

Conclusion

- ▶ Work still in progress, next steps:
 - ▶ Analyse "false" queries
 - ▶ Link with TAMARIN prover
 - ▶ Mount concrete attacks
 - ▶ Verified properties:
 - ▶ Agreement
 - ▶ Key and message secrecy
 - ▶ Anonymity
 - ▶ Contributions:
 - ▶ Complete model of WireGuard
 - ▶ Precise threat model, including initial key distribution and precomputations
 - ▶ Process with SAPIC⁺, PROVERIF, TAMARIN



- Thanks for your attention !
 - Do you have questions ?

A new symbolic analysis of WireGuard VPN

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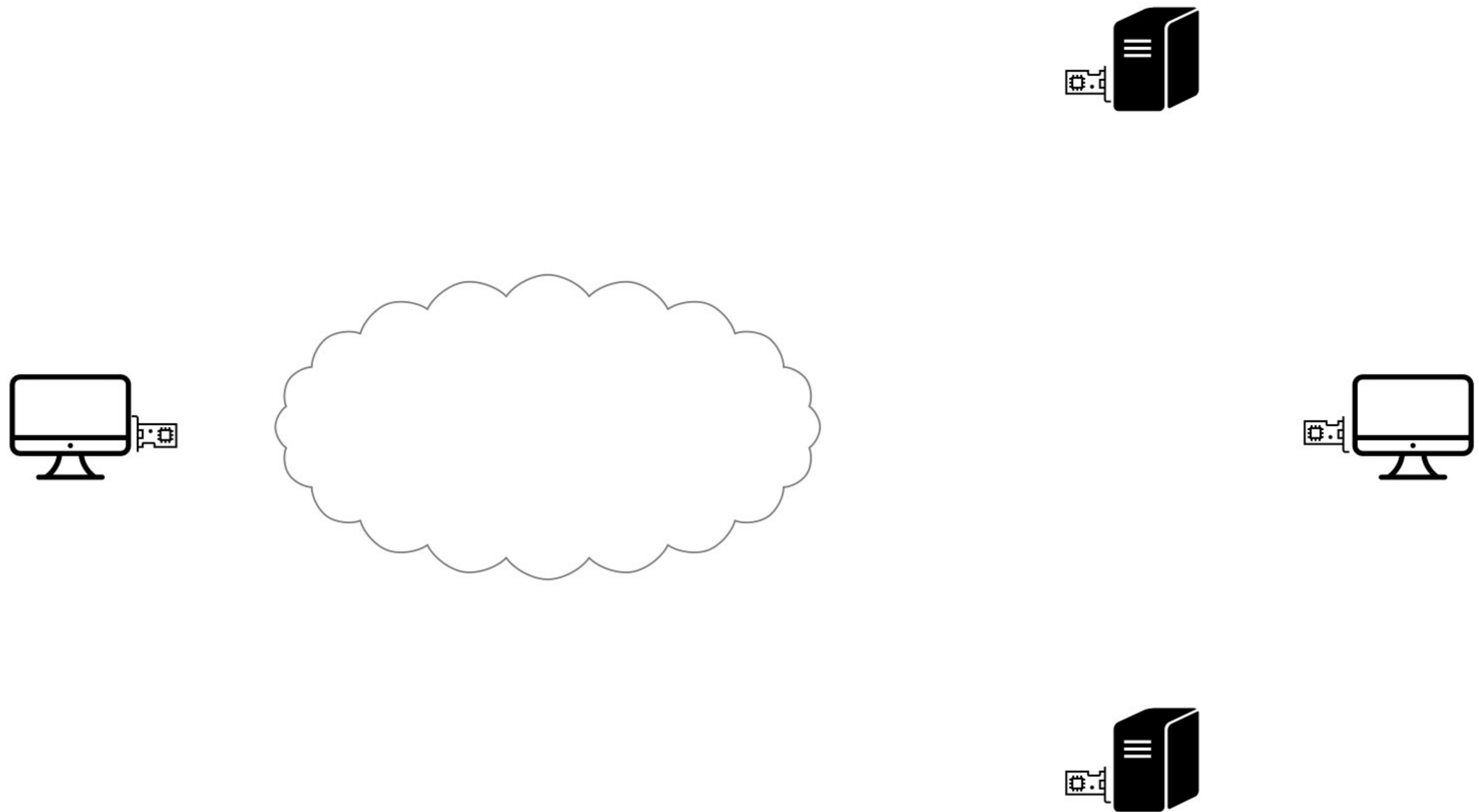




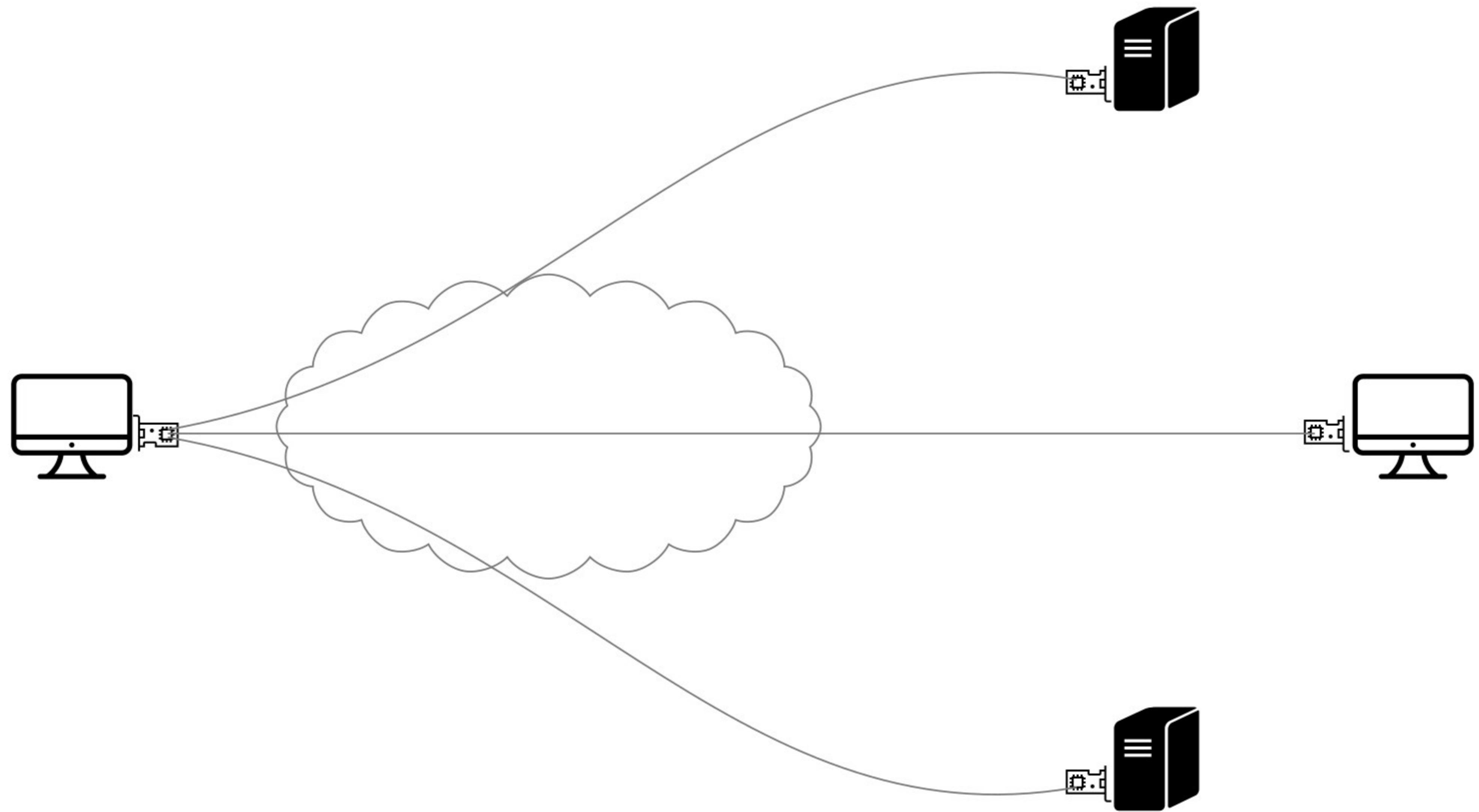
Agenda

- ▶ Context - VPN
 - ▶ Simple protocol
 - ▶ Key agreement - IKpsk2 in action
 - ▶ Complete protocol
 - ▶ Current analyses
 - ▶ New model

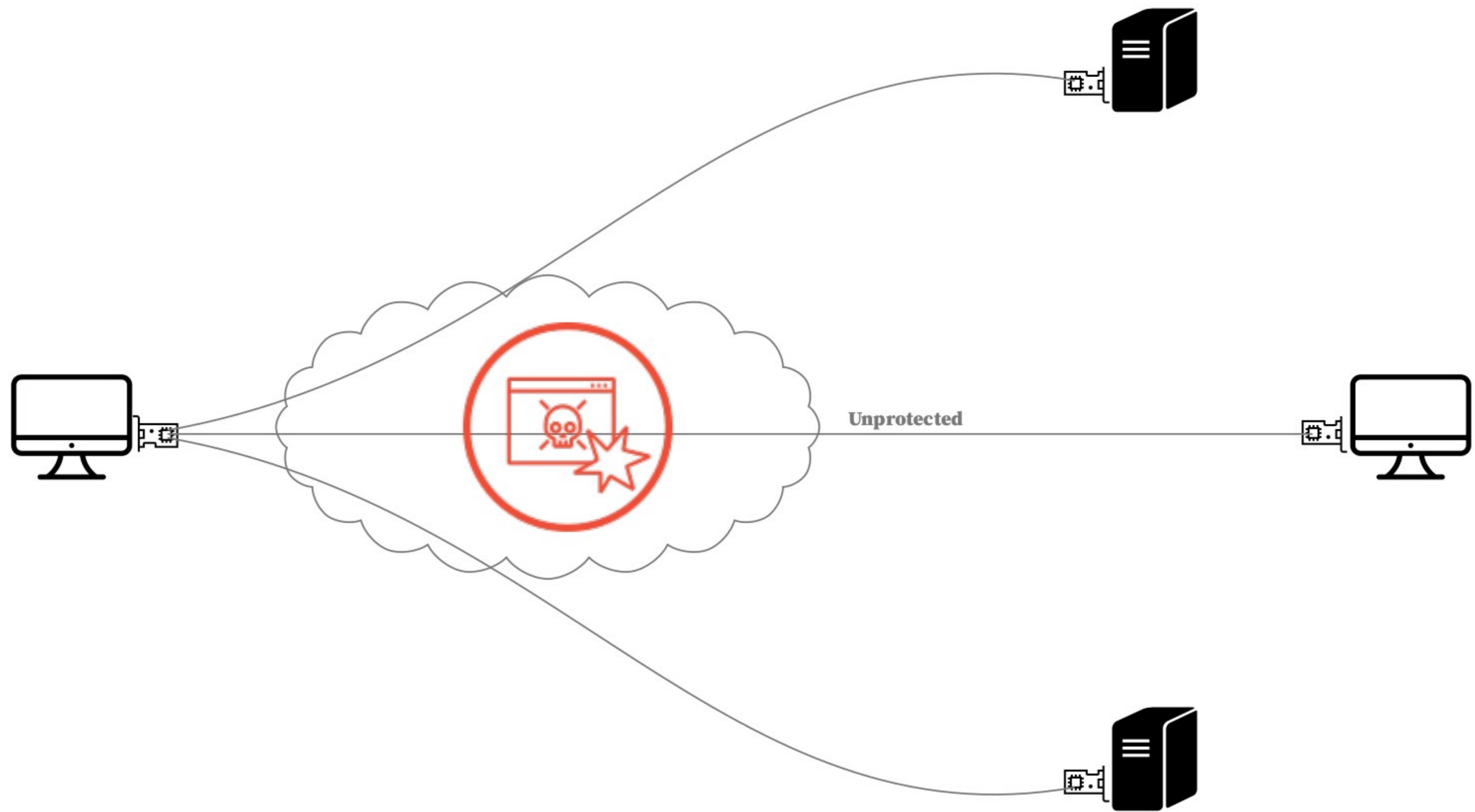
Context - VPN



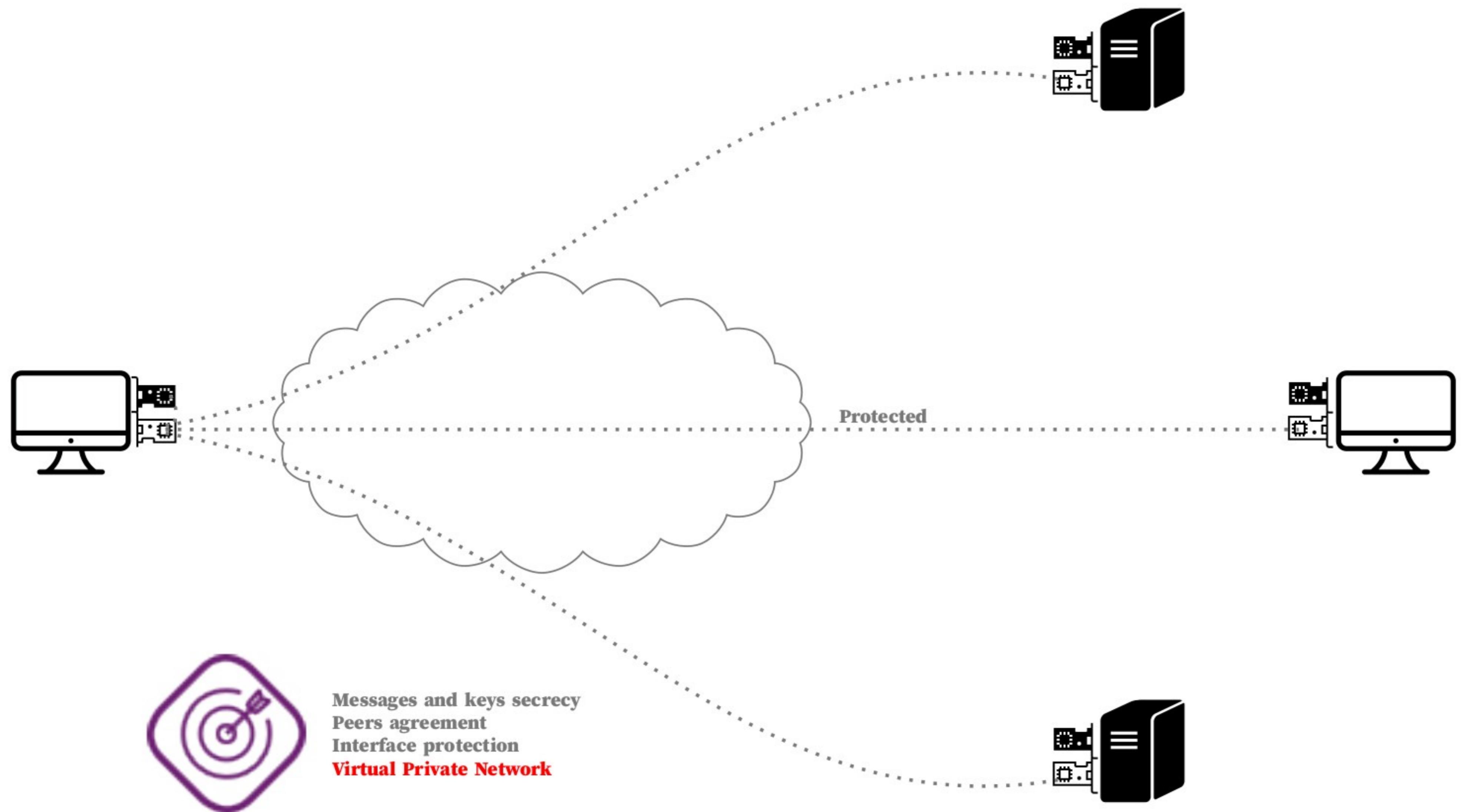
Context - VPN



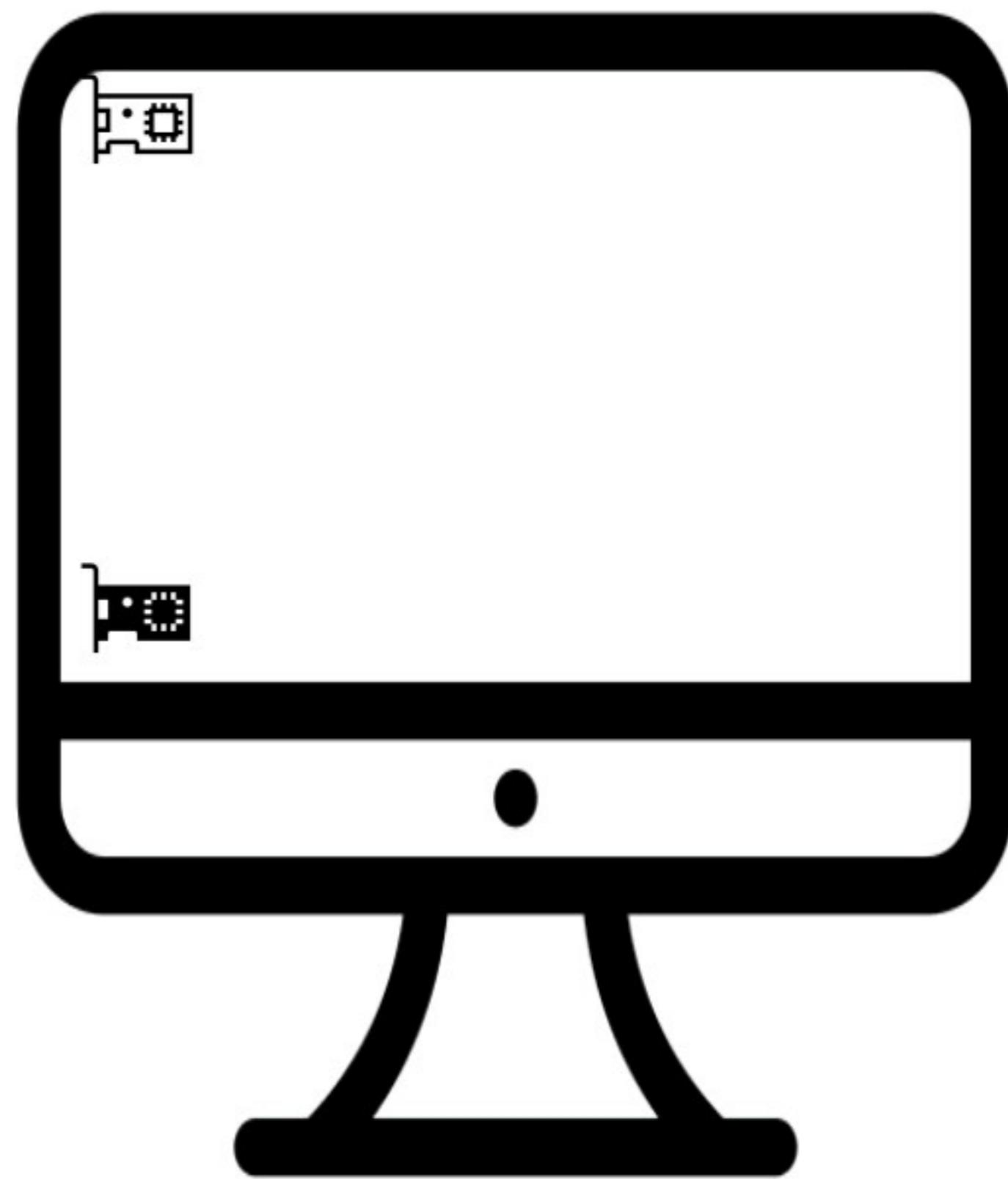
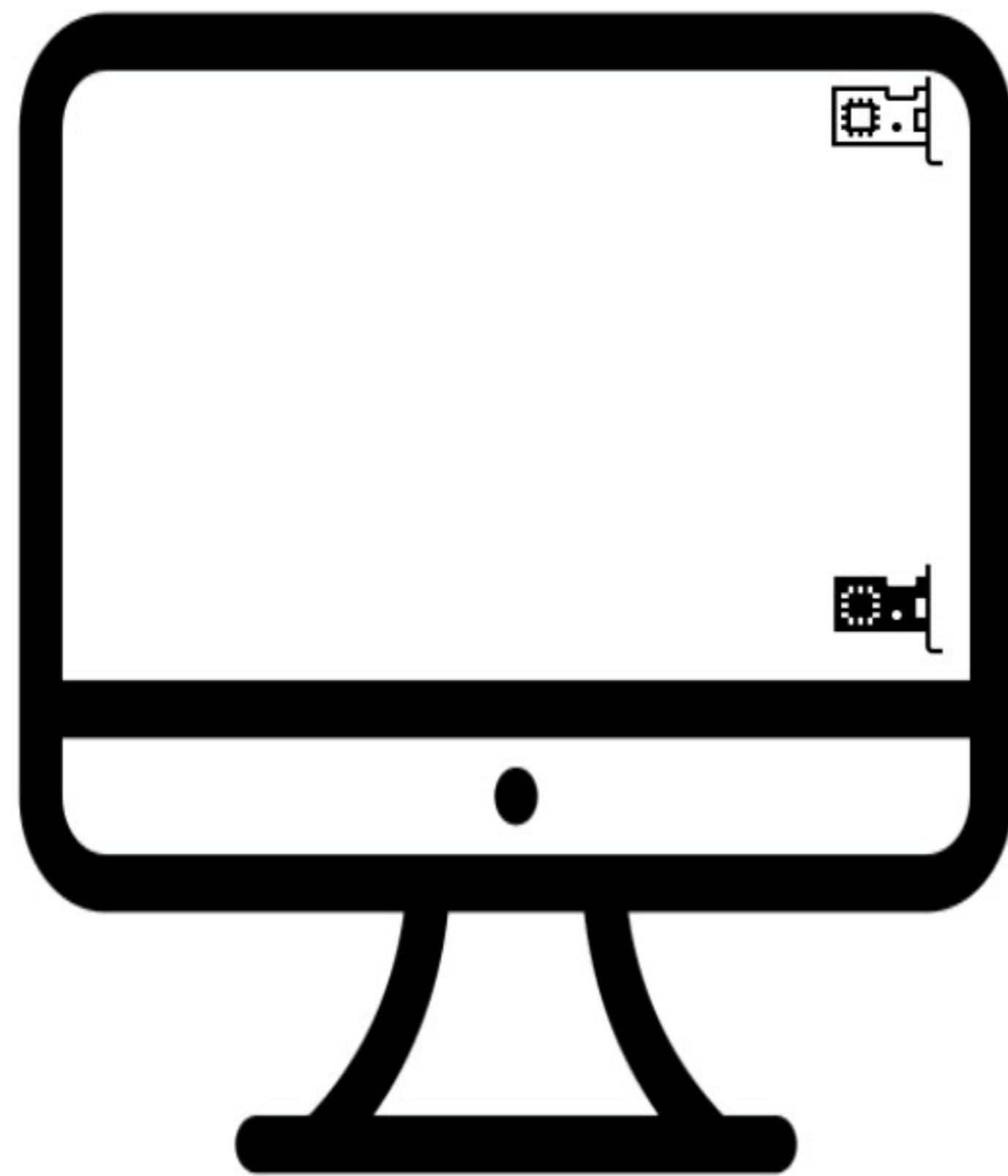
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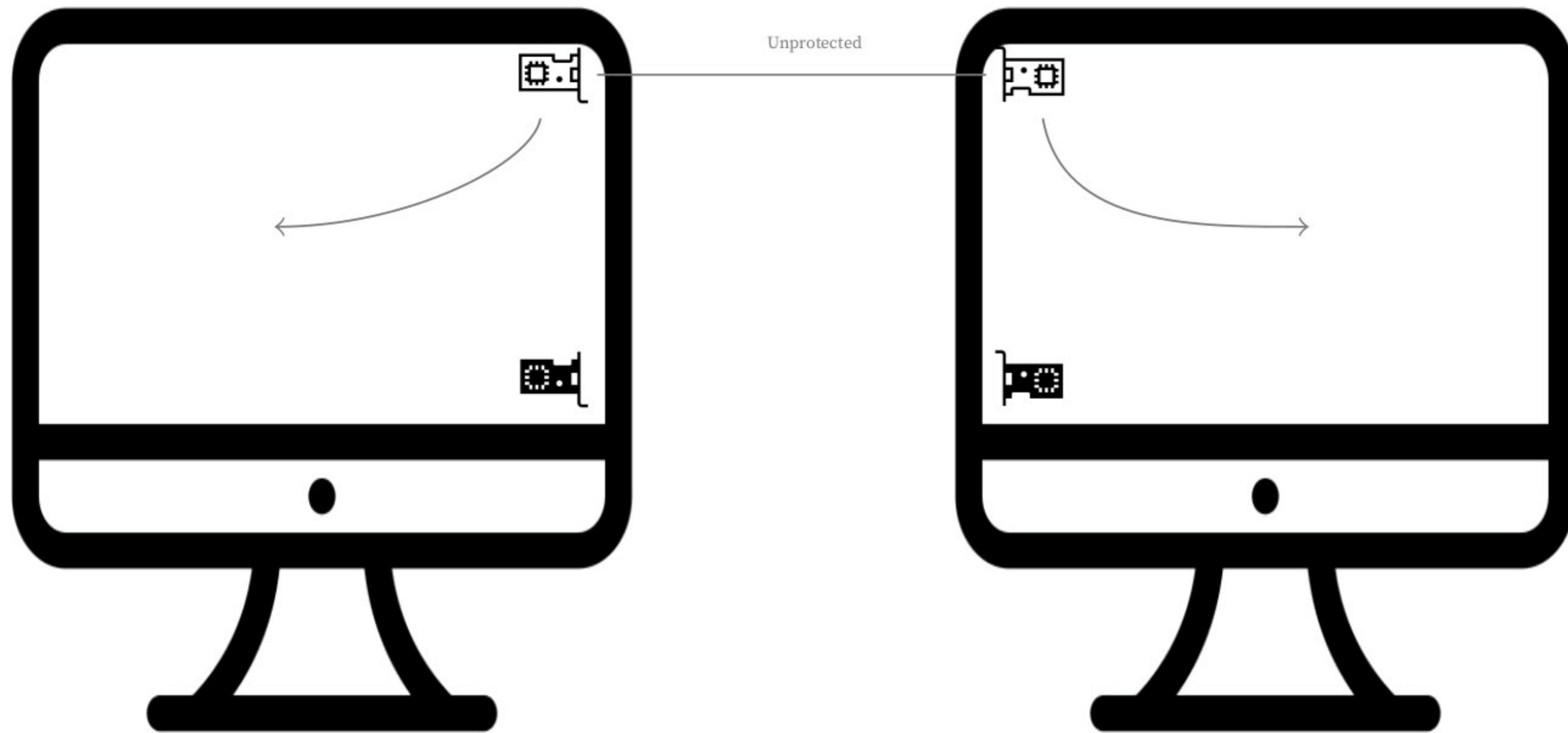
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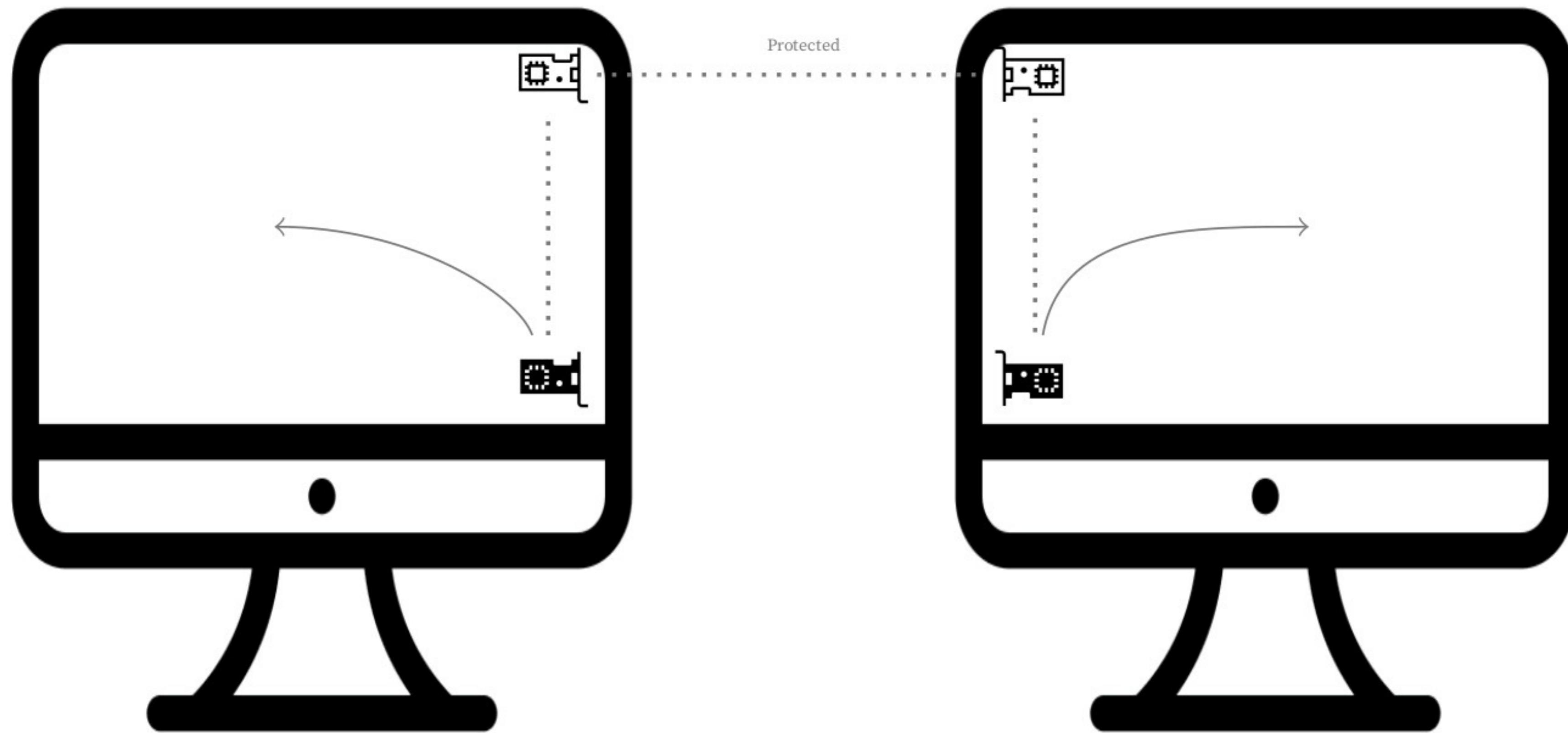
Context - VPN



Context - VPN



Context - VPN



WireGuard, a simple protocol

Main features

- ▶ New VPN solution (tunnel mode)
 - ▶ Integrated in Linux Kernel
 - ▶ Simple, light
 - ▶ Open source
 - ▶ IOS, Android, Windows, Go, ...

WireGuard, a simple protocol

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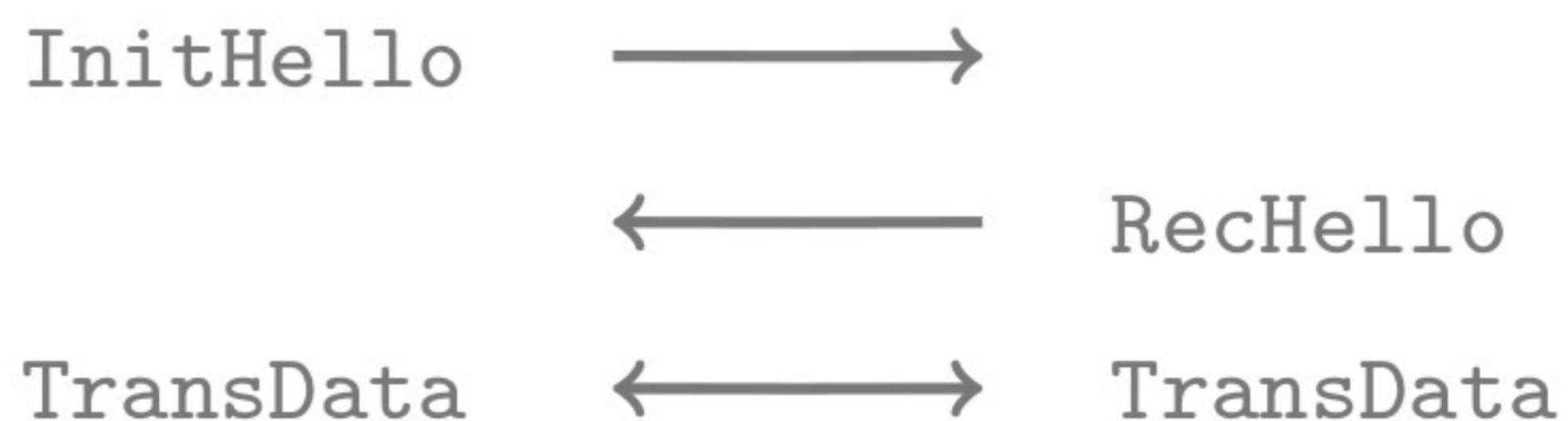
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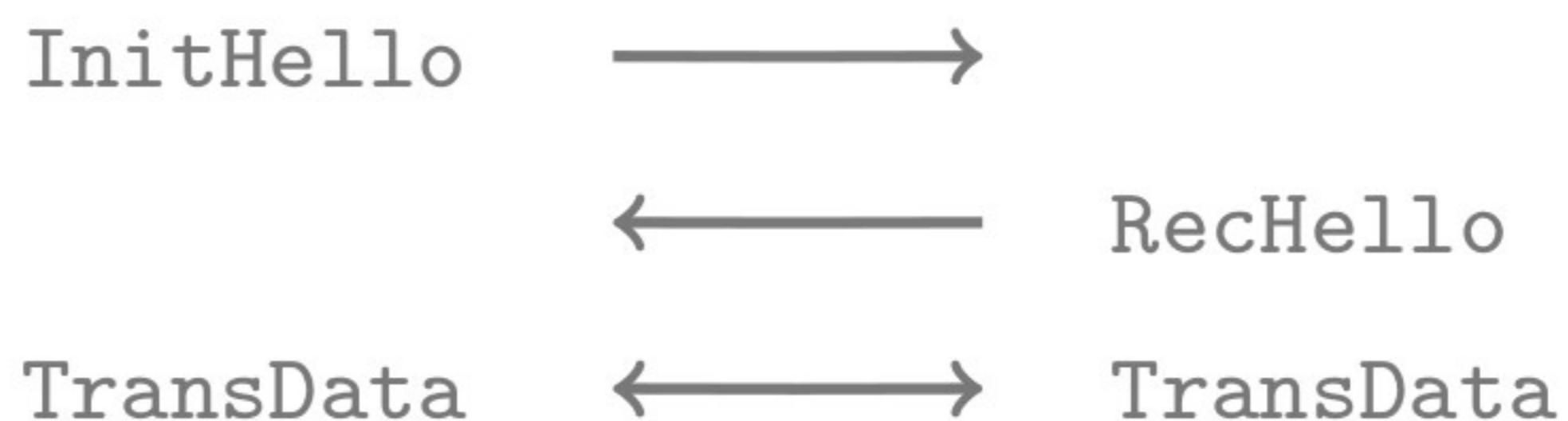
WireGuard, a simple protocol

Main features

- ▶ New VPN solution (tunnel mode)
 - ▶ Integrated in Linux Kernel
 - ▶ Simple, light
 - ▶ Open source
 - ▶ IOS, Android, Windows, Go, ...

No crypto-agility

- ▶ Curve25519
 - ▶ AEAD_CHACHA20_POLY1305
 - ▶ Blake2s
 - ▶ KDF₁, KDF₂, KDF₃
 - ▶ IKpsk2



Key agreement - IKEpsk2 in action

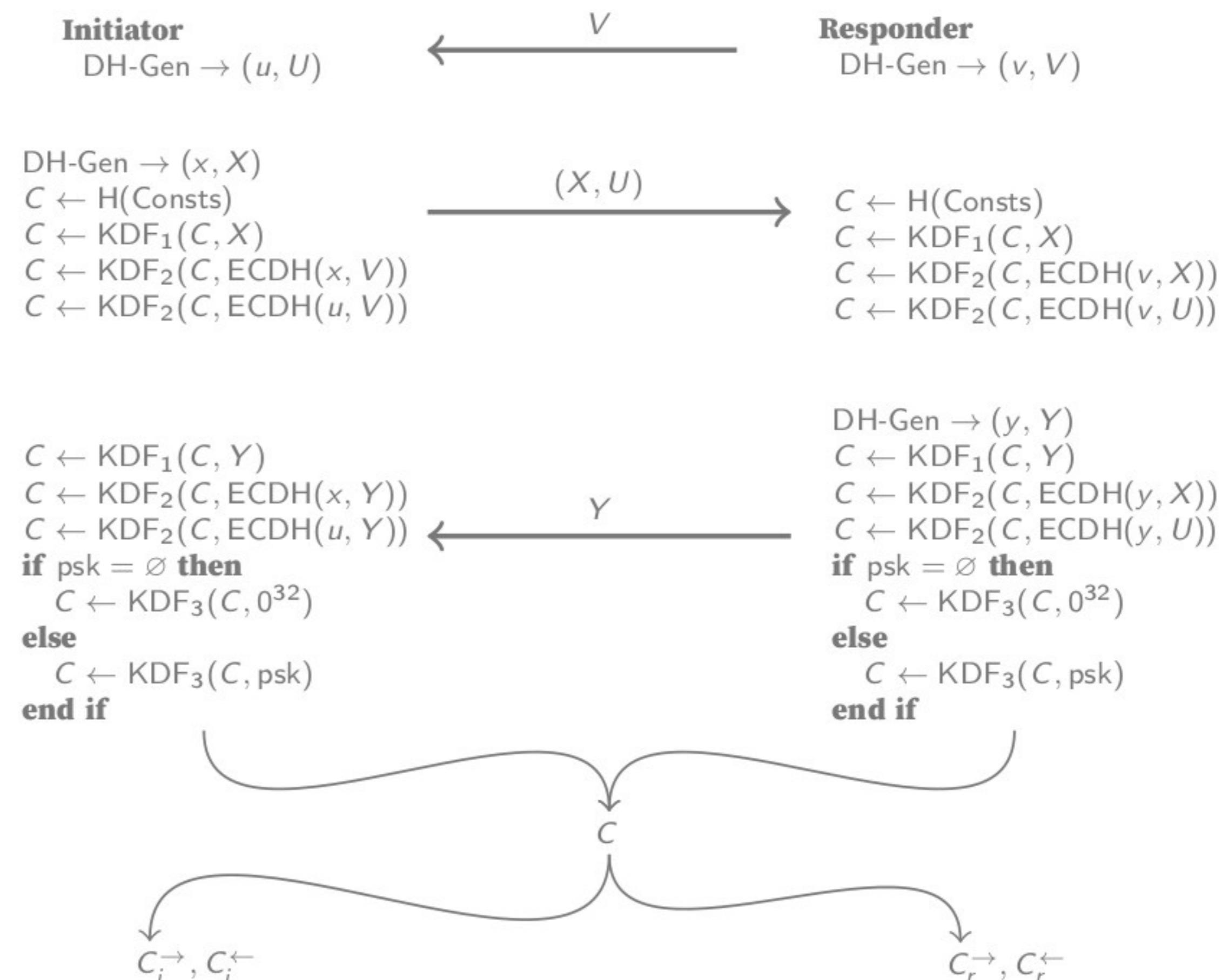
IKpsk2

```
<- s  
...  
-> e, es, s, ss  
<- e, ee, se, psk  
<-  
->
```

Key agreement - IKpsk2 in action

IKpsk2

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Key agreement - IKpsk2 in action

IKpsk2

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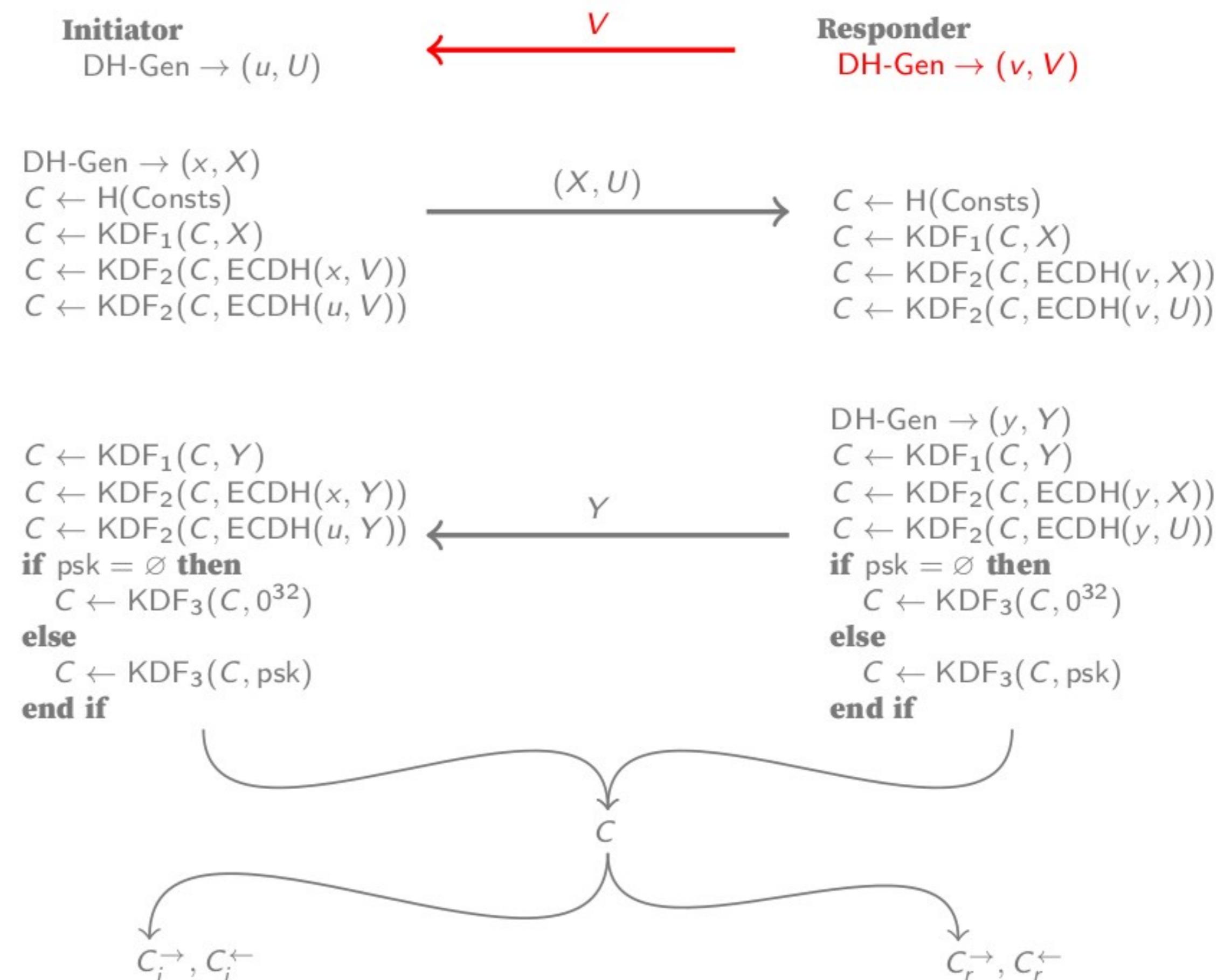
•

-> e, es, s, ss

<- e, ee, se, psk

<-

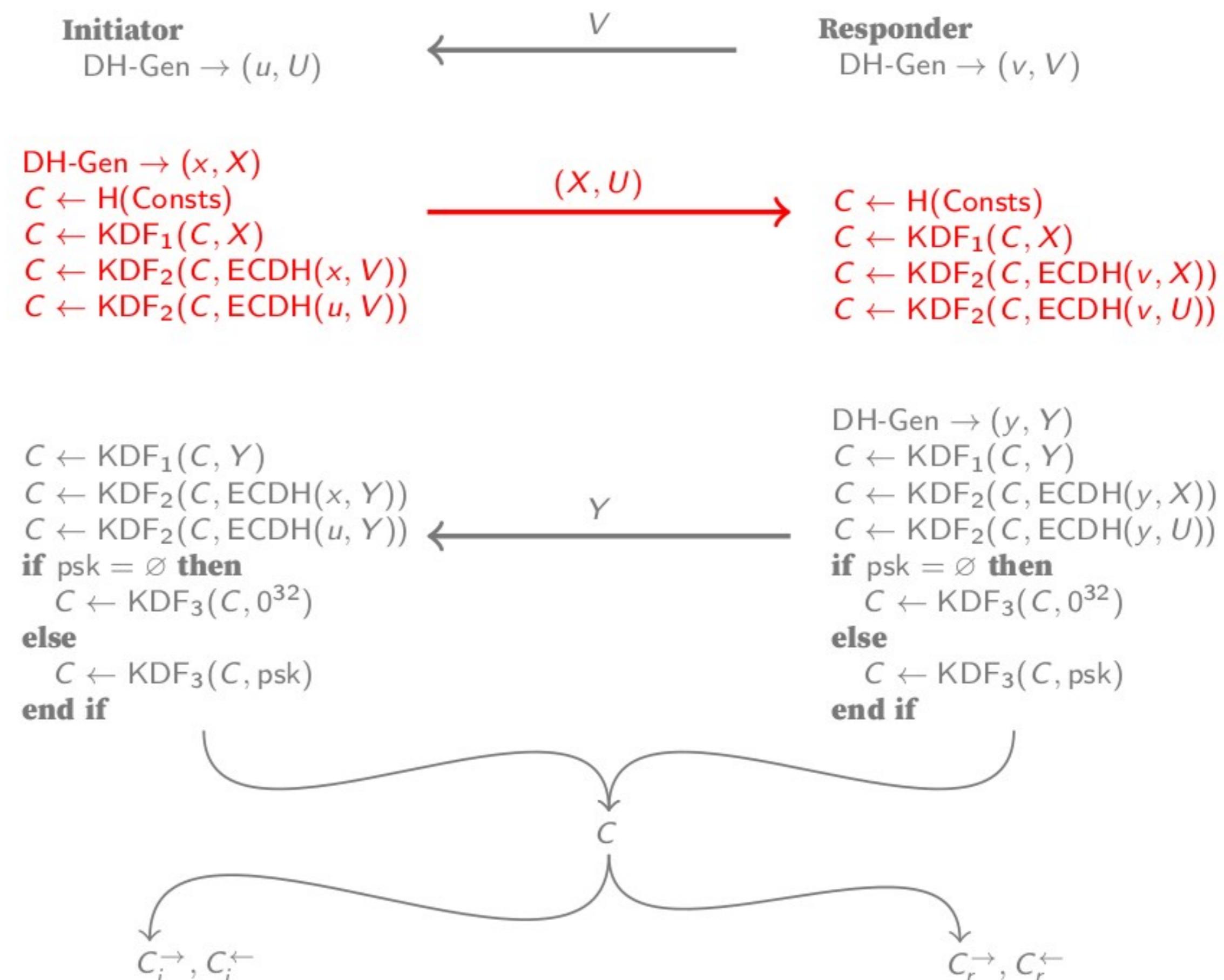
->



Key agreement - IKePSK2 in action

IKpsk2

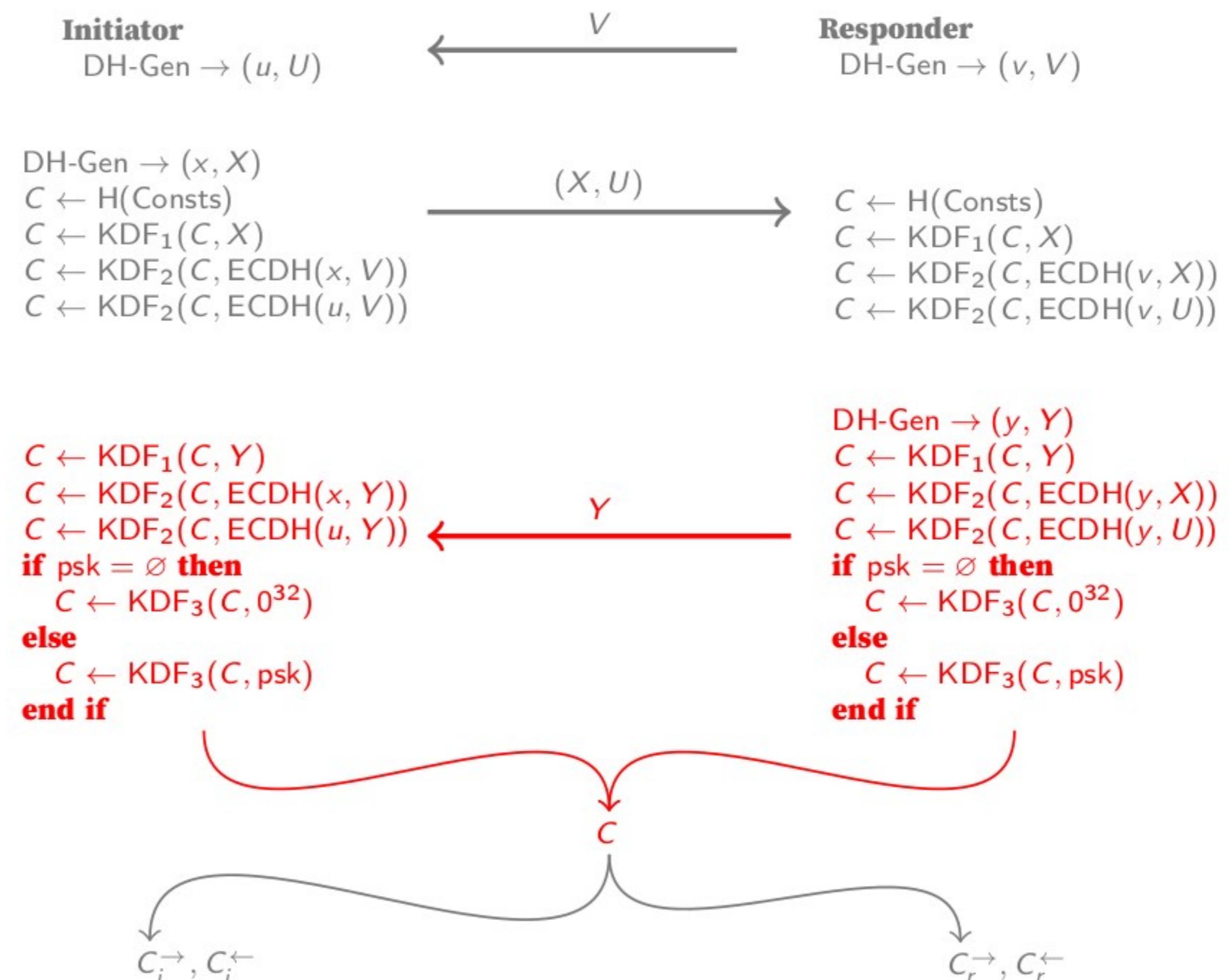
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Key agreement - IKePSK2 in action

IKpsk2

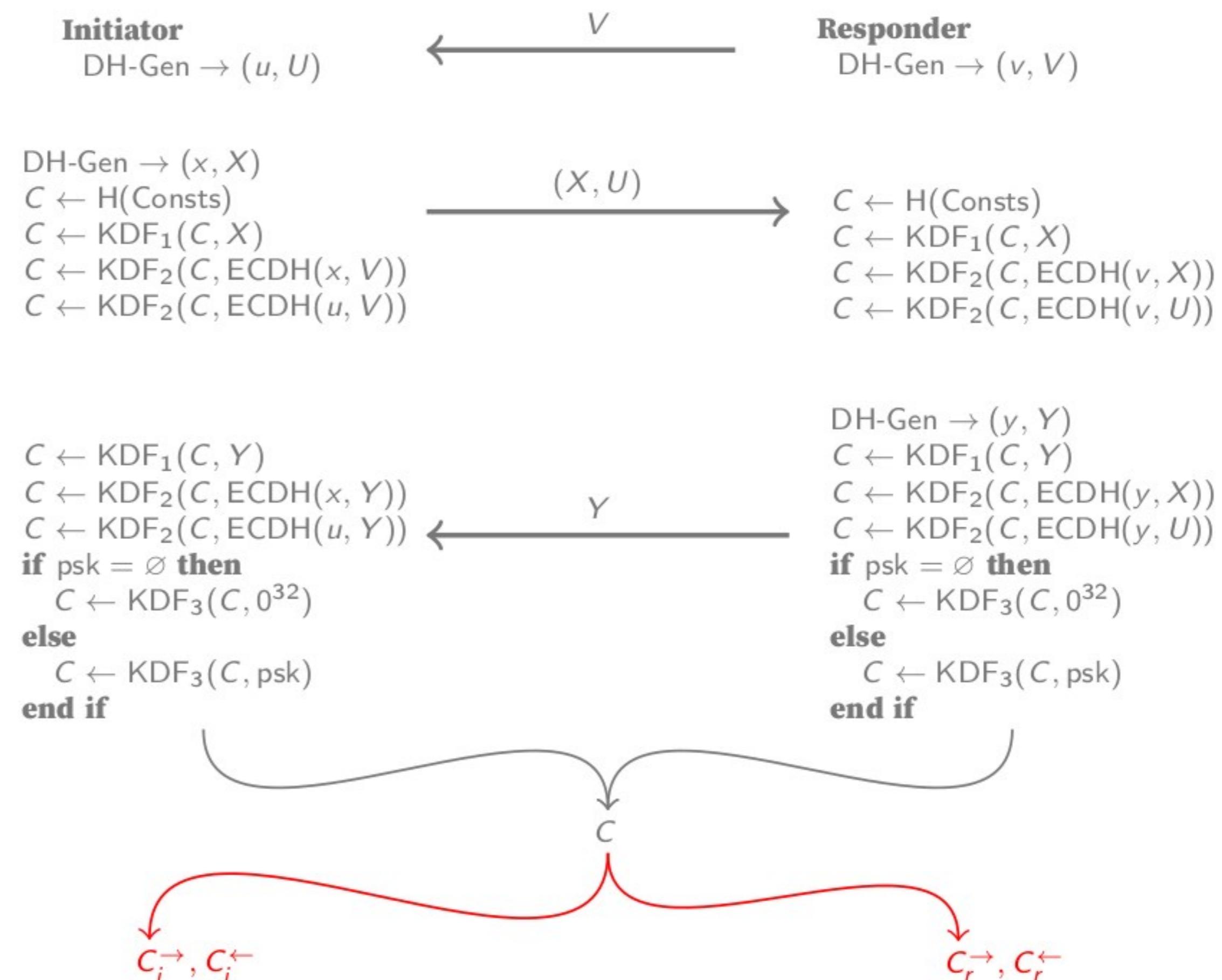
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Key agreement - IKpsk2 in action

IKpsk2

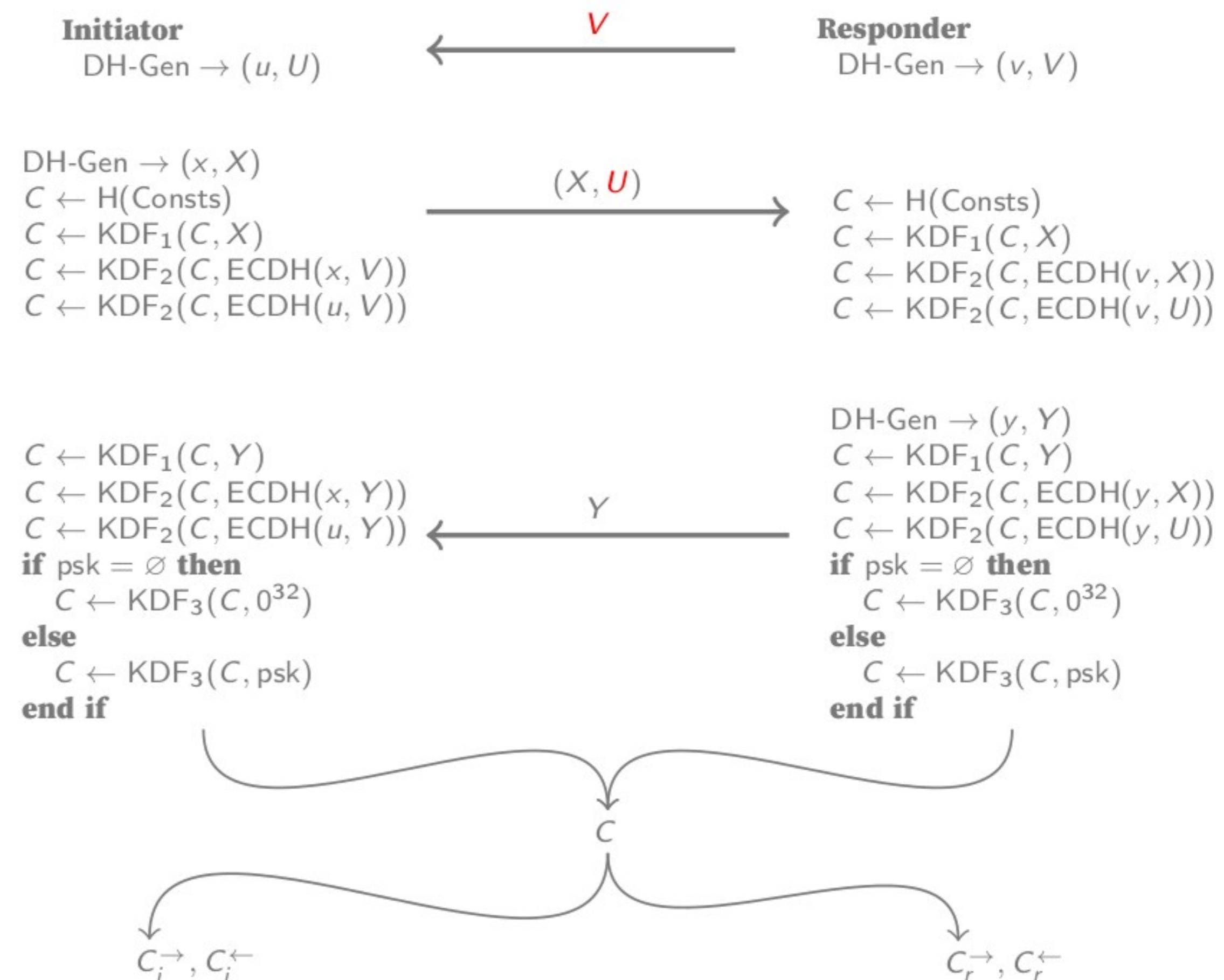
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Key agreement - IKpsk2 in action

IKpsk2

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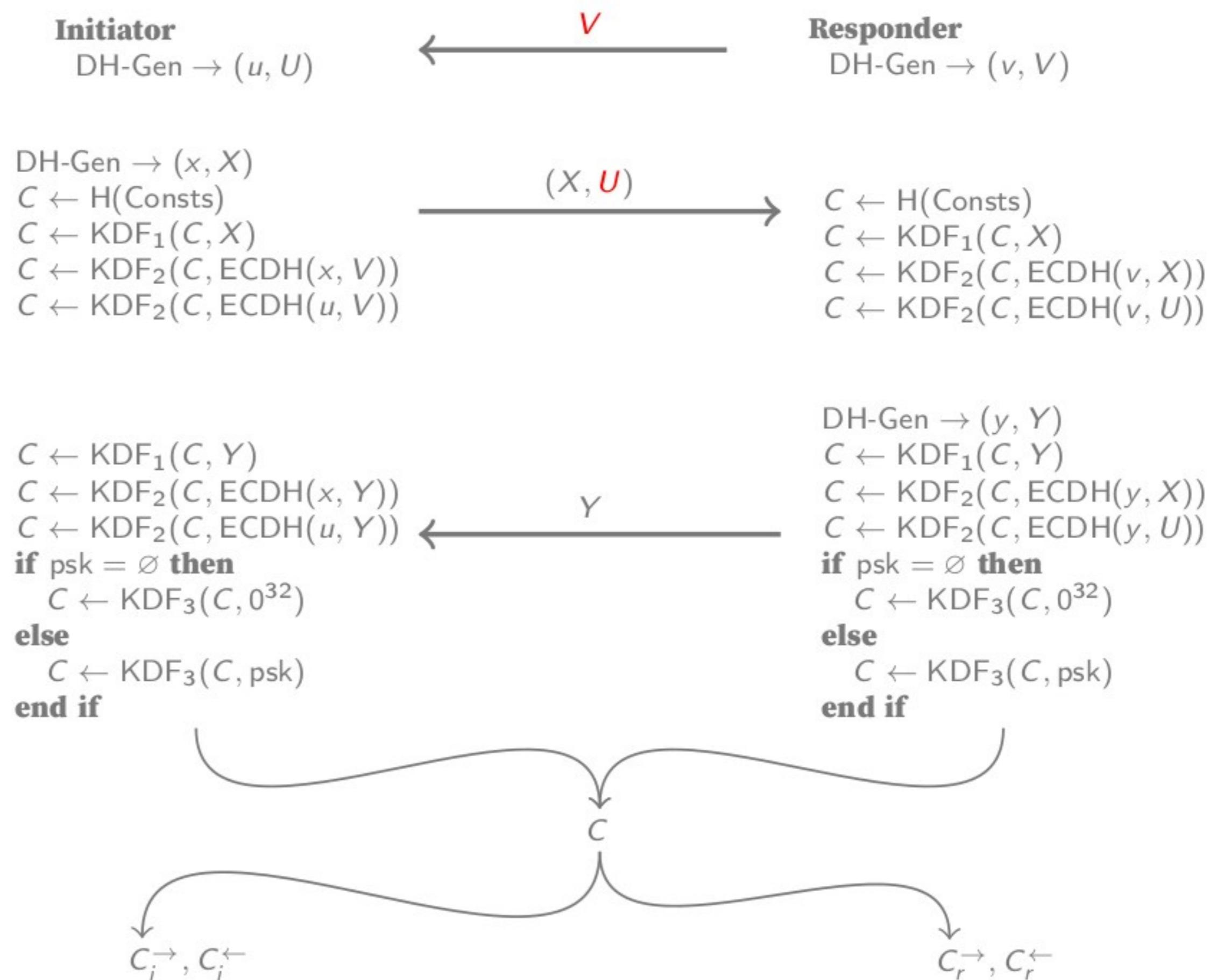
Static keys validation

- Noise specification: it's up to the application to determine whether the remote party's static public key is acceptable.

Key agreement - IKpsk2 in action

IKpsk2

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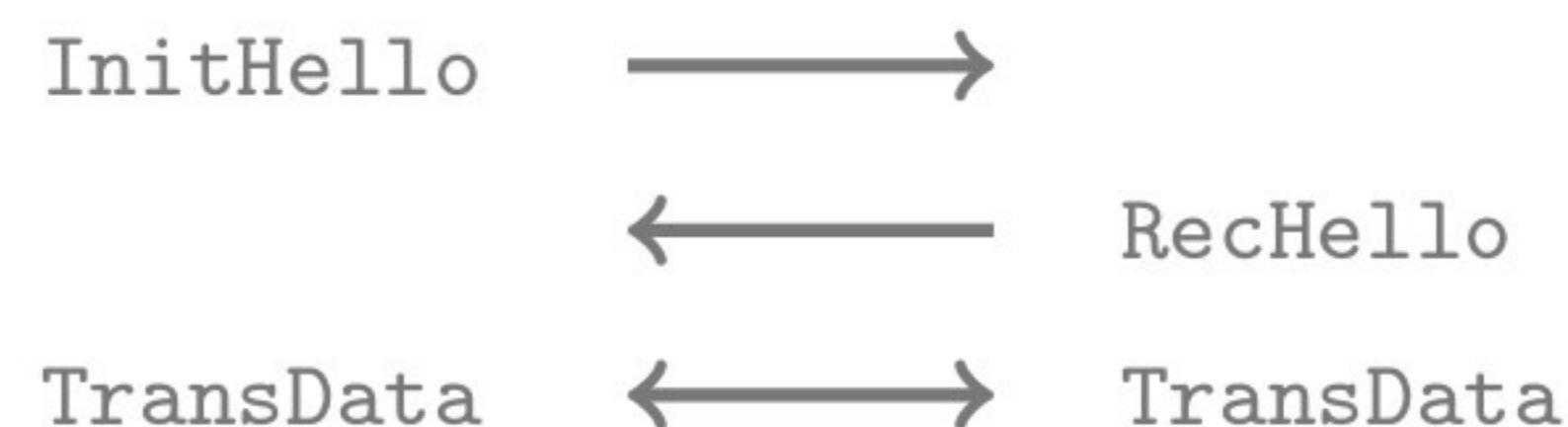
Static keys validation

- Noise specification: *it's up to the application to determine whether the remote party's static public key is acceptable.*
 - WireGuard specification: *WireGuard rests upon peers exchanging static public keys with each other.*

→ Not done in WireGuard ...

From simple to complete protocol

At first specified WireGuard protocol is simple ...



From simple to complete protocol

... initial static key exchange needs to be taken into account ...



From simple to complete protocol

... key exchange is considered complete *after* first transport message ...



From simple to complete protocol

... cookie messages are used to protect against DOS attacks.



Current analyses

Specifications

- 2017: J.A. Donenfeld, “WireGuard: Next generation kernel network tunnel”
 - 2018: T. Perrin, “The noise protocol framework”

Two types of proofs

- ▶ Computational:
 - ▶ Manual
 - ▶ Computer-aided (CRYPTOVERIF)
 - ▶ Symbolic, computer-aided:
 - ▶ PROVERIF
 - ▶ TAMARIN

Current analyses

Symbolic

- 2018: J. A. Donenfeld and K. Milner, “Formal verification of the WireGuard protocol” *WireGuard*
 - 2019: N. Kobeissi, G. Nicolas, and K. Bhargavan, “Noise explorer: Fully automated modeling and verification for arbitrary noise protocols” *IKpsk2*
 - 2020: G. Girol, L. Hirschi, R. Sasse, D. Jackson, C. Cremers, and D. A. Basin, “A spectral analysis of noise: A comprehensive, automated, formal analysis of Diffie-Hellman protocols” *IKpsk2*

Computational

- 2018: B. Dowling and K. G. Paterson, “A cryptographic analysis of the WireGuard protocol” *WireGuard*
 - 2019: B. Lipp, B. Blanchet, and K. Bhargavan, “A mechanised cryptographic proof of the “WireGuard virtual private network protocol” *WireGuard*

Current analyses



What is the scope of *WireGuard* analyses ?

- ▶ Lazy answer: full protocol !
 - ▶ Correct answer: should be studied !

Are IKpsk2 analyses applicable to WireGuard?

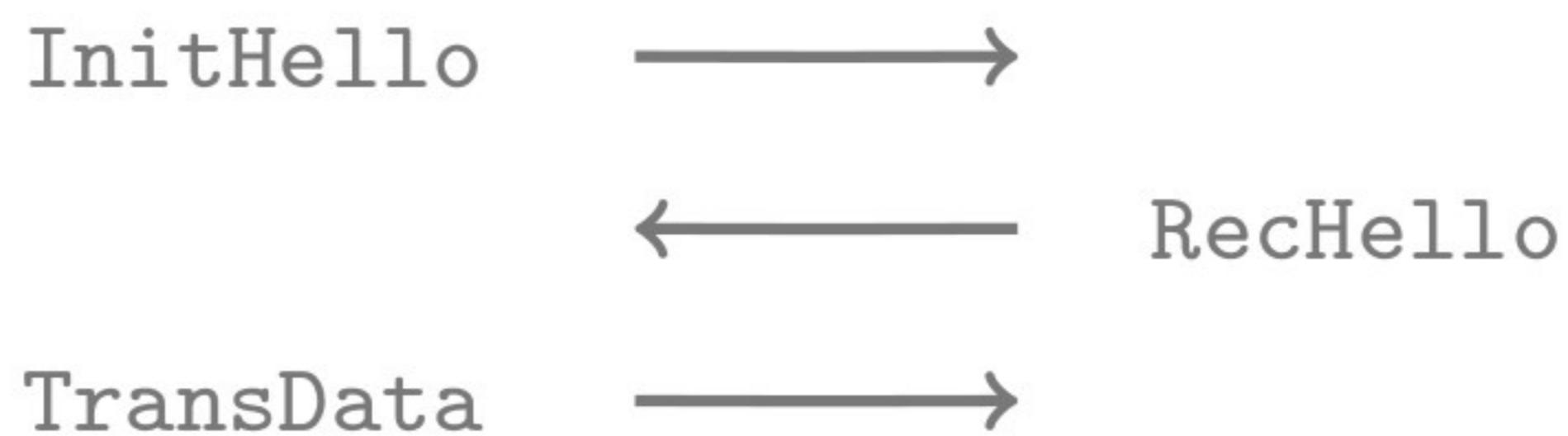
- ▶ Lazy answer: yes !
 - ▶ Correct answer: should be studied !

Are threat model equivalent?

- ▶ Lazy answer: come on we have a proof, it's enough !
 - ▶ Correct answer: should be studied !

Current analyses

What is the scope of *WireGuard* analyses?



Symbolic *WireGuard*

- 2018: J. A. Donenfeld and K. Milner, "Formal verification of the WireGuard protocol"
 - "Simple" version of the protocol (with only confirmation message) **X**
 - Initial key distribution not assessed **X**
 - No Cookie messages **X**

Current analyses

What is the scope of *WireGuard* analyses?



Computationnal *WireGuard*

- 2018: B. Dowling and K. G. Paterson, "A cryptographic analysis of the WireGuard protocol"
 - "Simple" version of the protocol (with *modified* confirmation message) **X**
 - Initial key distribution not assessed **X**
 - No Cookie messages **X**

Current analyses

What is the scope of *WireGuard* analyses?



Computationnal *WireGuard*

- 2019: B. Lipp, B. Blanchet, and K. Bhargavan, “A mechanised cryptographic proof of the WireGuard VPN protocol”

- "Complete" protocol (with confirmation message and transport messages) ✓
 - Initial key distribution ✓
 - Cookie messages not included in full protocol, but in a separate model ✗

Current analyses

Are IKpsk2 analyses applicable to WireGuard?

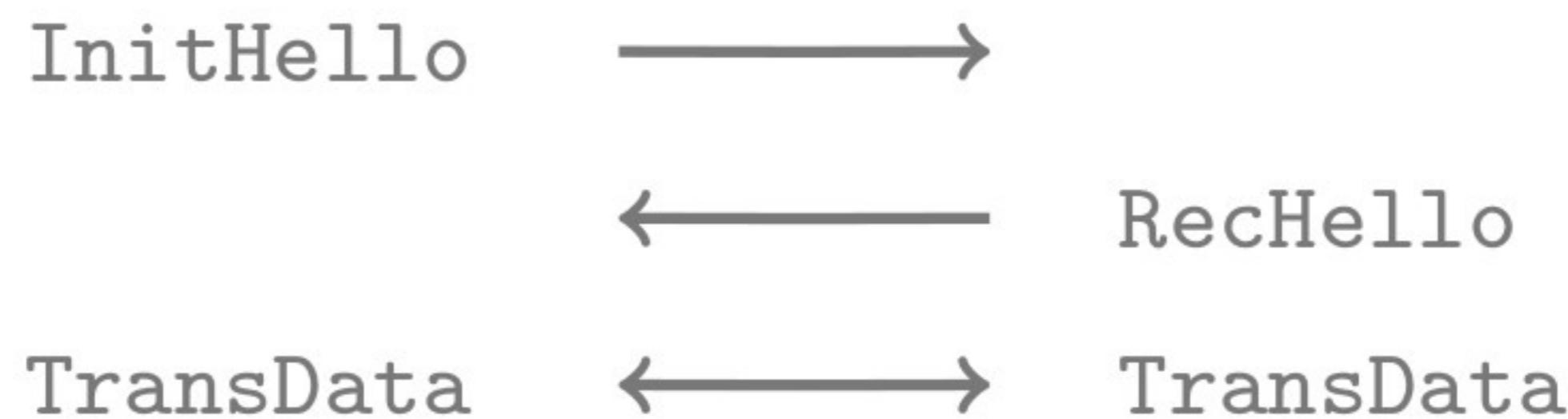


InitHello	RecHello
type(1)	type(2)
reserved	reserved
sender	sender
ephemeral	ephemeral
static	receiver
timestamp	empty
mac1	mac1
mac2	mac2
TransData	Cookie
type(3)	type(4)
reserved	reserved
receiver	receiver
counter	nonce
packet	cookie

- Fields static, timestamp, empty are specific to WireGuard
 - WireGuard includes
 - session identifiers sender, receiver
 - MAC computations mac1, mac2
 - Cookie messages

Current analyses

Are IKpsk2 analyses applicable to WireGuard?

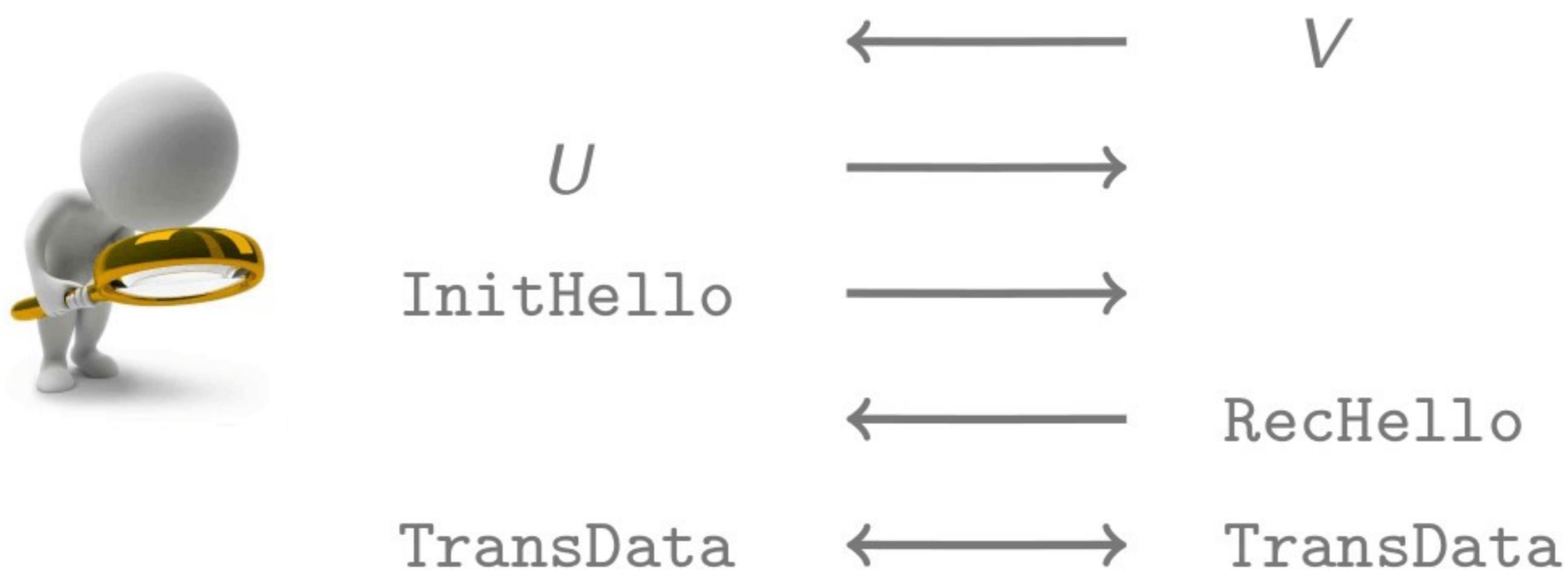


Symbolic *IKpsk2*

- 2019: N. Kobeissi, G. Nicolas, and K. Bhargavan, "Noise explorer: Fully automated modeling and verification for arbitrary noise protocols"
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Current analyses

Are IKpsk2 analyses applicable to WireGuard?



Symbolic *IKpsk2*

- 2020: G. Girol, L. Hirschi, R. Sasse, D. Jackson, C. Cremers, and D. A. Basin, "A spectral analysis of noise: A comprehensive, automated, formal analysis of Diffie-Hellman protocols"
 - "Simple" version of the protocol ✗
 - No confirmation message ✗
 - Initial key distribution assessed ✓

Current analyses

Threat models also differ !



Threats

- ▶ Static private key reveal / set
 - ▶ Ephemeral private key reveal / set
 - ▶ PSK reveal / set
 - ▶ Static key distribution corruption

Current analyses

Threat models also differ !



Threats

- Static private key reveal ✓ / set ✗
 - Ephemeral private key reveal ✓ / set ✗
 - PSK reveal ✓ / set ✗
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Symbolic *WireGuard*

- 2018: J. A. Donenfeld and K. Milner, “Formal verification of the WireGuard protocol”

Proof

- ## ► Computer-aided (TAMARIN)

Current analyses

Threat models also differ !



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- ▶ Static private key reveal ✓ / set ✗
- ▶ Ephemeral private key reveal ✓ / set ✗
- ▶ PSK reveal ✓ / set ✗
- ▶ Static key distribution corruption ✗

Computationnal **WireGuard**

- ▶ 2018: B. Dowling and K. G. Paterson, "A cryptographic analysis of the WireGuard protocol"

Proof

- ▶ Manual

Current analyses

Threat models also differ !



Threats

- ▶ Static private key reveal ✓ / set ✓
- ▶ Ephemeral private key reveal ✓ / set ✗
- ▶ PSK reveal ✓ / set ✓
- ▶ Static key distribution corruption ✓

Computationnal **WireGuard**

- ▶ 2019: B. Lipp, B. Blanchet, and K. Bhargavan, "A mechanised cryptographic proof of the WireGuard VPN protocol"

Proof

- ▶ Computer-aided (CRYPTOVERIF)

Current analyses

Threat models also differ !



Threats

- ▶ Static private key reveal ✓ / set ✗
- ▶ Ephemeral private key reveal ✗ / set ✗
- ▶ PSK reveal ✓ / set ✗
- ▶ Static key distribution corruption ✗

Symbolic IK_{psk2}

- ▶ 2019: N. Kobeissi, G. Nicolas, and K. Bhargavan, "Noise explorer: Fully automated modeling and verification for arbitrary noise protocols"

Proof

- ▶ Computer-aided (PROVERIF)

Current analyses

Threat models also differ !



Threats

- Static private key reveal ✓ / set ✓
 - Ephemeral private key reveal ✓ / set ✓
 - PSK reveal ✓ / set ✓
 - Static key distribution corruption ✓

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Proof

- ## ► Computer-aided (TAMARIN)

New model

Objective

- Be as complete as possible !
 - Key distribution
 - Confirmation message
 - Include Cookie message in full protocol
 - Focus on Symbolic analysis.
 - Should be verifiable with TAMARIN and PROVERIF.

New model

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 - Key distribution
 - Confirmation message
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 - Should be verifiable with TAMARIN and PROVERIF.



New proof assistant: **SAPIC**⁺

- 2022: V. Cheval, C. Jacomme, S. Kremer, and R. Künnemann, “SAPIC⁺: protocol verifiers of the world, unite!”

Target model



- "Complete" protocol (with confirmation message and transport messages) ✓
 - Initial key distribution ✓
 - Cookie messages included in full protocol ✓

Target threat model



Threats

- Static private key reveal ✓ / set ✓
 - Ephemeral private key reveal ✓ / set ✓
 - PSK reveal ✓ / set ✓
 - Static key distribution corruption ✓
 - **New!** Precomputation reveal ✓ / set ✓

Precomputation ?

- WireGuard implements static key ECDH precomputation.
 - That is
 - Initiator implements $\text{ECDH}(u, V)$
 - Responder implements $\text{ECDH}(v, U)$

before session begins, hence WireGuard maintains it.

Compromise of ECDH precomputation is *weaker* than compromise of private static keys:

- if adv. has v and g^u , adv. has g^{uv} ,
 - however if adv. has g^u and g^{uv} , adv. *does not have* v .

Methodology



- Start with a reference model with all "Gets" threats in SAPIC⁺
 - Derivate PROVERIF models for "Sets" threats
 - Verify queries on all derivated models in PROVERIF

How many models ? How many queries ?

- ▶ $2^9 = 512$ models, as adversary
 - ▶ Can set $u, v, \text{psk}, x, y, g^{uv}$ (for Initiator and Responder)
 - ▶ Can corrupt U and V distribution
 - ▶ And can combine !
 - ▶ Up to $2^6 = 64$ queries per model, as adversary
 - ▶ Can get $u, v, \text{psk}, x, y, g^{uv}$
 - ▶ And can combine !
 - ▶ Can be simplified (e.g no need to test adversary that gets and sets u .)
⇒ **4860** queries for each security property (instead of $2^{15} = 32768$) !



Illustration - reference model

process:

```
new ~ltkI;  
new ~ltkR;  
new ~psk;
```

new empty;

```
out(<'initiator', 'g'~~ltkI>);  
out(<'responder', 'g'~~ltkR>);  
out(empty);
```

!

```
Initiator(~ltkI, 'g'~~ltkI, 'g'~~ltkR, ('g'~~ltkR)~~ltkI, ~psk, empty, 'zero')
| Responder(~ltkR, 'g'~~ltkI, 'g'~~ltkR, ('g'~~ltkI)~~ltkR, ~psk, empty, 'zero')
| RevealPsk(~psk)
| RevealPri(~ltkI)
| RevealPri(~ltkR)
| RevealPre(~ltkI, ~ltkR)
```

)

```
let Initiator(~ltkI, pkI, pkR, sisr, ~psk, empty, zero_1) =  
  ...  
  new ~ekI;  
  ...  
  let pekI = 'g' ^~ ekI in  
  (  
    ...  
  )  
  | (RevealPri(~ekI))
```

```
let Responder(~ltkR, pkI, pkR, srsi, ~psk, empty, zero_1) =
  ...
  new ~ekR;
  ...
  let pekR = 'g' ^~ ekR in
  (
    ...
  )
  | (RevealPri(~ekR))
```

Illustration - model derivation (adversary sets psk and x and y)

process:

```
new ~ltkI;  
new ~ltkR;  
in(~psk);
```

new empty;

```
out(<'initiator', 'g'^~ltkI>);  
out(<'responder', 'g'^~ltkR>);  
out(empty);
```

```

!(
    Initiator(~ltkI, 'g'~~ltkI, 'g'~~ltkR, ('g'~~ltkR)~~ltkI, ~psk, empty, 'zero')
| Responder(~ltkR, 'g'~~ltkI, 'g'~~ltkR, ('g'~~ltkI)~~ltkR, ~psk, empty, 'zero')
// | RevealPsk(~psk)
| RevealPri(~ltkI)
| RevealPri(~ltkR)
| RevealPre(~ltkI, ~ltkR)
)

```

```
let Initiator(~ltkI, pkI, pkR, sisr, ~psk, empty, zero_1) =  
  ...  
  in(~ekI);  
  ...  
  let pekI  = 'g'^~ekI in  
  (  
    ...  
  )  
  // | (RevealPri(~ekI))
```

```
let Responder(~ltkR, pkI, pkR, srsi, ~psk, empty, zero_1) =
  ...
  in (~ekR);
  ...
  let pekR = 'g' ^~ ekR in
  (
  ...
  )
  // | (RevealPri(~ekR))
```

Methodology



- Verify queries on all derived models in PROVERIF
 - Extract all "true" properties
 - Compute a combination of all "true" properties

Combination of all "true" properties ?

- ▶ Compute conjunction.
 - ▶ Compute DNF.

⇒ compact result !

Inspired by:

Symbolic *IKpsk2*

- 2020: G. Girol, L. Hirschi, R. Sasse, D. Jackson, C. Cremers, and D. A. Basin, “A spectral analysis of noise: A comprehensive, automated, formal analysis of Diffie-Hellman protocols”

Illustration with agreement on 3rd message

Verify all 4860 queries ...

```

query i:time, j:time, pki:bitstring, pkr:bitstring, peki:bitstring, pekr:bitstring, psk:bitstring, ck:bitstring;
(event(eRConfirm(pki, pkr, peki, pekr, psk, ck))@i)
==> ((event(eIConfirm(pki, pkr, peki, pekr, psk, ck))@j) && (j < i))).
```

```

query i:time, j:time, pki:bitstring, pkr:bitstring, peki:bitstring, pekr:bitstring, psk:bitstring, ck:bitstring,
j1:time, j2:time, j3:time, j4:time, j5:time, j6:time;
(event(eRConfirm(pki, pkr, peki, pekr, psk, ck))@i)
==> (((event(eIConfirm(pki, pkr, peki, pekr, psk, ck))@j) && (j < i))
||((event(eRevPri(pki))@j1) && (j1 < i))
||((event(eRevPri(pkr))@j2) && (j2 < i))
||((event(eRevPri(peki))@j3) && (j3 < i))
||((event(eRevPri(pekr))@j4) && (j4 < i))
||((event(eRevPre(pki, pkr))@j5) && (j5 < i))
||((event(eRevPsk(psk))@j6) && (j6 < i))).
```



- ▶ **1824** queries are "true"
 - ▶ **3036** queries are "false"
 - ▶ **0** queries are "cannot be proved"

Illustration with agreement on 3rd message

Extract and compute DNF requires the use of symbols:

- D_u, D_v : adversary corrupts public keys distribution
 - $R_u, R_v, R_x, R_y, R_s, R_c$: adversary gets private keys (u, v, x, y) , psk (s) or precomp. value (c)
 - $M_u, M_v, M_x, M_y, M_s, M_i, M_r$: adversary sets private keys (u, v, x, y) , psk (s) or precomp value $(i$ for Initiator, r for Responder)

$\text{DNF} = (\text{Du} \ \& \ \text{Rs}) \mid (\text{Ms} \ \& \ \text{Ru}) \mid (\text{Mu} \ \& \ \text{Rs}) \mid (\text{Rs} \ \& \ \text{Ru}) \mid (\text{Mi} \ \& \ \text{Ms} \ \& \ \text{Ry}) \mid (\text{Mi} \ \& \ \text{My} \ \& \ \text{Rs}) \mid (\text{Mi} \ \& \ \text{Rs} \ \& \ \text{Ry}) \mid$
 $(\text{Mr} \ \& \ \text{Ms} \ \& \ \text{Ry}) \mid (\text{Mr} \ \& \ \text{My} \ \& \ \text{Rs}) \mid (\text{Mr} \ \& \ \text{Rs} \ \& \ \text{Ry}) \mid (\text{Ms} \ \& \ \text{Mv} \ \& \ \text{Ry}) \mid (\text{Ms} \ \& \ \text{My} \ \& \ \text{Rc}) \mid (\text{Ms} \ \& \ \text{My} \ \& \ \text{Rv}) \mid$
 $(\text{Ms} \ \& \ \text{Rc} \ \& \ \text{Ry}) \mid (\text{Ms} \ \& \ \text{Rv} \ \& \ \text{Ry}) \mid (\text{Mv} \ \& \ \text{My} \ \& \ \text{Rs}) \mid (\text{Mv} \ \& \ \text{Rs} \ \& \ \text{Ry}) \mid (\text{My} \ \& \ \text{Rc} \ \& \ \text{Rs}) \mid (\text{My} \ \& \ \text{Rs} \ \& \ \text{Rv}) \mid$
 $(\text{Rc} \ \& \ \text{Rs} \ \& \ \text{Ry}) \mid (\text{Rs} \ \& \ \text{Rv} \ \& \ \text{Ry})$

Interpretation

We have agreement on 3rd message ***unless*** adversary

- ▶ compromises initiator's static key distribution **AND** gets psk
 - ▶ **OR** sets psk **AND** gets initiator's static private key u
 - ▶ **OR** ...
 - ▶ **OR** gets psk **AND** gets responder's static private key v **OR** **AND** gets responder's ephemeral private key y

Illustration with agreement on 3rd message

Extract, compute DNF. Requires the use of symbols:

- D_u, D_v : adversary corrupts public keys distribution
 - $R_u, R_v, R_x, R_y, R_s, R_c$: adversary gets private keys (u, v, x, y) , psk (s) or precomp. value (c)
 - $M_u, M_v, M_x, M_y, M_s, M_i, M_r$: adversary sets private keys (u, v, x, y) , psk (s) or precomp value $(i$ for Initiator, r for Responder)

$$\text{DNF} = (\text{Du} \wedge \text{Rs}) \mid (\text{Ms} \wedge \text{Ru}) \mid (\text{Mu} \wedge \text{Rs}) \mid (\text{Rs} \wedge \text{Ru}) \mid (\text{Mi} \wedge \text{Ms} \wedge \text{Ry}) \mid (\text{Mi} \wedge \text{My} \wedge \text{Rs}) \mid (\text{Mi} \wedge \text{Rs} \wedge \text{Ry}) \mid \\ (\text{Mr} \wedge \text{Ms} \wedge \text{Ry}) \mid (\text{Mr} \wedge \text{My} \wedge \text{Rs}) \mid (\text{Mr} \wedge \text{Rs} \wedge \text{Ry}) \mid (\text{Ms} \wedge \text{Mv} \wedge \text{Ry}) \mid (\text{Ms} \wedge \text{My} \wedge \text{Rc}) \mid (\text{Ms} \wedge \text{My} \wedge \text{Rv}) \mid \\ (\text{Ms} \wedge \text{Rc} \wedge \text{Ry}) \mid (\text{Ms} \wedge \text{Rv} \wedge \text{Ry}) \mid (\text{Mv} \wedge \text{My} \wedge \text{Rs}) \mid (\text{Mv} \wedge \text{Rs} \wedge \text{Ry}) \mid (\text{My} \wedge \text{Rc} \wedge \text{Rs}) \mid (\text{My} \wedge \text{Rs} \wedge \text{Rv}) \mid \\ (\text{Rc} \wedge \text{Rs} \wedge \text{Ry}) \mid (\text{Rs} \wedge \text{Rv} \wedge \text{Ry})$$

Key distribution corruption

We have agreement on 3rd message ***unless*** adversary:

- compromises initiator's static key distribution **AND** gets psk
⇒ **Key distribution has an impact on security !**

Illustration with agreement on 3rd message

Extract, compute DNF. Requires the use of symbols:

- D_u, D_v : adversary corrupts public keys distribution
 - $R_u, R_v, R_x, R_y, R_s, R_c$: adversary gets private keys (u, v, x, y) , psk (s) or precomp. value (c)
 - $M_u, M_v, M_x, M_y, M_s, M_i, M_r$: adversary sets private keys (u, v, x, y) , psk (s) or precomp value $(i$ for Initiator, r for Responder)

```

DNF = (Du & Rs) | (Ms & Ru) | (Mu & Rs) | (Rs & Ru) | (Mi & Ms & Ry) | (Mi & My & Rs) | (Mi & Rs & Ry) |
(Mr & Ms & Ry) | (Mr & My & Rs) | (Mr & Rs & Ry) | (Ms & Mv & Ry) | (Ms & My & Rc) | (Ms & My & Rv) | 
(Ms & Rc & Ry) | (Ms & Rv & Ry) | (Mv & My & Rs) | (Mv & Rs & Ry) | (My & Rc & Rs) | (My & Rs & Rv) | 
(Rc & Rs & Ry) | (Rs & Rv & Ry)

```

Precomputation

We have agreement on 3rd message ***unless*** adversary:

- sets initiator's precomputation **AND** sets psk **AND** gets responder's ephemeral private key
 - **OR** ...
 - **OR** gets precomputation value **AND** gets psk **AND** gets responder's ephemeral private key

Illustration with agreement on 3rd message

Extract, compute DNF. Requires the use of symbols:

- D_u, D_v : adversary corrupts public keys distribution
 - $R_u, R_v, R_x, R_y, R_s, R_c$: adversary gets private keys (u, v, x, y) , psk (s) or precomp. value (c)
 - $M_u, M_v, M_x, M_y, M_s, M_i, M_r$: adversary sets private keys (u, v, x, y) , psk (s) or precomp value $(i$ for Initiator, r for Responder)

$\text{DNF} = (\text{Du} \wedge \text{Rs}) \mid (\text{Ms} \wedge \text{Ru}) \mid (\text{Mu} \wedge \text{Rs}) \mid (\text{Rs} \wedge \text{Ru}) \mid (\text{Mi} \wedge \text{Ms} \wedge \text{Ry}) \mid (\text{Mi} \wedge \text{My} \wedge \text{Rs}) \mid (\text{Mi} \wedge \text{Rs} \wedge \text{Ry}) \mid$
 $(\text{Mr} \wedge \text{Ms} \wedge \text{Ry}) \mid (\text{Mr} \wedge \text{My} \wedge \text{Rs}) \mid (\text{Mr} \wedge \text{Rs} \wedge \text{Ry}) \mid (\text{Ms} \wedge \text{Mv} \wedge \text{Ry}) \mid (\text{Ms} \wedge \text{My} \wedge \text{Rc}) \mid (\text{Ms} \wedge \text{My} \wedge \text{Rv}) \mid$
 $(\text{Ms} \wedge \text{Rc} \wedge \text{Ry}) \mid (\text{Ms} \wedge \text{Rv} \wedge \text{Ry}) \mid (\text{Mv} \wedge \text{My} \wedge \text{Rs}) \mid (\text{Mv} \wedge \text{Rs} \wedge \text{Ry}) \mid (\text{My} \wedge \text{Rc} \wedge \text{Rs}) \mid (\text{My} \wedge \text{Rs} \wedge \text{Rv}) \mid$
 $(\text{Rc} \wedge \text{Rs} \wedge \text{Ry}) \mid (\text{Rs} \wedge \text{Rv} \wedge \text{Ry})$

Precomputation

In some cases, R_c has the same impact as M_v or R_v , although R_c is *weaker* than M_v or R_v .

⇒ Precomputation has a negative impact on security !

Illustration with agreement on 3rd message

Extract, compute DNF. Requires the use of symbols:

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 - $R_u, R_v, R_x, R_y, R_s, R_c$: adversary gets private keys (u, v, x, y) , psk (s) or precomp. value (c)
 - $M_u, M_v, M_x, M_y, M_s, M_i, M_r$: adversary sets private keys (u, v, x, y) , psk (s) or precomp value $(i$ for Initiator, r for Responder)

$$\begin{aligned} DNF = & (Du \wedge Rs) \mid (Ms \wedge Ru) \mid (Mu \wedge Rs) \mid (\textcolor{red}{Rs \wedge Ru}) \mid (Mi \wedge Ms \wedge Ry) \mid (Mi \wedge My \wedge Rs) \mid (Mi \wedge Rs \wedge Ry) \mid \\ & (Mr \wedge Ms \wedge Ry) \mid (Mr \wedge My \wedge Rs) \mid (Mr \wedge Rs \wedge Ry) \mid (Ms \wedge Mv \wedge Ry) \mid (Ms \wedge My \wedge Rc) \mid (Ms \wedge My \wedge Rv) \mid \\ & (Ms \wedge Rc \wedge Ry) \mid (Ms \wedge Rv \wedge Ry) \mid (Mv \wedge My \wedge Rs) \mid (Mv \wedge Rs \wedge Ry) \mid (My \wedge Rc \wedge Rs) \mid (My \wedge Rs \wedge Rv) \mid \\ & (Rc \wedge Rs \wedge Ry) \mid (\textcolor{red}{Rs \wedge Rv \wedge Ry}) \end{aligned}$$

Comparison with previous work

- 2018: J. A. Donenfeld and K. Milner, “Formal verification of the WireGuard protocol” (*Symbolic WireGuard*)

⇒ More accurate analysis !

Illustration with agreement on 3rd message

Extract, compute DNF. Requires the use of symbols:

- D_u, D_v : adversary corrupts public keys distribution
 - $R_u, R_v, R_x, R_y, R_s, R_c$: adversary gets private keys (u, v, x, y) , psk (s) or precomp. value (c)
 - $M_u, M_v, M_x, M_y, M_s, M_i, M_r$: adversary sets private keys (u, v, x, y) , psk (s) or precomp value $(i$ for Initiator, r for Responder)

$$\text{DNF} = (\text{Du} \wedge \text{Rs}) \mid (\text{Ms} \wedge \text{Ru}) \mid (\text{Mu} \wedge \text{Rs}) \mid (\text{Rs} \wedge \text{Ru}) \mid (\text{Mi} \wedge \text{Ms} \wedge \text{Ry}) \mid (\text{Mi} \wedge \text{My} \wedge \text{Rs}) \mid (\text{Mi} \wedge \text{Rs} \wedge \text{Ry}) \mid \\ (\text{Mr} \wedge \text{Ms} \wedge \text{Ry}) \mid (\text{Mr} \wedge \text{My} \wedge \text{Rs}) \mid (\text{Mr} \wedge \text{Rs} \wedge \text{Ry}) \mid (\text{Ms} \wedge \text{Mv} \wedge \text{Ry}) \mid (\text{Ms} \wedge \text{My} \wedge \text{Rc}) \mid (\text{Ms} \wedge \text{My} \wedge \text{Rv}) \mid \\ (\text{Ms} \wedge \text{Rc} \wedge \text{Ry}) \mid (\text{Ms} \wedge \text{Rv} \wedge \text{Ry}) \mid (\text{Mv} \wedge \text{My} \wedge \text{Rs}) \mid (\text{Mv} \wedge \text{Rs} \wedge \text{Ry}) \mid (\text{My} \wedge \text{Rc} \wedge \text{Rs}) \mid (\text{My} \wedge \text{Rs} \wedge \text{Rv}) \mid \\ (\text{Rc} \wedge \text{Rs} \wedge \text{Ry}) \mid (\text{Rs} \wedge \text{Rv} \wedge \text{Ry})$$



Performances

- ▶ Evaluate **4860** queries $\approx 14,5$ hours (with 5 parallel sets)
 - ▶ Compute DNF: ≈ 2 hours (compute first CNF, then DNF(CNF))

Conclusion

- ▶ Work still in progress, next steps:
 - ▶ Analyse "false" queries
 - ▶ Link with TAMARIN prover
 - ▶ Mount concrete attacks
 - ▶ Verified properties:
 - ▶ Agreement
 - ▶ Key and message secrecy
 - ▶ Anonymity
 - ▶ Contributions:
 - ▶ Complete model of WireGuard
 - ▶ Precise threat model, including initial key distribution and precomputations
 - ▶ Process with SAPIC⁺, PROVERIF, TAMARIN