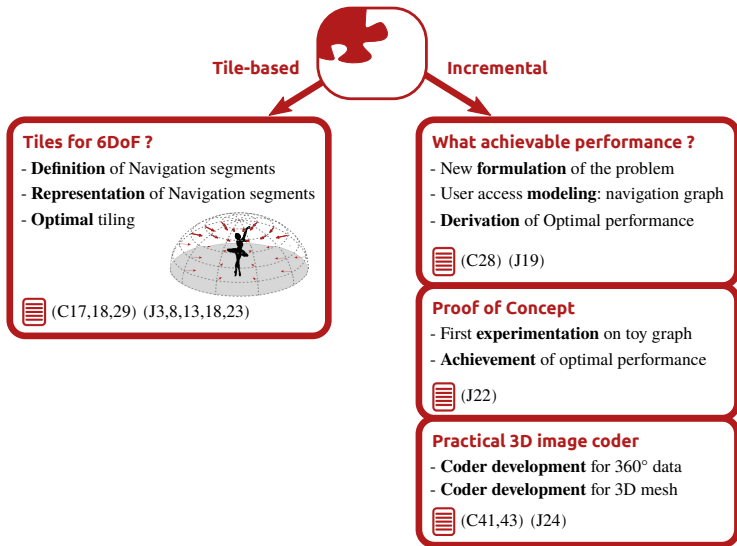


Common solution: data segmentation / tiling

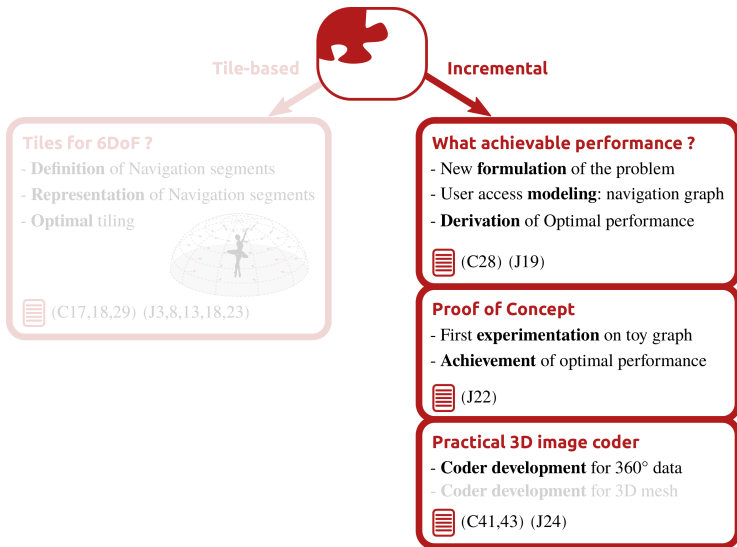


Do tile-based solutions minimize R and S ?

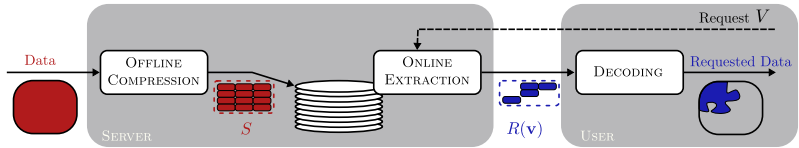
Research achievements



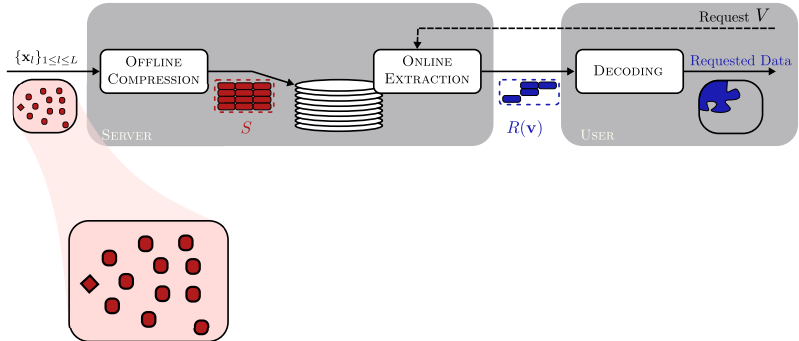
Research achievements



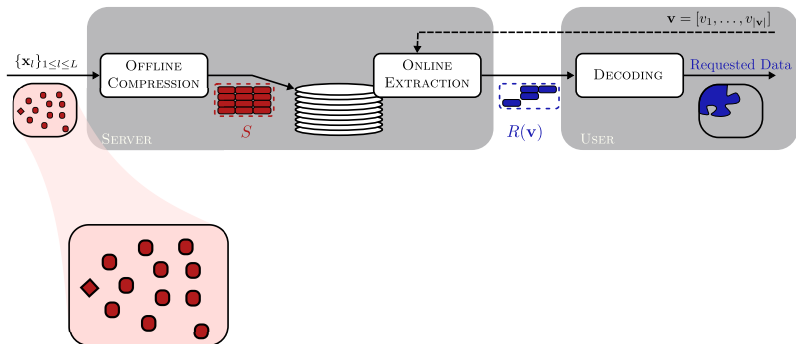
Problem formulation



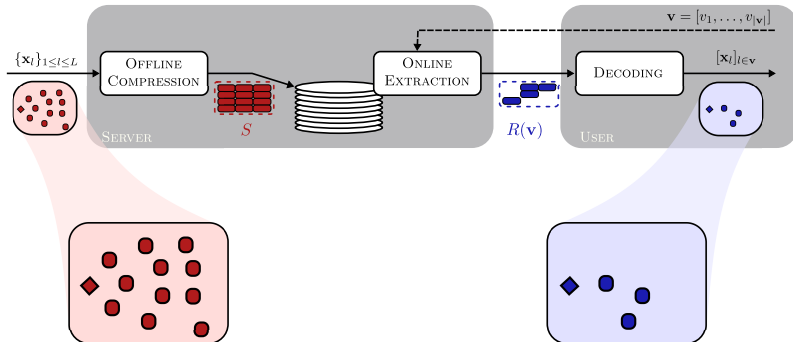
Problem formulation



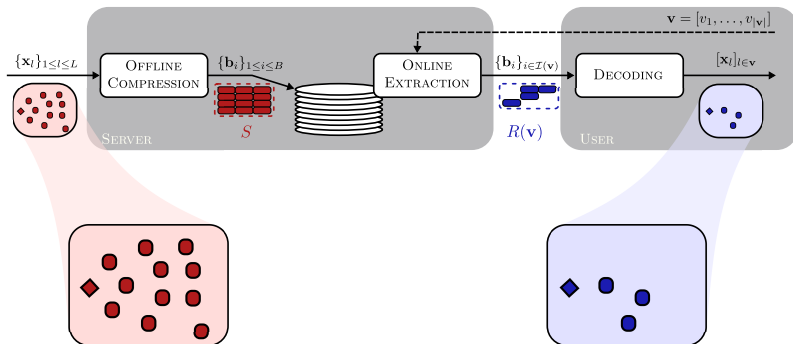
Problem formulation



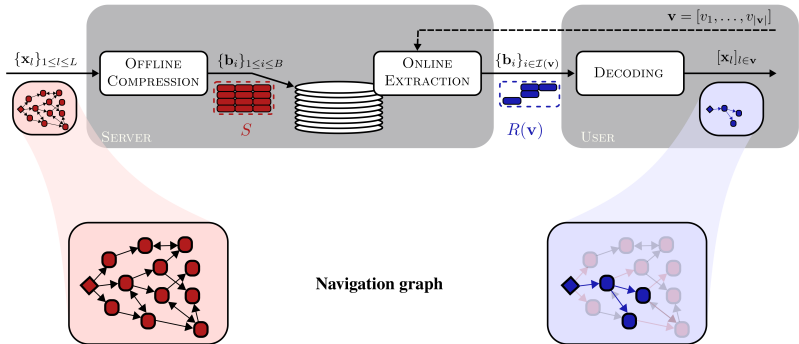
Problem formulation



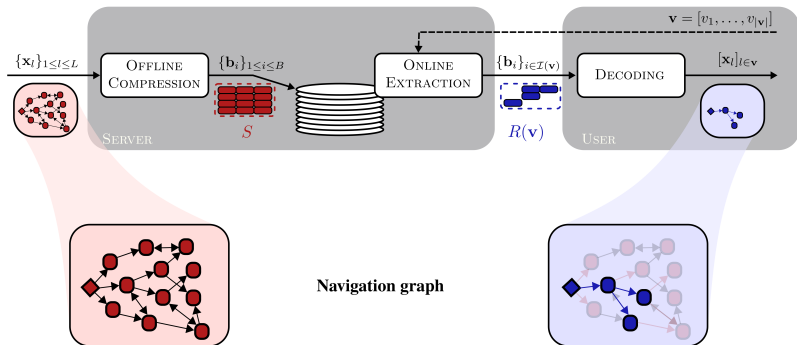
Problem formulation



Problem formulation

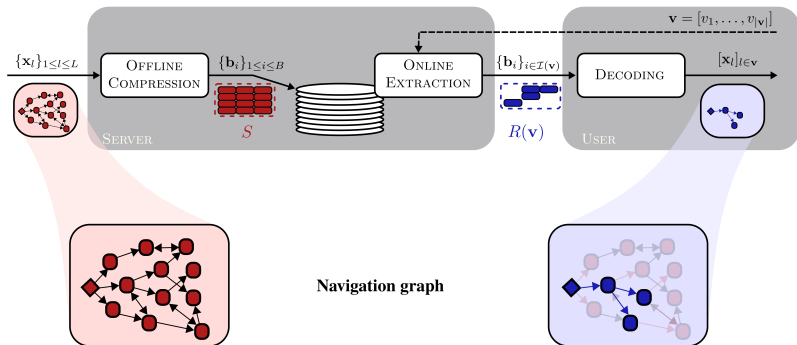


Problem formulation



$$S = \sum_{i=1}^B |\mathbf{b}_i| \text{ and } R(\mathbf{v}) = \sum_{i \in \mathcal{I}(\mathbf{v})} |\mathbf{b}_i|$$

Problem formulation



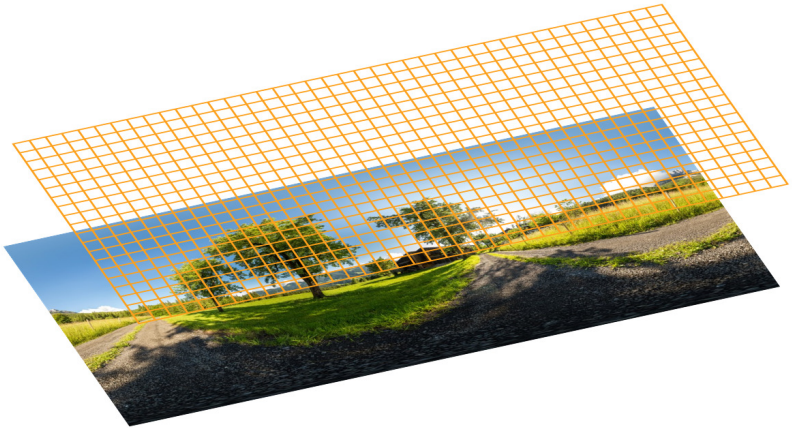
$$S = \sum_{i=1}^B |b_i| \text{ and } R(\mathbf{v}) = \sum_{i \in \mathcal{I}(\mathbf{v})} |b_i|$$

What are the achievable S and $R(\mathbf{v})$?

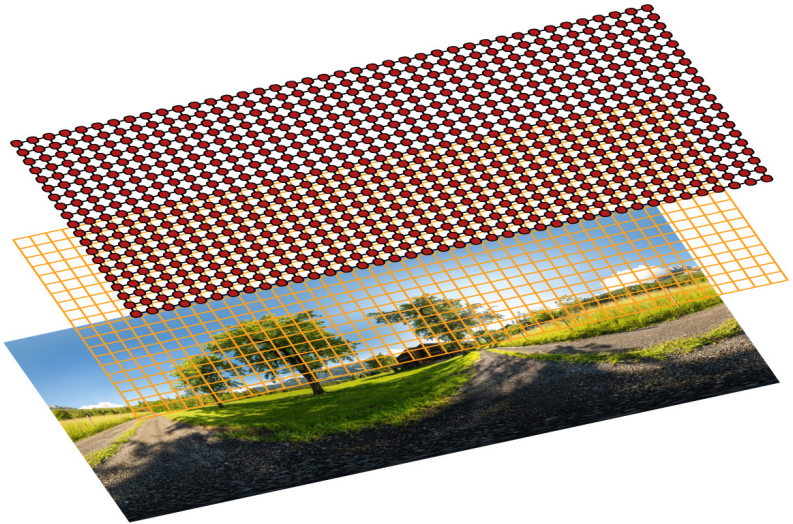
Example of navigation graph



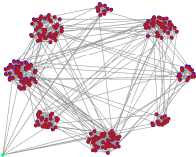
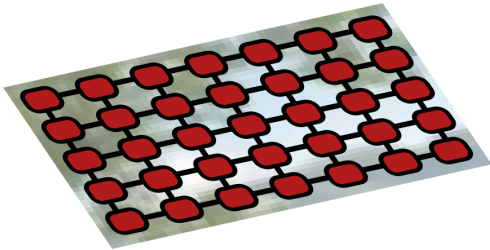
Example of navigation graph



Example of navigation graph

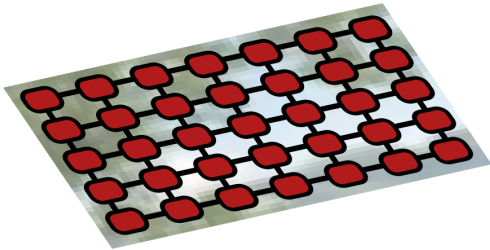


Coding cost evaluation



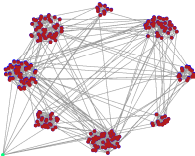
(C28) Roumy and TM, 2015, (J19) Dupraz, TM, Roumy, Kieffer, 2019,
(J22) TM, Roumy, Dupraz, Kieffer, 2020.

Coding cost evaluation

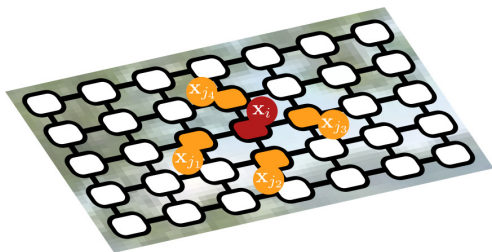


Hypothesis 1

Sources are coded **individually**
(\neq independently)

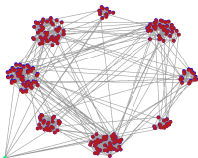


Coding cost evaluation

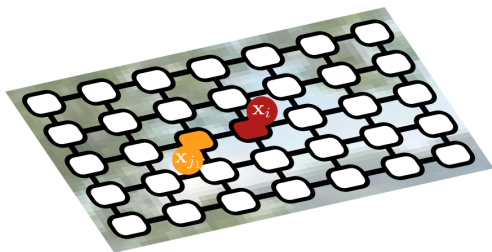


Hypothesis 2

When coding source x_i ,
at least one neighbor
($x_{j_1}, x_{j_2}, x_{j_3}, x_{j_4}$) is available



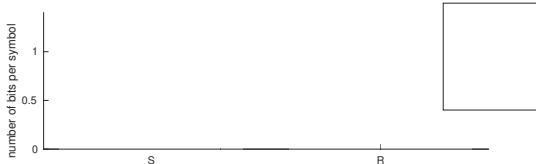
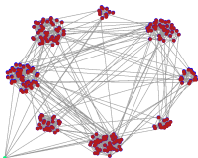
Coding cost evaluation



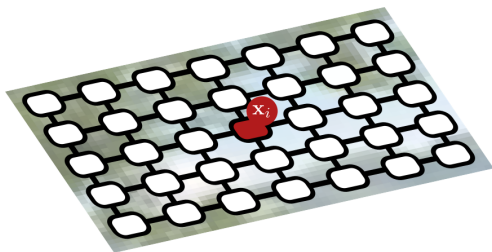
Hypothesis 3

When coding source x_i ,
based on source x_j
the rate is:

$$h_{i|j} = H(X_i|X_j)$$



Coding cost evaluation

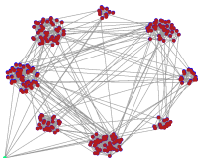


All Intra (AI)

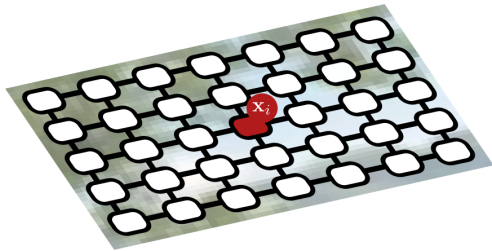
The source x_i
is coded **independently**

$$S_{AI} = h_i$$

$$R_{AI} = h_i$$



Coding cost evaluation

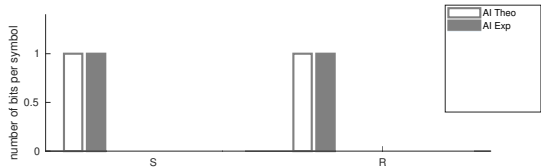
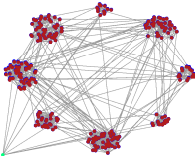


All Intra (AI)

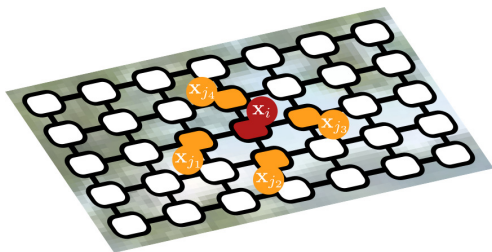
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Coding cost evaluation

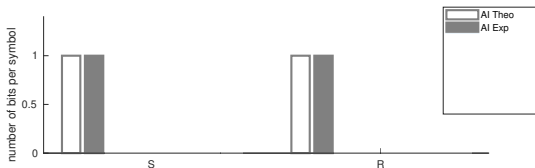
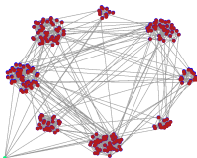


Multiple Prediction (MP)

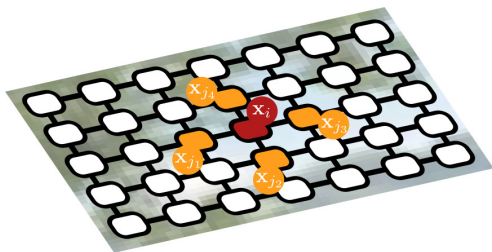
Each residual $\mathbf{x}_i - f(\mathbf{x}_j)$ is stored

$$S_{MP} = \sum_j h_{i|j}$$

$$R_{MP} = h_{i|j}$$



Coding cost evaluation

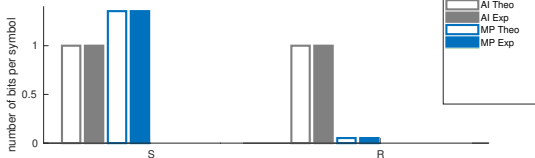
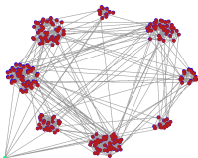


Multiple Prediction (MP)

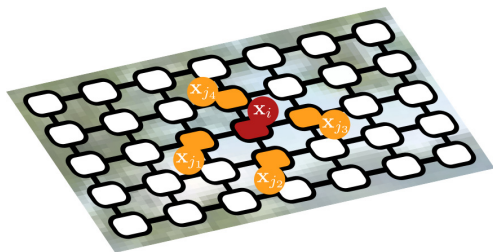
Each residual $\mathbf{x}_i - f(\mathbf{x}_j)$ is stored

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$$R_{MP} = h_{i|j}$$



Coding cost evaluation

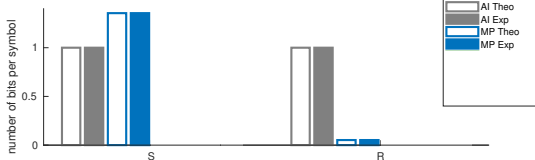
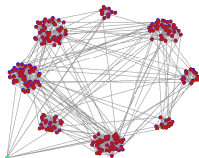


Compound (C) [Cheung11]

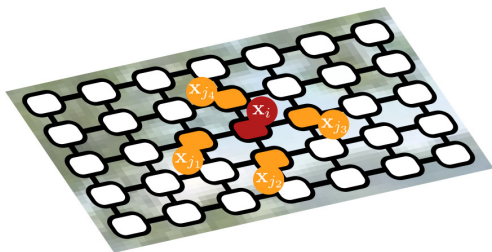
A parity codeword able to decode any prediction

$$S_C = \max_j h_{i|j}$$

$$R_C = \max_j h_{i|j}$$



Coding cost evaluation

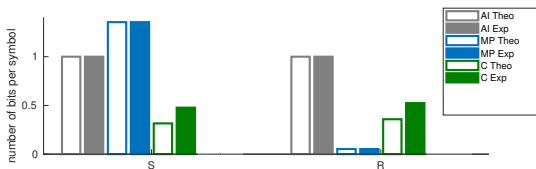
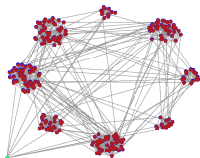


Compound (C) [Cheung11]

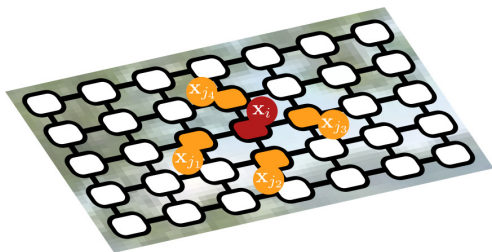
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Coding cost evaluation

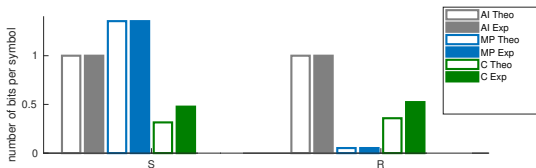
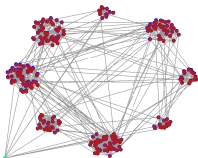


Our result

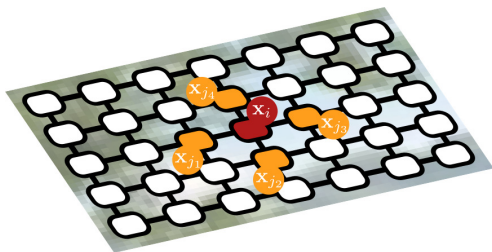
We have proven that theoretically

$$S^* = \max_j h_{i|j}$$

$$R^* = h_{i|j}$$



Coding cost evaluation

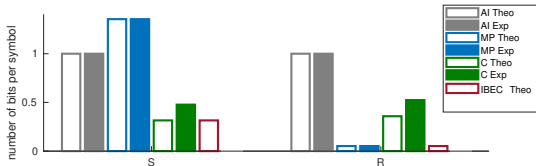
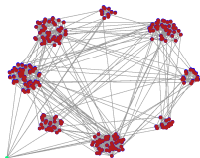


Our result

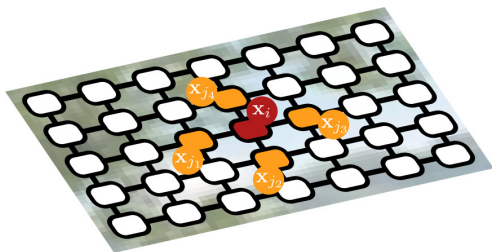
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Coding cost evaluation



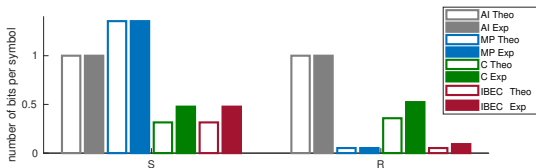
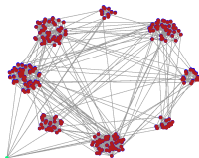
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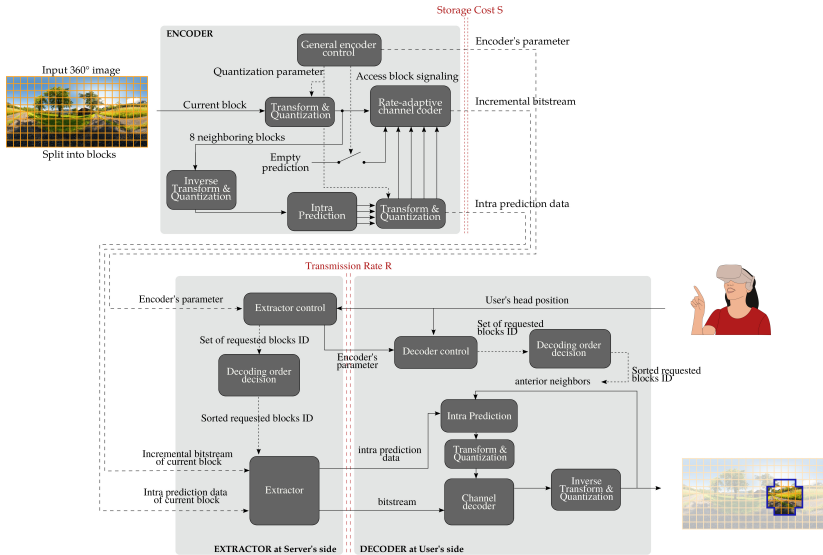
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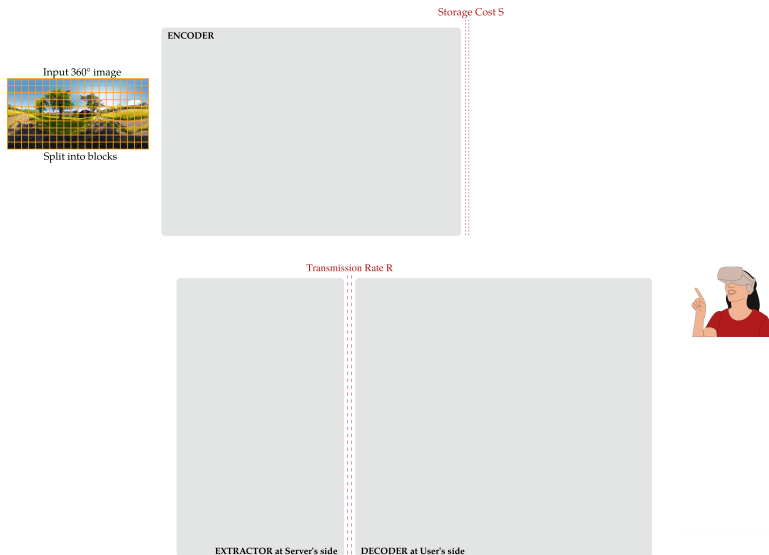
Achievable in practice



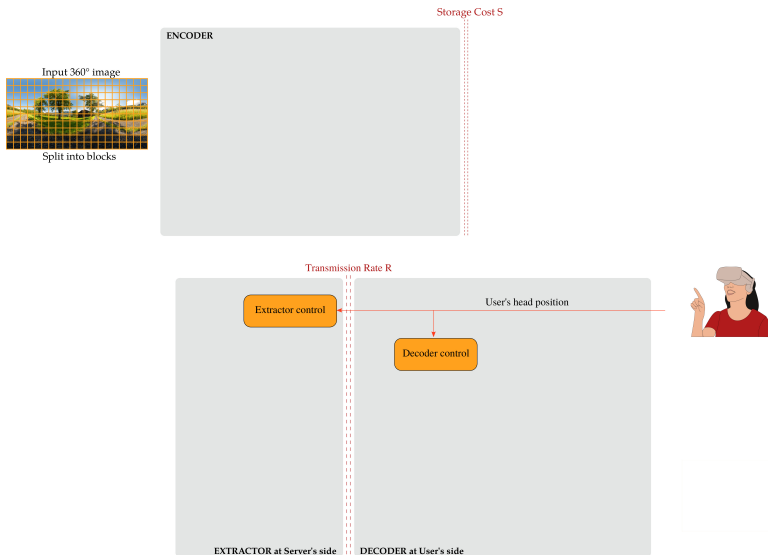
Complete Coding Scheme



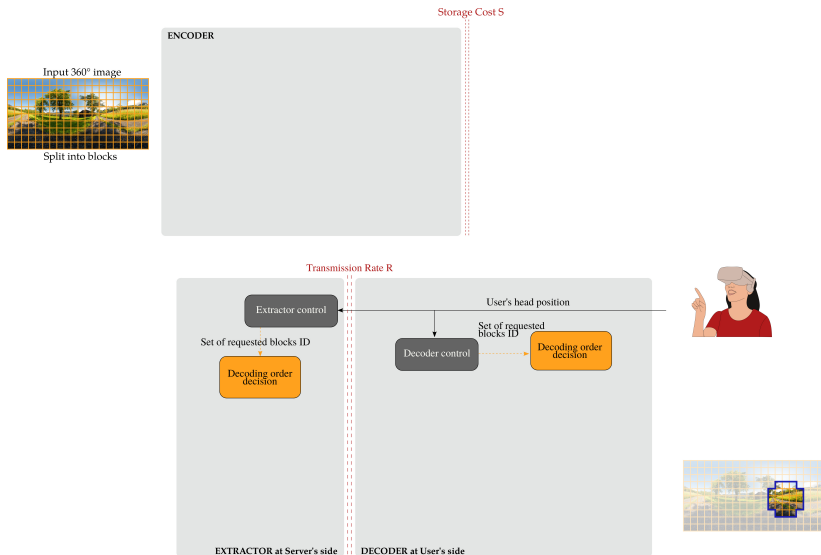
Coding Scheme: step by step



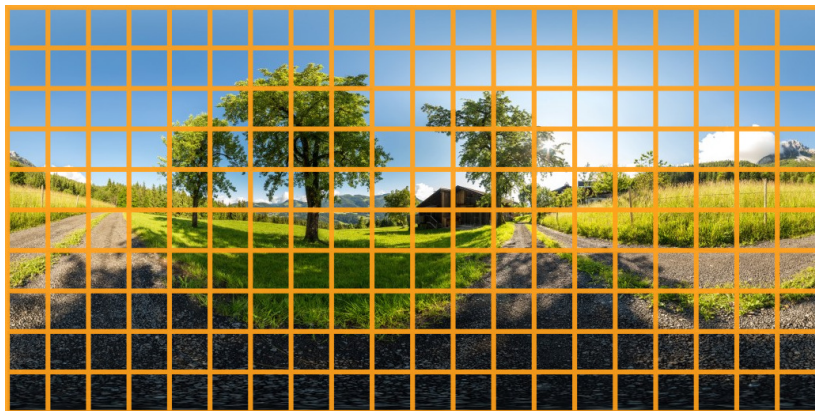
Coding Scheme: step by step



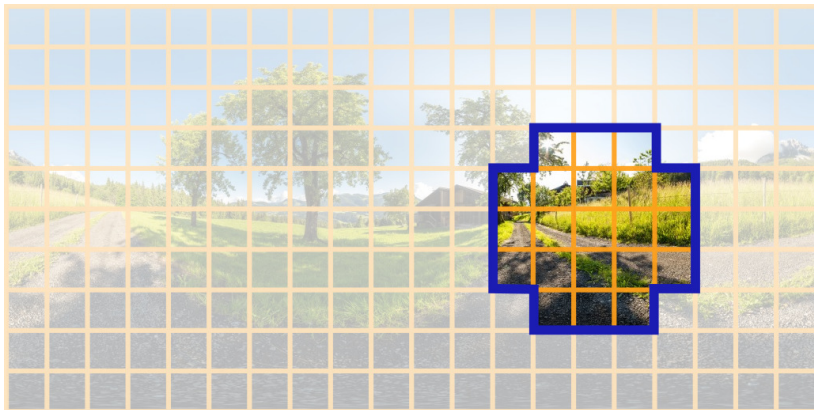
Coding Scheme: step by step



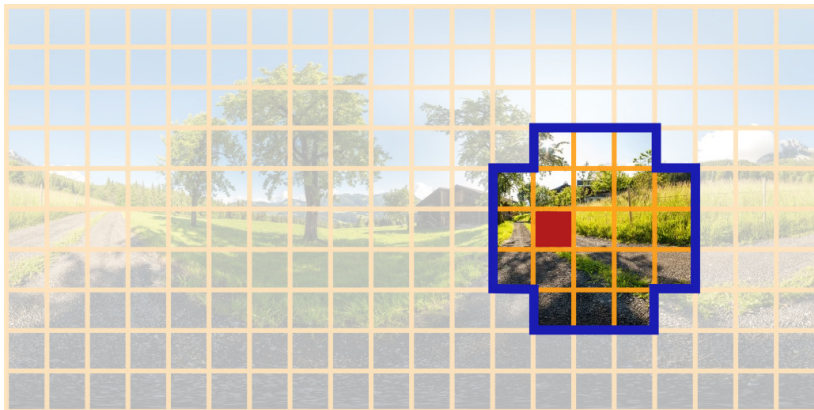
Decoding order



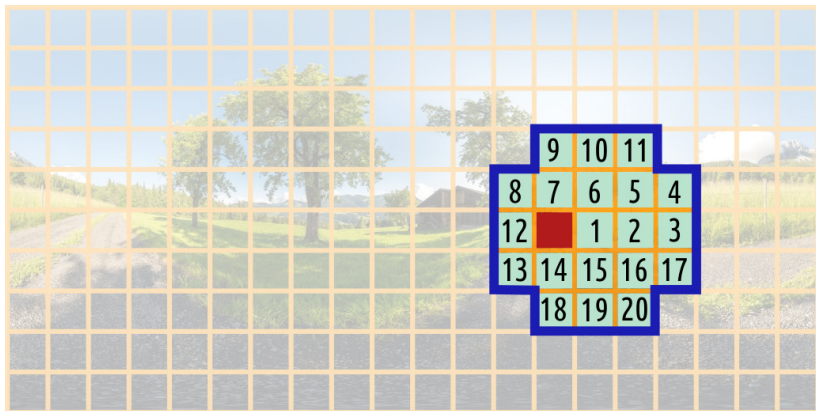
Decoding order



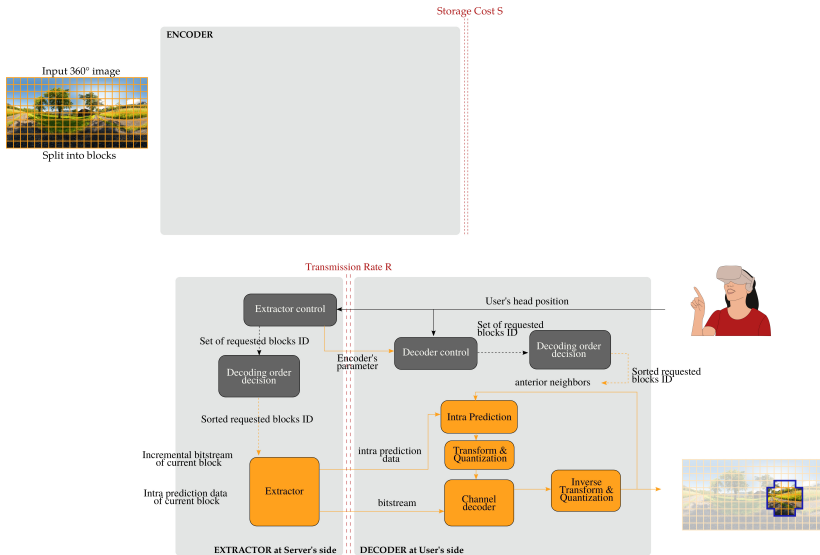
Decoding order



Decoding order



Coding Scheme: step by step

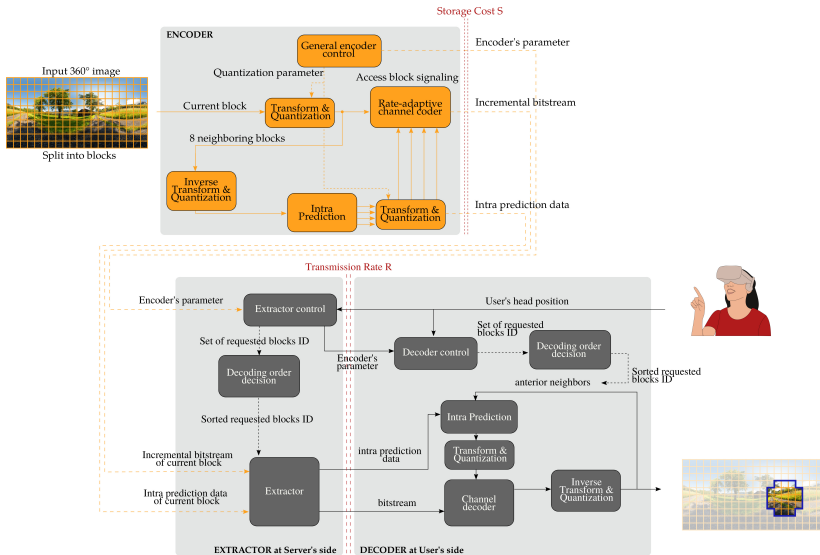


At Encoder's side

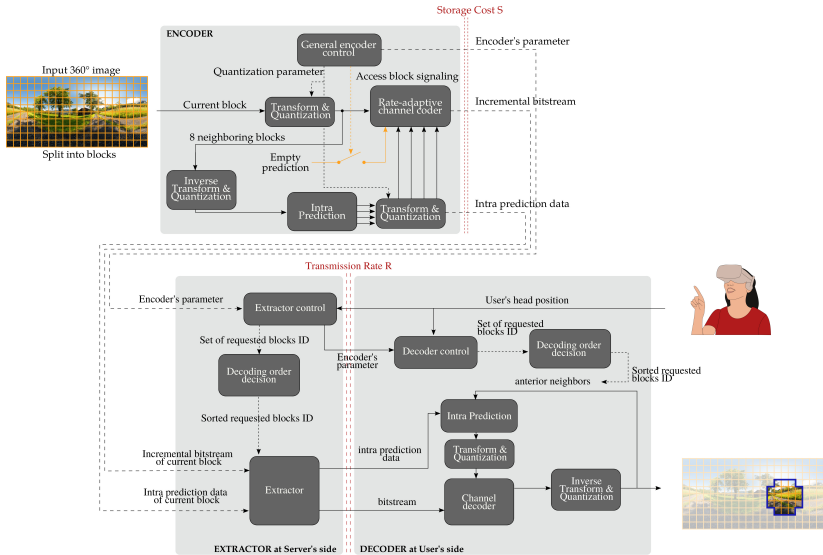
8 possible *intra predictions* (e.g., those of VVC [Pfaff21]) have to be anticipated:



Coding Scheme: step by step



Coding Scheme: step by step



Results

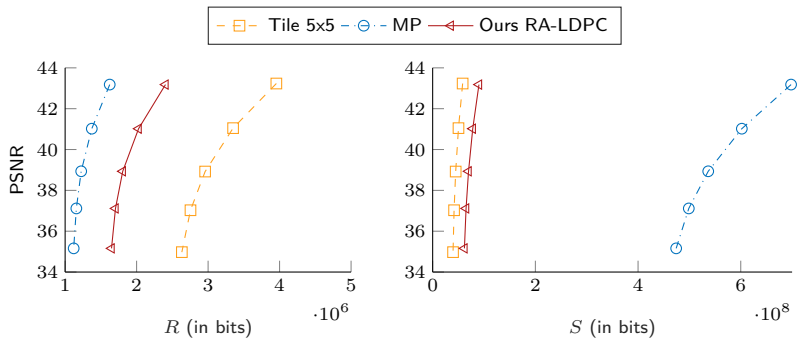


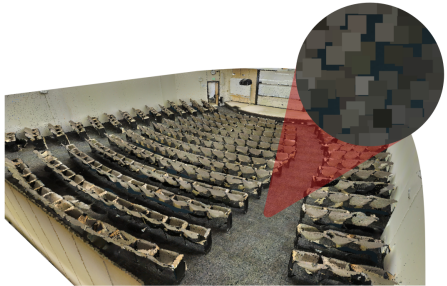
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① Compression with random access

② Compression with Graph-based Transforms

③ Perspectives

Dealing with irregular topology



Dealing with irregular topology

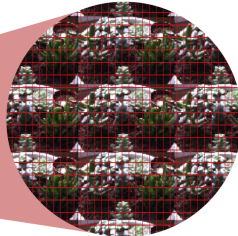
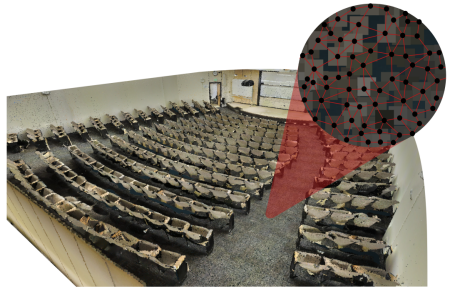
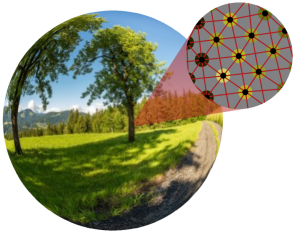


Image on a graph

Graphs represent a pairwise relationship between the pixels.

$\mathcal{G} = (\mathcal{V}, \mathcal{E}, \mathcal{W})$, where

- \mathcal{V} are the nodes (indexed from 1 to N)
- \mathcal{E} are the edges
- \mathcal{W} are the weights on the edges

An **image** on a graph: assign a **color** to each node

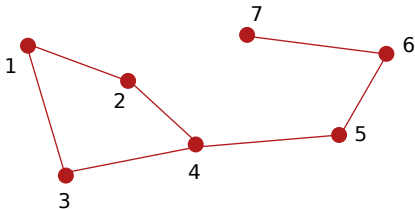


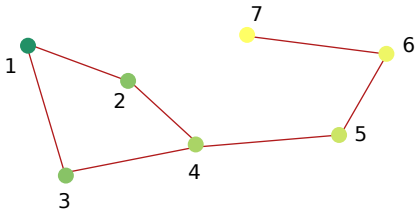
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An **image** on a graph: assign a **color** to each node \rightarrow a **vector** \mathbf{z}



Useful definitions

Adjacency matrix A :

$$a_{ij} = \begin{cases} 1 & \text{if } e_{i,j} \in \mathcal{E} \\ 0 & \text{otherwise} \end{cases}$$

Degree matrix D :

$$d_{ij} = \begin{cases} \text{degree}(v_i) & \text{if } i = j \\ 0 & \text{otherwise} \end{cases}$$

Laplacian matrix L :

$$\mathbf{L} = \mathbf{D} - \mathbf{A}$$

Graph Fourier Transform

Compute the Laplacian matrix:

$$\mathbf{L} = \mathbf{D} - \mathbf{A}$$

Find the eigenvectors and the eigenvalues:

$$\mathbf{L} = \mathbf{U}\mathbf{\Lambda}\mathbf{U}^{\top}$$

Project the signal \mathbf{z} on the eigenvectors to get the transformed coefficients:

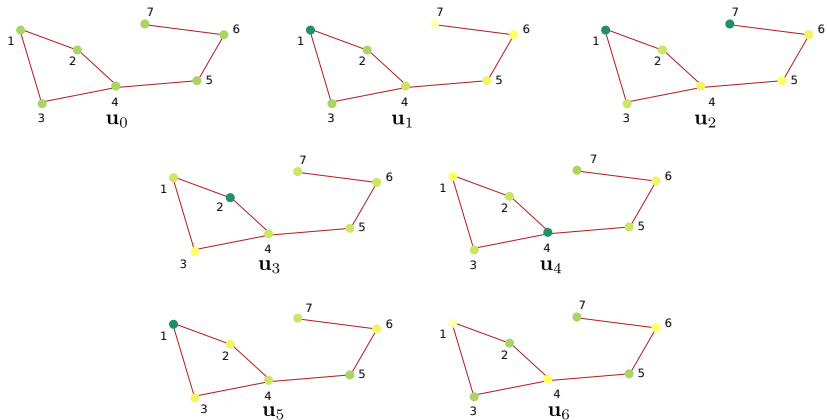
$$\boldsymbol{\alpha} = \mathbf{U}^{\top} \mathbf{z}$$

The inverse transform is:

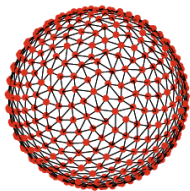
$$\mathbf{z} = \mathbf{U}\boldsymbol{\alpha}$$

More details in e.g., [Shuman13] [Cheung18] [Hu21]

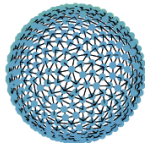
Frequency in the graph



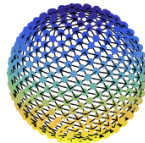
Graph Transforms on the sphere



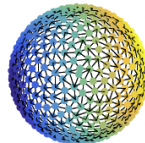
Input graph



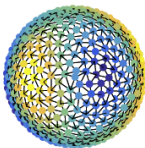
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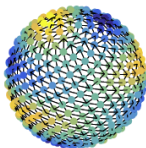
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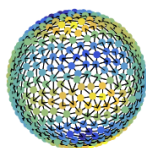
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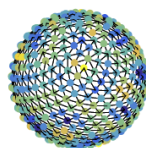
10



20



30



100

Research achievements

How to construct the graph ?




How to reduce GFT complexity ?

Graph for 3D modalities

Graph construction:

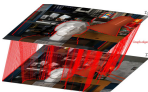
- 360°
- 3D mesh
- Light Fields




 (C32, 39,44)

Graph describing the 3D geometry


- GBR construction
- Color compression
- Generalization to any camera config.



 (C19,20,21,24,30) (J10,16)

Graph segmentation

- Rate-distortion oriented **partitioning**

 (C35,36) (J21)

Separable transform

- graph **separation**
- eigenvector **alignment**

 (J20)

Graph reduction

- graph **coarsening**
- **optimal** graph reduction

 (J28)

Research achievements



How to construct the graph ?

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 (J28)

GFT complexity issue

$\mathbf{L} =$



(a) Full Laplacian

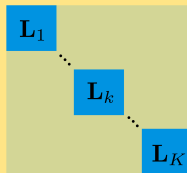
GFT complexity issue

$$\mathbf{L} =$$



(a) Full Laplacian

$$\mathbf{L} \approx$$



(b) Segmentation

Light-field super-ray

A graph applied on each super-ray (estimated e.g., with [Hog17]):



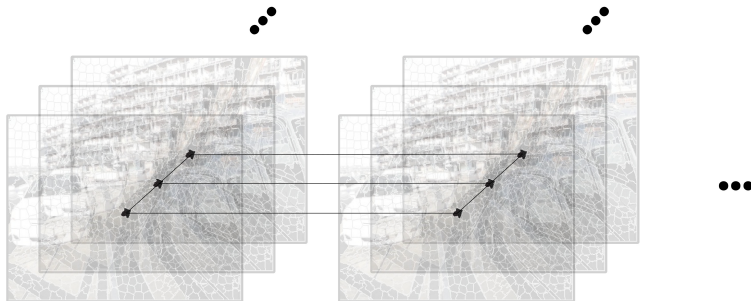
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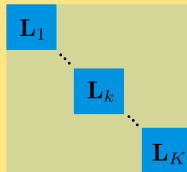
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(b) Segmentation

$$\mathbf{L} \approx \mathbf{L}_1 \otimes \dots \otimes \mathbf{L}_d \otimes \dots \otimes \mathbf{L}_D$$

(c) Dimension separation

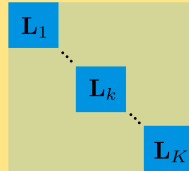
GFT complexity issue

$$\mathbf{L} =$$



(a) Full Laplacian

$$\mathbf{L} \approx$$

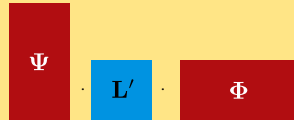


(b) Segmentation

$$\mathbf{L} \approx \mathbf{L}_1 \otimes \dots \otimes \mathbf{L}_d \otimes \dots \otimes \mathbf{L}_D$$

(c) Dimension separation

$$\mathbf{L} \approx$$



(d) Reduction

Laplacian interpretation

2nd derivative, it says how much a z_i value can be estimated by the linear combination of its neighbors:

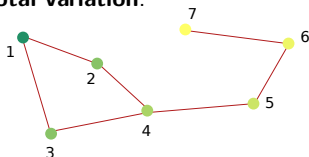
$$\mathbf{Lz} \rightarrow \begin{pmatrix} \vdots \\ d_i z_i - \sum_{j \in \mathcal{N}(i)} w_{i,j} z_j \\ \vdots \end{pmatrix}$$

Laplacian interpretation

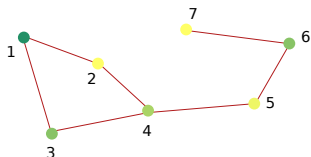
2nd derivative, it says how much a z_i value can be estimated by the linear combination of its neighbors:

$$\mathbf{Lz} \rightarrow \begin{pmatrix} \vdots \\ d_i z_i - \sum_{j \in \mathcal{N}(i)} w_{i,j} z_j \\ \vdots \end{pmatrix}$$

Total variation:



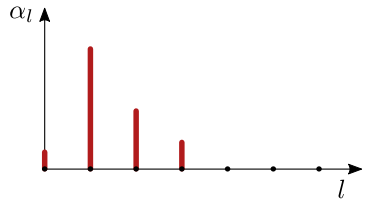
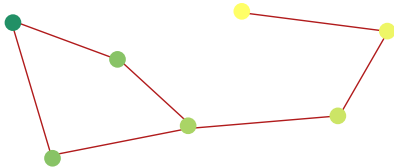
$$\text{TV}_{\mathbf{L}}(\mathbf{z}_1) = \mathbf{z}_1^{\top} \mathbf{L} \mathbf{z}_1 = 60$$



$$\text{TV}_{\mathbf{L}}(\mathbf{z}_2) = \mathbf{z}_2^{\top} \mathbf{L} \mathbf{z}_2 = 120$$

Link with compression

Smooth signal \rightarrow compact energy



A small number of coefficients sufficient to describe the signal

\rightarrow Decrease the graph size

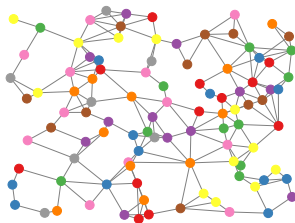
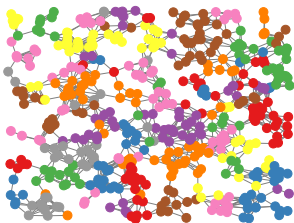
Graph coarsening

In [Loukas 2019], a projection matrix \mathbf{P} :

$$\mathbf{z}' = \mathbf{P}\mathbf{z}$$

$$\mathbf{L}' = \mathbf{P}^\top \mathbf{L} \mathbf{P}^+$$

$$\tilde{\mathbf{z}} = \mathbf{P}^+ \mathbf{z}'$$

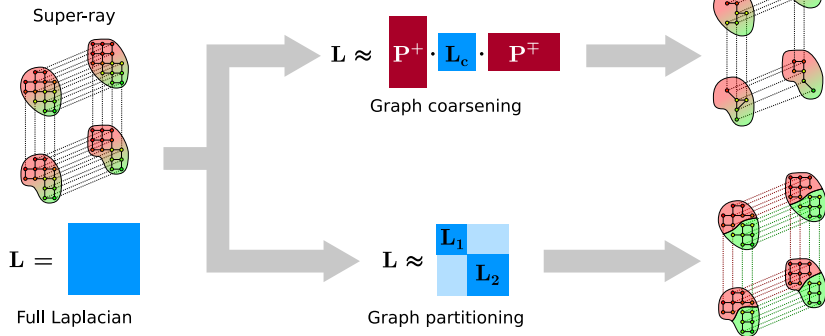


Theoretical link between $\text{TV}_{\mathbf{L}}(\mathbf{z})$ and $\|\mathbf{z} - \tilde{\mathbf{z}}\|_2^2$

Application to Light Field compression



Signal-oriented decision



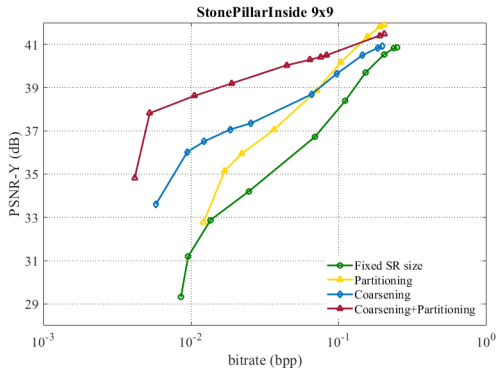


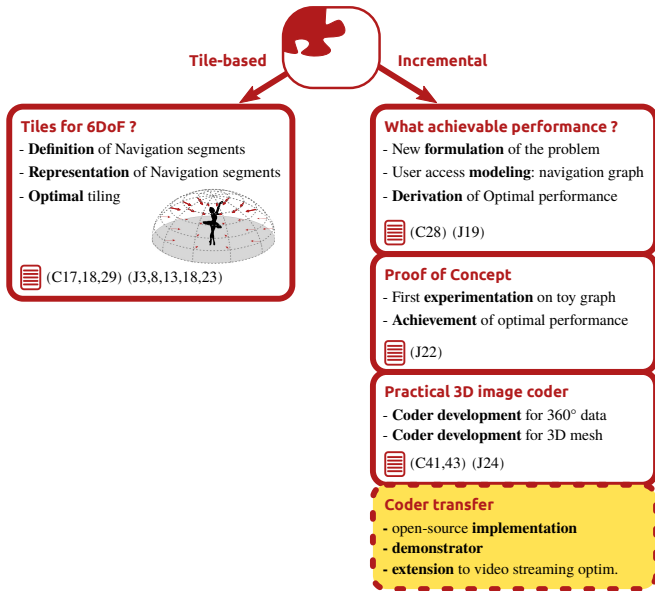
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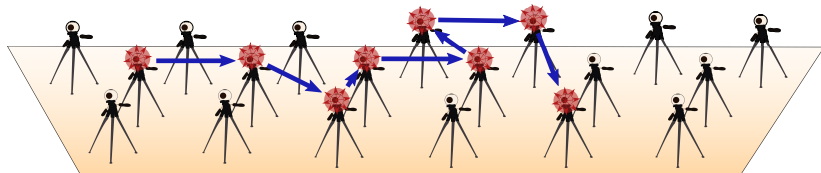
② Compression with Graph-based Transforms

③ Perspectives

Interactive coding dissemination



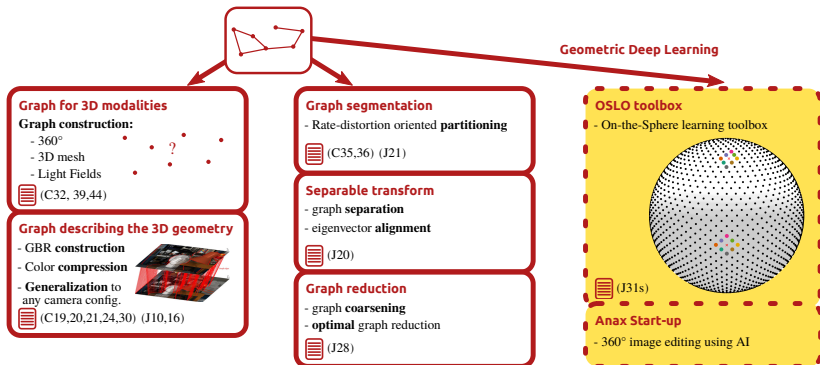
Multi-view 360° view synthesis



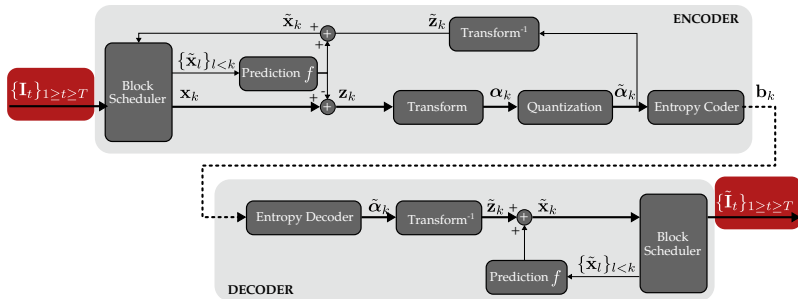
—→ User is able to make discrete translation in the scene

★ At every discrete camera position, the user is able to watch every direction

Learning on the Sphere

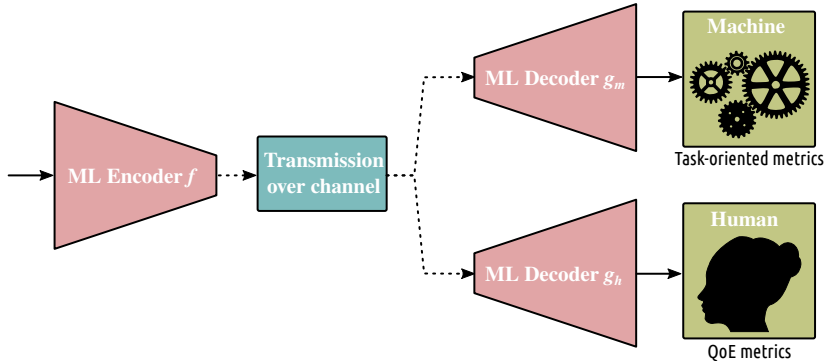


Another conventional coding limitation

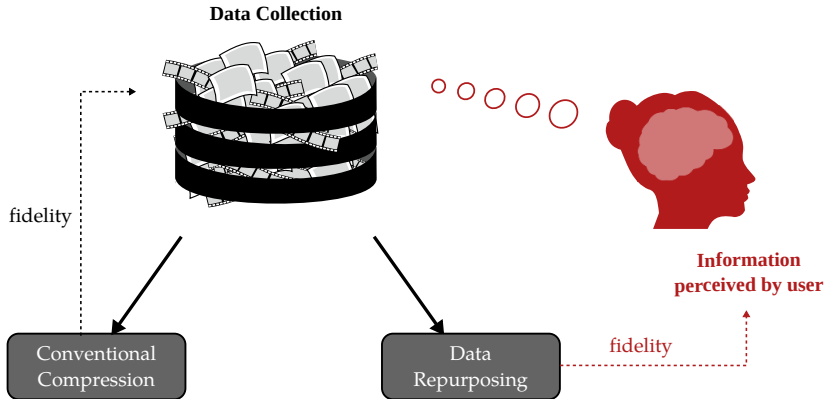


Compression gain limited by the **fidelity criterion**

Coding for machine

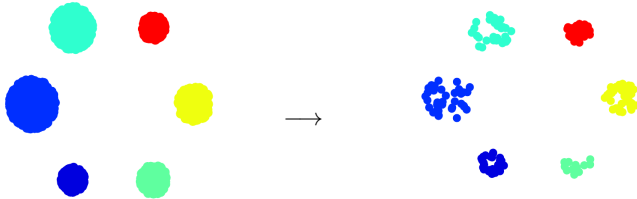


Data Repurposing



Data Repurposing

★ Sampled data collection



★ Generative compression: content regenerated from a digest [Agustsson19]



Thank you

Main collaborators

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- Kai Gu (2021-now)
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- Anju Jose Tom (2020-now)

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- Antoine Crinière (2016-2018)
- Sébastien Bellenous (2020-now)

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